

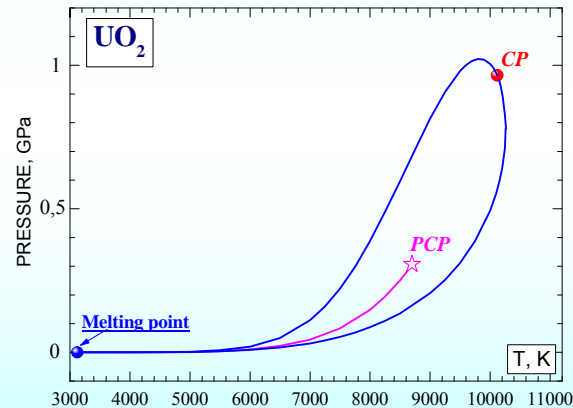


Seminar for young scientists  
**Physics of high energy density in matter**  
*FAIR-Russia Research Centre,*  
*Moscow, 21-22 November 2011*



# Non-congruent Phase Transitions

*in Cosmic Matter and Laboratory*



Igor Iosilevskiy

*Joint Institute for High Temperature (Russian Academy of Science)*  
*Moscow Institute of Physics and Technology (State University)*



# Content

Non-congruence in general

The base: Non-congruent phase transition in U-O system

Non-congruence in terrestrial and planetary applications

Non-congruence in exotic situations (compact stars)

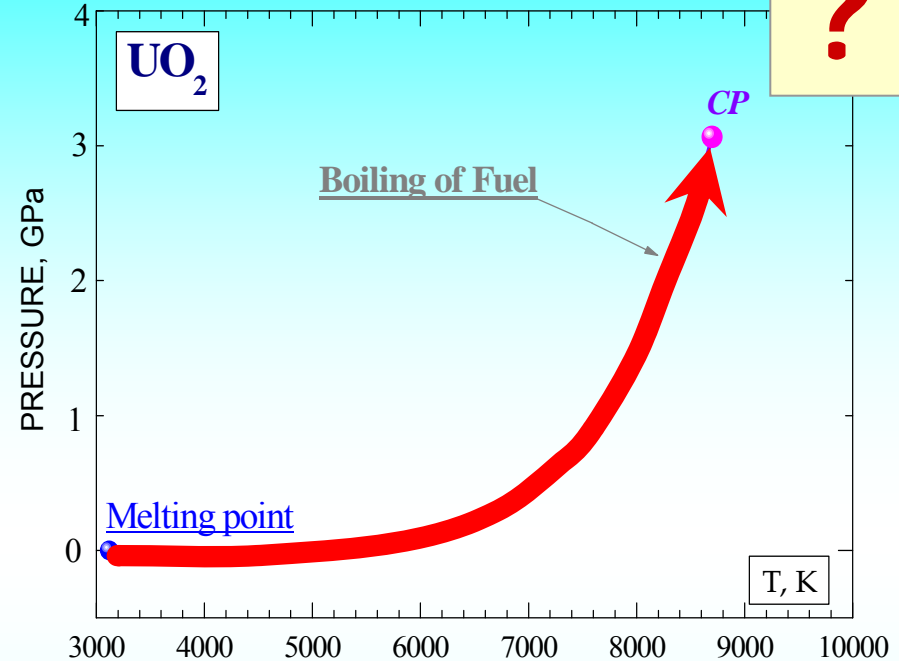
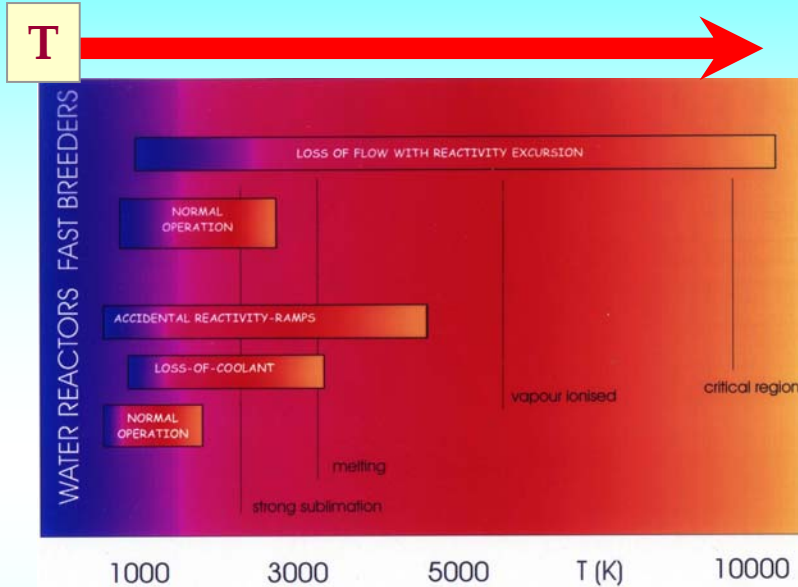
Summary

