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Shock compression of liquid nitrogen

Thermodynamic analysis of new experimental data in megabar range



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Shock compression of liquid nitrogen

(new experimental data in megabar pressure range)

Mochalov M., Zhernokletov M., Il'kaev R., Mikhailov A., Mezhevov A., Kovalev A., Kirshanov S., Grigorieva Yu., Novikov M., Shuikin A., Fortov V., Gryaznov V., Iosilevskiy I.

JETP, 137, 77 (2010)

Density, temperature and **electroconductivity** measurements in shock compressed condensed **nitrogen** at megabar pressure

Trunin R., Boriskov G., Bykov A., Medvedev A., Simakov G., Shuikin A. JETP Letters, 88 (3), 189 (2008)

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Shock compression of condensed nitrogen at megabar pressure



<u>Collaboration:</u> Eugene & Lidia Yakyb (Odessa University, Ukraine)

Shock Hugoniot of liquid nitrogen

(primary experimental data in kinematic variables)



JETF Letters, **88**, 220 (2008)

Shock Hugoniot of liquid nitrogen

(experimental data in thermodynamic variables)



Internal energy is close to be linear function of pressure!



The region of approximate constancy for Gruneizen parameter $\Rightarrow \rho \approx 3.3 \pm 0.1$ g/cc 90 < P < 330 GPa

Temperature of shock compressed nitrogen

measurements of thermal equation of state



★ - Experiment (Mochalov M., Zhernokletov M. et al., JETF 137, 77 (2010)

2 – linear approximation of experimental data ($P \approx 90 - 300 \text{ }\Gamma\Pi a$)

Temperature is close to be linear function of pressure

+ isochoric behavior of nitrogen Hugoniot



Id. gas N⁺ + e: Z= **2.0**

What does it mean?

High-temperature part of nitrogen Hugoniot

Internal energy ~ linear function on temperature at isochore



Isochoric heat capacity (*C_V*) **is almost constant on nitrogen isochore**

$$C_v \equiv (\partial E / \partial T)_v \approx const \approx 2.0 \text{ (J/gK)}$$

$$C_V/R_N \approx 3.5$$

What does it mean?

Constancy of Grüneizen parameter and Heat capacity at isochore



Gr \approx *const* + **C**_V \approx *const* \Leftrightarrow thermal pressure coefficient $\gamma_v^* \approx const$

NB!
$$(\partial p/\partial T)_v \approx 4.54 \text{ GPa/K}$$
!

$$\gamma_v^* \equiv (v/k_{\rm B}) (\partial p/\partial T)_v \approx const \approx$$

Summary

Thermodynamics of shock compressed nitrogen

High-temperature part nitrogen Hugoniot is close to be isochoric

 $\rho \approx 3.3 \pm 0.1 \text{ g/cc}$ (90 < P < 330 GPa)

Internal energy is almost linear on pressure at isochore

 $\operatorname{Gr} = V(\partial P/\partial E)_V \approx const \approx 0.62$

Temperature is almost linear on pressure at isochore

 $(\partial p/\partial T)_V \approx const \approx 4.54 \text{ (GPa/K)}$

$$Z \equiv PV/RT \equiv P/n_{\rm N}kT \approx const \approx 2.66 \pm 0.20$$

Internal energy is almost linear on temperature at isochore

$$C_V \equiv (\partial E / \partial T)_V \approx const \approx 2.06 \text{ (J/g·K)}$$

Mochalov M., Zhernokletov M. *et al.*, *JETF* **137**, 77 (2010) Trunin R., Boriskov G., Bykov A., Medvedev A. JETF Letters, **88**, 220 (2008)

Expected behavior of nitrogen Hugoniot M.Ross & F.Rogers



FIG. 6. Nitrogen Hugoniot calculated to extreme conditions, plotted as pressure versus compression (V_0/V) . V_0 is the initial liquid volume. Experimental data (filled circles) (Ref. 11), connected to ACTEX calculations (solid curve) by a smoothed interpolation (long-dashed curve). The small dashed line locates approximately the liquid molecular-polymer transition.

New experiments vs expected behavior of nitrogen Hugoniot



Nitrogen Hugoniot problem in plasma state – what do we need?