## The base

**Non-congruent phase transitions  
in chemically reacting U-O plasma**

# Non-congruent phase transition in uranium dioxide

Expected temperature at hypothetical severe accident at fast-breeder nuclear reactor



## INTAS Project (1995–2002)

Cooperation: MIPT – IHED RAS – IPCP RAS – OSEU – MPEI ⇔ ITU (JRC, Germany)

Project Coordinator – **C. Ronchi** (ITU, JRC) ⇔ Project Supervisor – **V. Fortov**

## ISTC Project (2002–2005)

Cooperation: MIPT – IHED RAS – IPCP RAS – ITEP – VNIIEF ⇔ GSI (JRC, Germany)

Project Manager – **B. Sharkov** (ITEP, Moscow) ⇔ Project Science Supervisor – **V. Fortov**

## Two stages

- **Construction of Equation of State (EOS)**

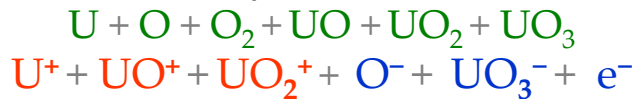
- **Phase coexistence parameters calculation**

# Quasi-chemical representation

("Chemical picture")

## Multi-molecular model

(*Liquid & Gas*)



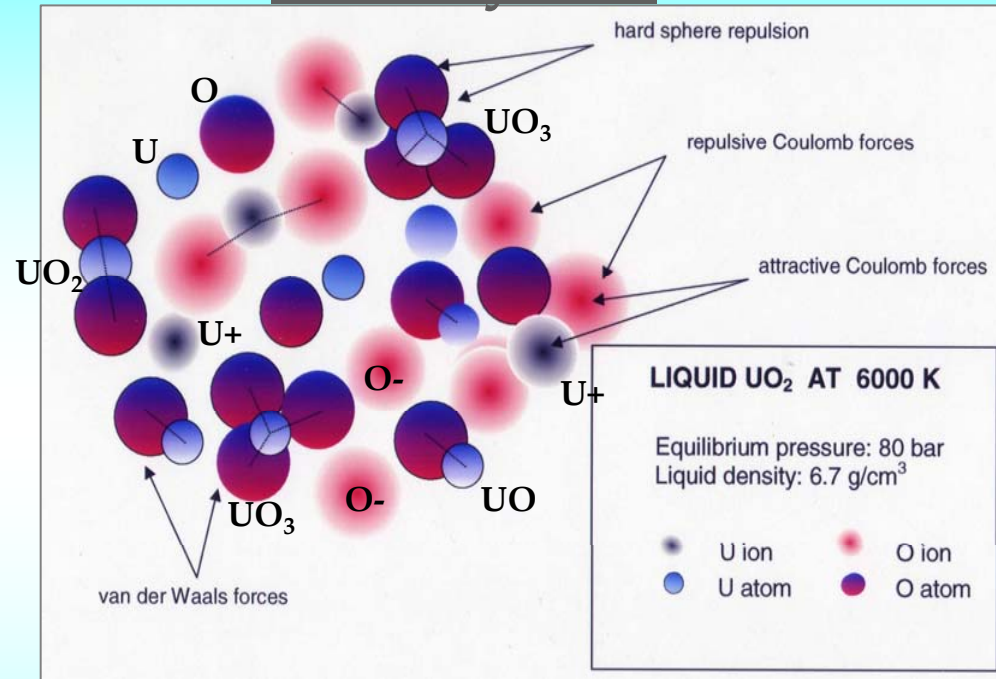
### Interactions: (*Pseudopotential components*)

- Intensive short-range repulsion
- Coulomb interaction between charged particles
- Short-range effective attraction between all particles

### Interaction corrections: (*Modified for mixtures*)

- Hard-sphere mixture with varying diameters
- Modified Mean Spherical Approximation
- Modified Thermodynamic Perturbation Theory

## U - O system



\* I.L.I., Yakub E., Hyland G., Ronchi C. *Trans. Amer. Nucl. Soc.* **81** (1999) // *Int. Journ. Thermophysics* **22** (2001)

\* I.L.I., Gryaznov V., Yakub E., Ronchi C., Fortov V. *Contrib. Plasma Phys.* **43**, (2003)

\* Ronchi C., I.L.I., Yakub E. *Equation of State of Uranium Dioxide* / Springer, Berlin, (2004)

\* I.L.I., Gryaznov V., Semenov A.M., Yakub E., Fortov V. Ronchi C., Hyland G., *High Temperature* **48**, (2010)

\* I.L.I., Son E., Fortov V. *Thermophysics of non-ideal plasmas*. MIPT (2000); FIZMATLIT, (2011)

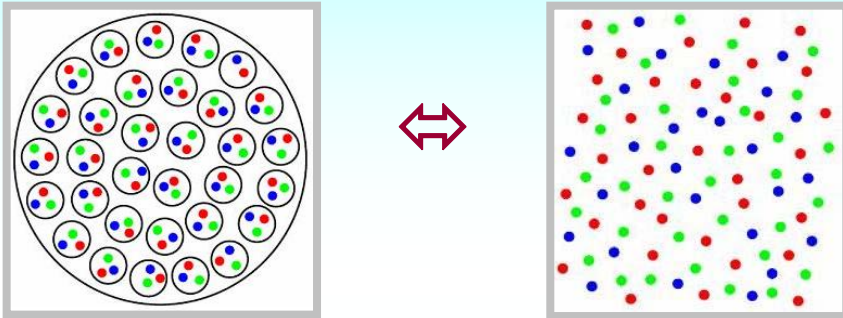
# Quasi-chemical representation

("Chemical picture" - in plasma community)

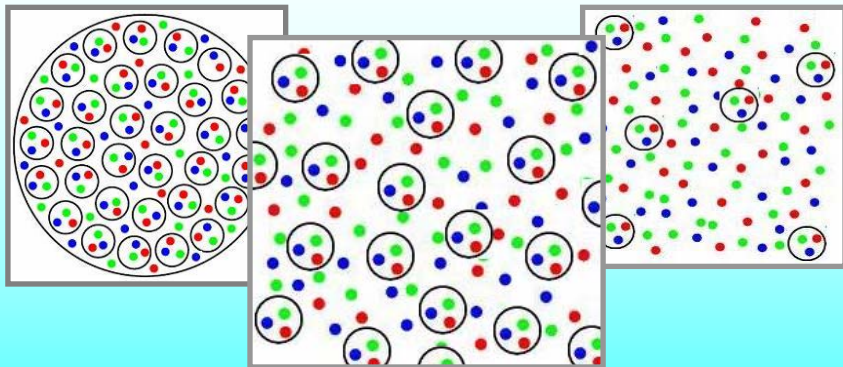
## Strange (hybrid) stars

Different EOS for coexisting phases

No critical point !