Nitrogen Hugoniot (comes trough polymeric phase **?**)



Ab initio calculations - DFT/MD



Ab initio calculations - DFT/MD



DFT/MD: Scandolo S. *PNAS* **100**, (2003) // Bonev S., Militzer B., Galli G. *PRB* **69** (2004) WPMD : Jakob B. *et al. PRE* (2007) // DFT/MD: Morales M. *et al. PNAS* **107**, (2010)/ DFT/MD: Lorenzen W. *et al. PRB* (2010)

Nitrogen phase diagram in the region of polymerization



 $\mathbf{Gr} > 0 // \mathbf{Gr} < 0$ – domains of positive and negative sign of Grüneisen coefficient { $\mathbf{Gr} = V(\partial P / \partial E)_V$ }

hypothetical boundary between polymeric and non-ideal plasma states (1st-order phase transition or continuous **?**)

•••• the same as "smoothed" phase transition

B. Boates & S. Bonev, Phys. Rev. Lett. 102 (2009)

Ab initio calculations

 DFT/MD – calculation of of polymer molecule boundary in liquid nitrogen (S.Bonev et al. – 2009)

Phase Diagram of Dense Nitrogen (summary)



* - Mochalov M., Zhernokletov M. et al., JETP 137, 77 (2010) // * - Trunin R., Boriskov G., Bykov A., Medvedev A. JETP Letters, 88, 220 (2008)

Comments

microphysics





<u>Figures after Eugene Yakub: "Non-simple problems for simple molecules</u>" FAIR-Russia School «*Physics of high energy density in matter*» December 2009, Moscow

Polymeric nitrogen - structure



F.Zahariev, A.Hu, J.Hooper, F.Zhang, &T.Woo. Phys.Rev. B 72, 214108 (2005)

Simple molecular models

First estimations of molecular-polymeric transition



Plasma model for nitrogen thermodynamics (code SAHA-N)

Shock compression of nitrogen

(chemical picture) SAHA-code

Gryaznov, Iosilevskiy (1970-2010)

Equilibrium composition: $\{N_2, N, N^+, e, N_2^+, N^-\}$

Coulomb interaction:

Modified pseudopotential model for partially ionized plasma (*I. Iosilevskiy 1980-2010*)

Short range repulsion:

"Soft Spheres" approximation (*D. Young*) modified for <u>mixture</u> of soft spheres with <u>different radii</u> – shift of dissociation level.



Basic points:

- All assumption are provided at micro-level.
- Input: Choice of Φ_{ie} , Φ_{ii} and Φ_{ee} pseudopotentials.
- Input: Approximations for binary correlation functions
- Strong correlation of the pseudopotentials for "free" charges and upper energy level for partition functions for bound states.
- Priority for general equalities (*normalizing conditions*) valid independently on degree of non-ideality.
- Non-ideality corrections through the correlation functions and general equalities, valid for Coulomb interaction.

<u>**Key parameter**</u> – ratio of intrinsic volumes: *molecule /atom / ion*: $R(N)/R(N_2) = 0.63$ - *in accordance with recommendations of "Atom-atomic approximation"* of E.Yakub, *LT*, 1993

Coulomb Corrections for Free Charge Subsystem

Modified Pseudopotential Approximation (*):



Binary *i-i*, *i-e*, *e-e* correlation functions



The <u>form</u> of *i-i, i-e, e-e* binary correlation functions - «ring» (Debye) approximation with potential $\Phi_{ie}^{*}(r)$

$$F_{ab}(r) = 1 \pm A \frac{\mathrm{e}^{-pr} - \mathrm{e}^{-qr}}{r} \equiv 1 \pm \Psi_0 \mathrm{e}^{-\nu r} \frac{\mathrm{sh}\{\omega r\}}{\omega r}$$

"Zero and second moment" conditions (*Stillinger & Lovett*)

$$n\int [F_{+}(r) - F_{-}(r)]d\mathbf{r} = 1 \qquad n\int [F_{+}(r) - F_{-}(r)]\left(\frac{r^{2}}{r_{D}^{2}}\right)d\mathbf{r} = 3$$

Positive sign of all correlation functions

 $\iff F_{ab}(r) > 0$

(*) Iosilevskiy I. *High Temp*. 18 (1980) // in: "Encyclopedia of Low-T Plasma" (Suppl.), Moscow: FIZMATLIT, 2004, pp. 349

Thermodynamic contributions in modified pseudopotential model for Coulomb corrections

$$\Phi_{ie}^{*}(r) = -\frac{Z_{i}e^{2}}{r}(1 - e^{-r/\sigma}) \equiv -\left(\frac{Z_{i}e^{2}}{\sigma}\right)\frac{(1 - e^{-r/\sigma})}{r/\sigma} \ge -\Phi_{ie}^{*}(0) \sim -\varepsilon \qquad \iff \qquad F_{ab}(r) = 1 \pm A \frac{e^{-pr} - e^{qr}}{r} \equiv 1 \pm \Psi_{0}e^{-rr} \frac{sh\omega r}{\omega r}$$
Pseudopotentials
Correlation Functions
Homogeneity of Coulomb potential
$$\Leftrightarrow \qquad \qquad Pressure Correction - \Delta P$$

$$U = U_{Kin} + U_{Pot} \qquad 3PV = 2U_{Kin} + U_{Pot}$$
Total Energy correction
$$\Delta U = -Vn^{2}\int (F_{+}\Phi_{ei}^{*} - F_{-}\Phi_{ii}^{*})d\mathbf{r}$$
Approximate relation between Coulomb corrections
for chemical potential and energy (\Delta\mu \Leftrightarrow \Delta U/N)
$$\Delta U_{pot} = -Vn\int \Phi_{coul}(F_{+} - F_{-})d\mathbf{r}$$

<u>NB</u> !

Positive shift in average kinetic energy due to non-ideality of free charges subsystem $\Delta U_{kin} = 3\Delta PV - \Delta U$

Well-known relation between pressure and energy corrections for <u>free charges subsystem</u> $\Delta U = 3\Delta PV$

which is valid at weak non-ideality ($\Gamma \ll 1$), is <u>no longer valid</u> in strong non-ideality conditions ($\Gamma \sim 1$)

It is equivalent to additional effective electron-ion repulsion

(in comparison with ordinary one-parametric Coulomb corrections, depending on non-ideality parameter only

 $\Delta F/NkT = f(\Gamma)$

Experimental data \Leftrightarrow Theoretical models

(comparison)

Summary

Thermodynamics of shock compressed nitrogen (primary thermodynamic results of experiment)

High-temperature part of Hugoniot is close to isochore

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Check of theoretical models

Quasi-isochoric behavior of nitrogen Hugoniot



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Thermodynamics of shock compressed nitrogen

Quasi-linear behavior of *E(p)* **at Q** = *const*

Hugoniot: ~ $\rho \approx const$ (3.3 ± 0.1 g/cc)



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Temperature of shock compressed nitrogen General P-T diagram



Quasi-linear behavior of *T*(*p*) at *Q* = *const*

Electroconductivity of shock compressed nitrogen



Electroconductivity of shock compressed nitrogen



Quasi-isentropic Plane Compression of Matter at Megabar Pressures by Using of a Layered System to Diminish First Shock Wave Intensity

Ternovoi V., Pyalling A., Filimonovet A. (05.2010)

Summary and conclusion

Explosive driven quasi-isentropic compression generators were proposed for matter investigation in the megabar pressure region. Results of the first experiments on quasi-isentropic compression of liquid nitrogen are presented. It was shown, that **pressure ionization** of nitrogen proceeds at **densities** from **3.15 to 3.4 g/cc** at a **temperature** of about **3000 K**. Diminishing of temperature growth was measured during onset of nitrogen electrical conductivity.

Perspectives

Modelling

Improvement of Plasma model (SAHA-code):

- From EOS of soft spheres to EOS of {exp - 6} potential system

Improvement of Polymeric models (E. & L. Yakub):

- Calibration of both model on results of ab initio calculations (DFT/MD)

<u>Collaboration</u> (*Gryaznov, Iosilevskiy* ⇔ *E.* & *L. Yakub*)

- Incorporation of polymeric state model into SAHA-code

<u>New approaches are desirable</u>: (*new calculations and comparisons*)

- <u>Ab initio</u>: **RPIMC**, **DPIMC** // **DFT/MD** // WPMD // TBM . . .
- <u>Wigner-Zeits cell model</u>: TFC, MHFS, ...
 -
- Semiempirical (wide-range) EOS-s
 - • • •

Perspectives (new experiments)

- ! Strong shock compression of liquid nitrogen at high pressure (P > 3 Mbar)
- ! Strong shock compression of solid nitrogen at high pressure (P > 3 Mbar)
- Strong shock compression of pre-compressed gaseous nitrogen at high pressure (mesurement of series of Hugoniots with varying initial densities (like in VNIIEF experiments with deuterium)
- **! Strong isentropic compression of nitrogen by explosive at Mb pressure** search of density discontinuity (hypothetical phase transition ?) on nitrogen isentrope(s) (like in VNIIEF's experiments with deuterium (M.Mochalov, V.Fortov et al. PRL, 2007)

Exotics:

.

! - Heavy Ion Beam and Laser heating of cryogenic nitrogen

Conclusions

- New experimental data on shock compression of cryogenic liquid nitrogen in megabar pressure range "open new page" in investigation of properties for warm dense matter of "simple" molecular gases
- **Simultaneous** measurement of **caloric** and **thermal** equation of state (EOS) *(pressure, density, temperature and internal energy)* on the same Hugoniot give powerful tool for **checking** theoretical **models** and "calibration" of wide-range EOS-*s*
- New experimental data in nitrogen may be considered as the thermodynamic manifestation of non-standard form of pressure ionization (*from polymeric to plasma state*)
- This new form of **pressure ionization** (*from polymeric to plasma state*) seems to be **general**, **universal** and **interesting** phenomenon
- It is promising to continue and extend experimental investigation of pressure ionization of polymeric state
- It is promising to study pressure ionization of polymeric state in direct numerical simulations ("*numerical experiment*") DFT_MD, PIMC, WP_MD...



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Thank you!



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