Unique EOS for coexisting phases



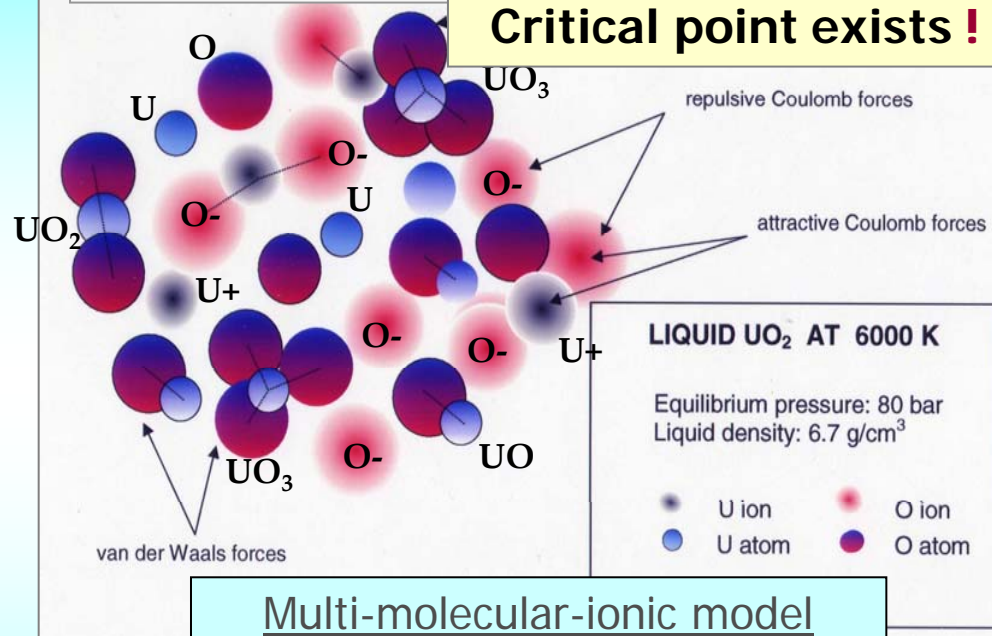
Critical point exists !

Why not ?

## U - O system

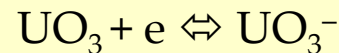
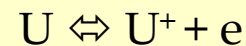
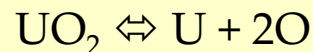
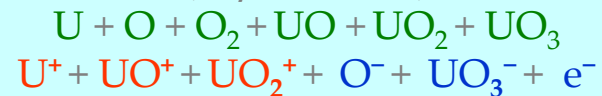
Unique EOS for coexisting phases

Critical point exists !



Multi-molecular-ionic model

(Liquid & Gas)



.....

$$\mu_{UO_2} = \mu_U + 2\mu_O$$

$$\mu_{O_2} = 2\mu_O$$

$$\mu_U = \mu_{U^+} + \mu_e$$

$$\mu_{UO_3} + \mu_e = \mu_{UO_3^-}$$

.....

# Two problems in phase transition calculation

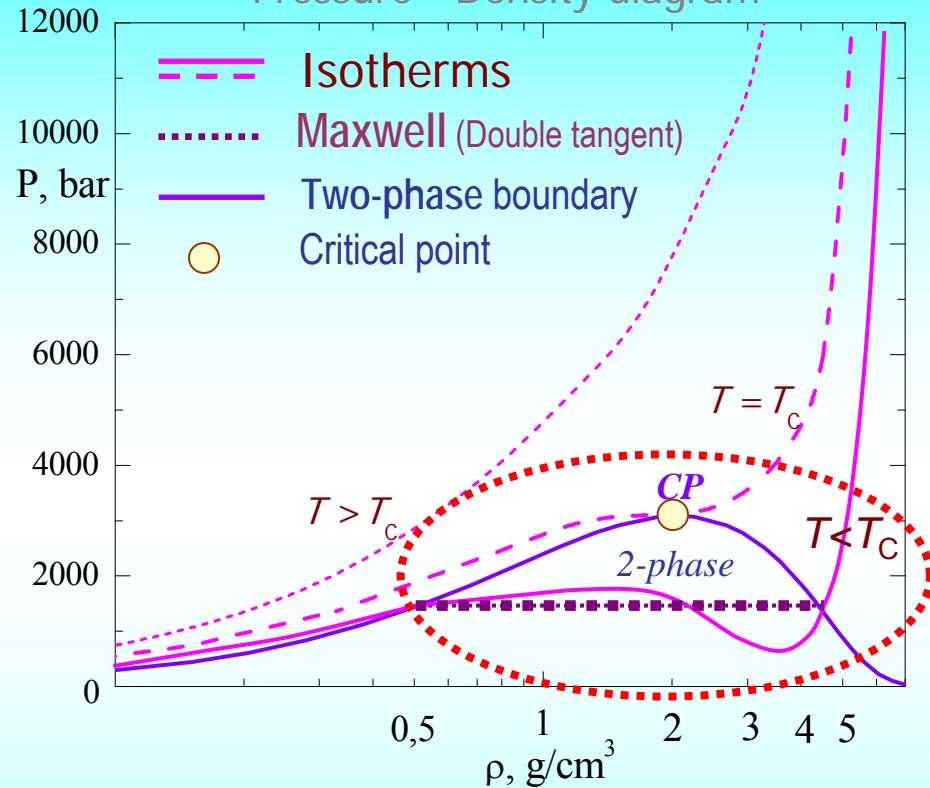
- Construction of Equation of State (EOS)

**- Phase coexistence parameters calculation**

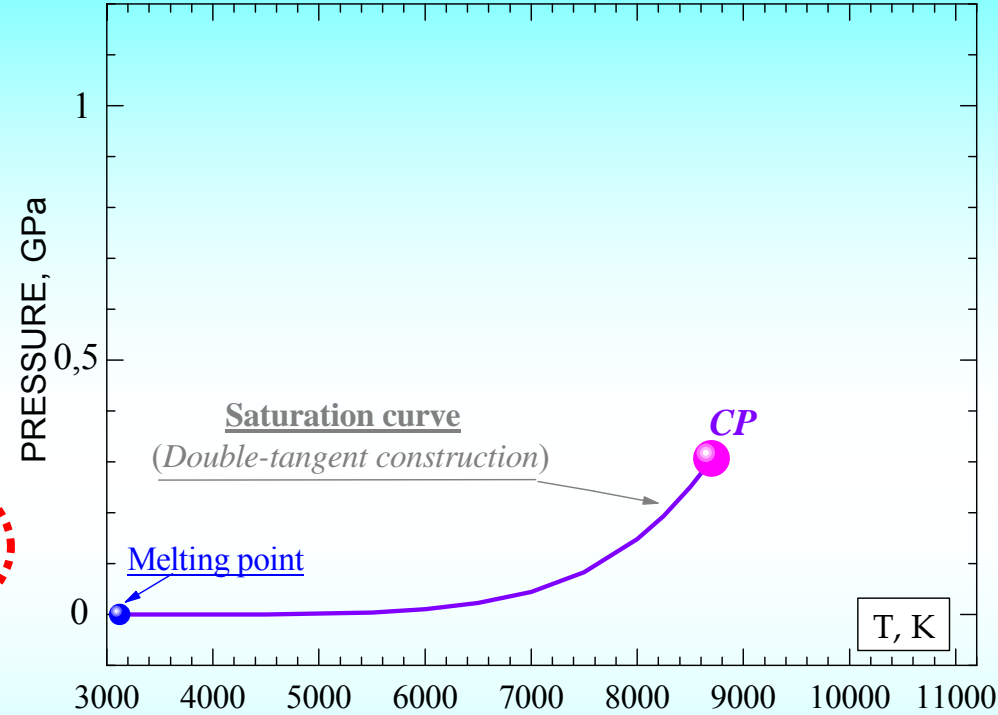
# Standard

## Congruent evaporation in U-O system

Pressure - Density diagram



Pressure - Temperature diagram



- Stoichiometry of coexisting phases are equal:  $x' = x''$
- Van der Waals loops (at  $T < T_c$ ) corrected via the “double tangent construction”
- Standard phase equilibrium conditions:

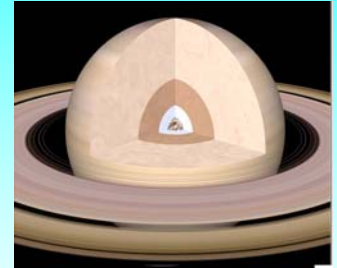
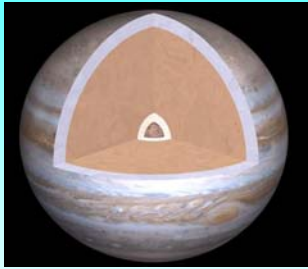
$$P' = P'' \quad // \quad T' = T'' \quad // \quad G'(P, T, x) = G''(P, T, x)$$

- Standard critical point:

$$(\partial P / \partial V)_T = 0 \quad // \quad (\partial^2 P / \partial V^2)_T = 0 \quad // \quad (\partial^3 P / \partial V^3)_T < 0$$



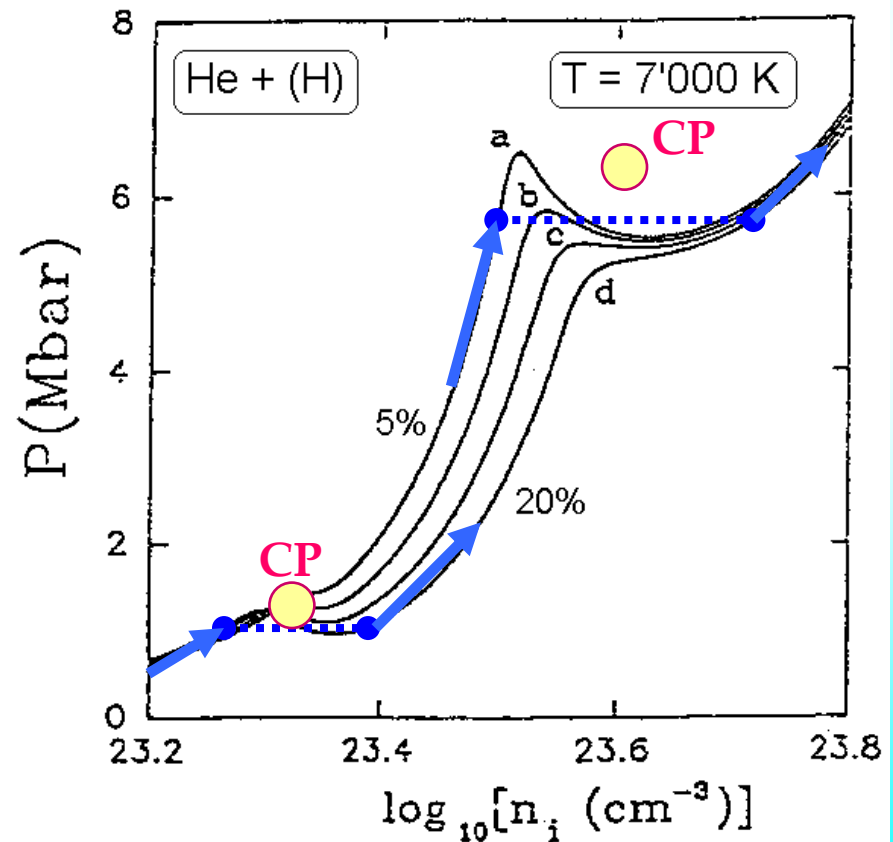
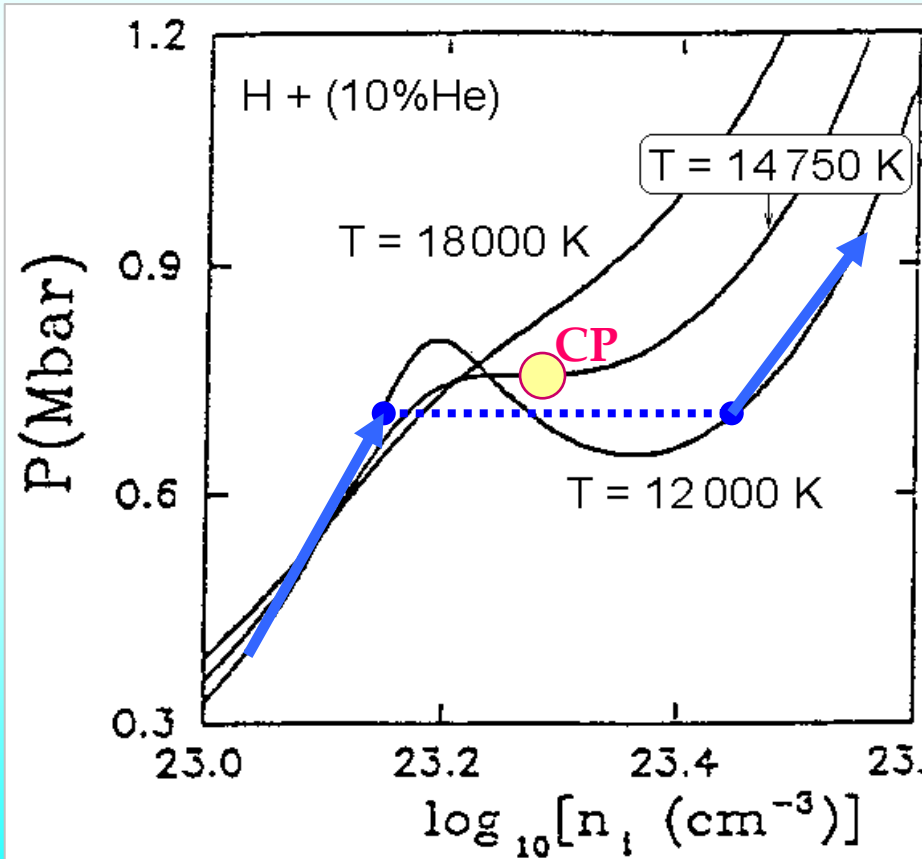
# Plasma Phase Transitions in H<sub>2</sub> + He plasma (planetary science)



Contrib. Plasma Phys. 35 (1995) 2, 109–125

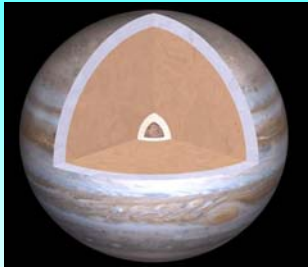
Plasma Phase Transition  
in Fluid Hydrogen-Helium Mixtures

M. SCHLANGES (a), M. BONITZ (b), and A. TSCHTTSCHJAN (b)



# Plasma Phase Transitions in $H_2 + He$ plasma

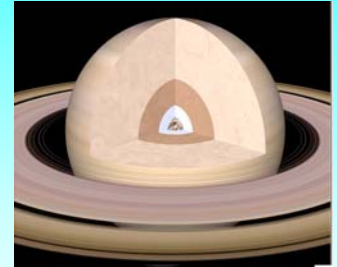
(continued)



Contrib. Plasma Phys. 35 (1995) 2, 109–125

Plasma Phase Transition  
in Fluid Hydrogen-Helium Mixtures

M. SCHLANGES (a), M. BONITZ (b), and A. TSCHTTSCHJAN (b)



M. SCHLANGES, M. BONITZ, and A. TSCHTTSCHJAN

123

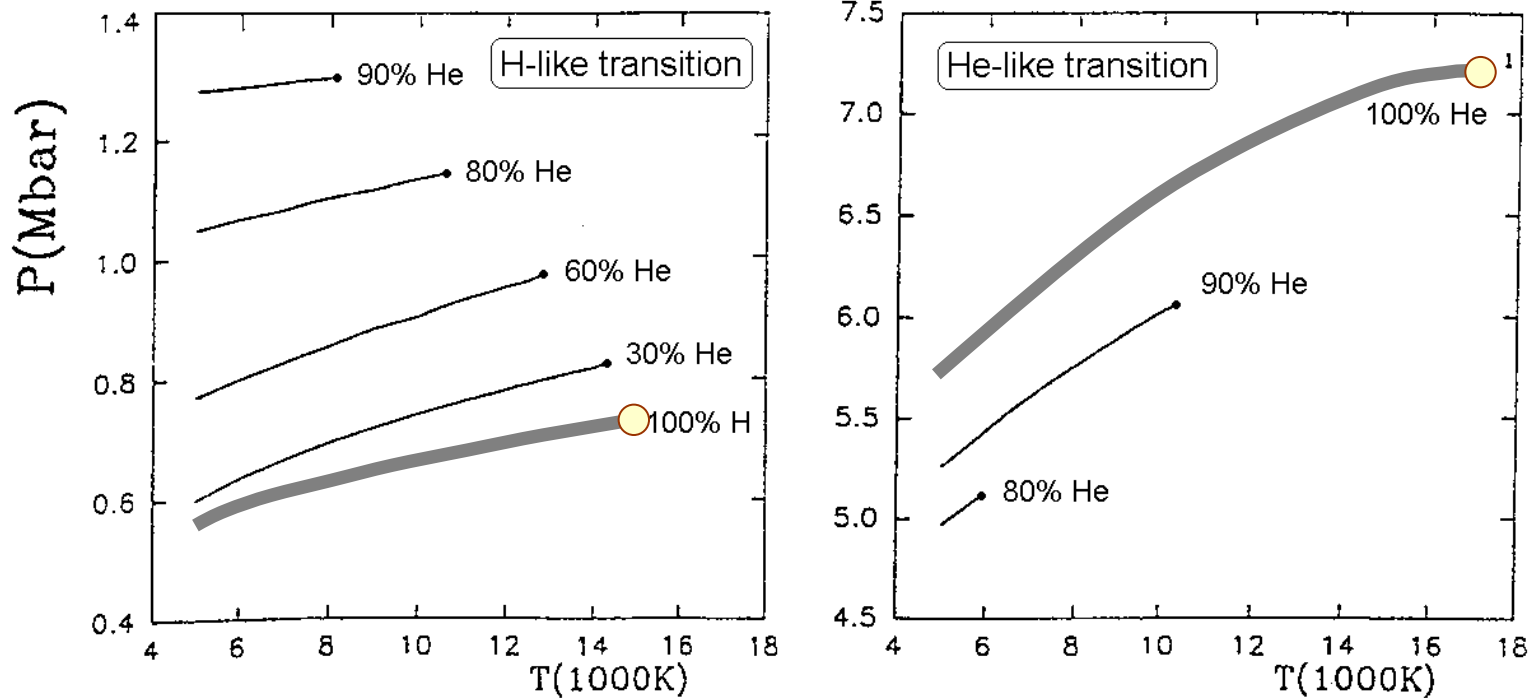
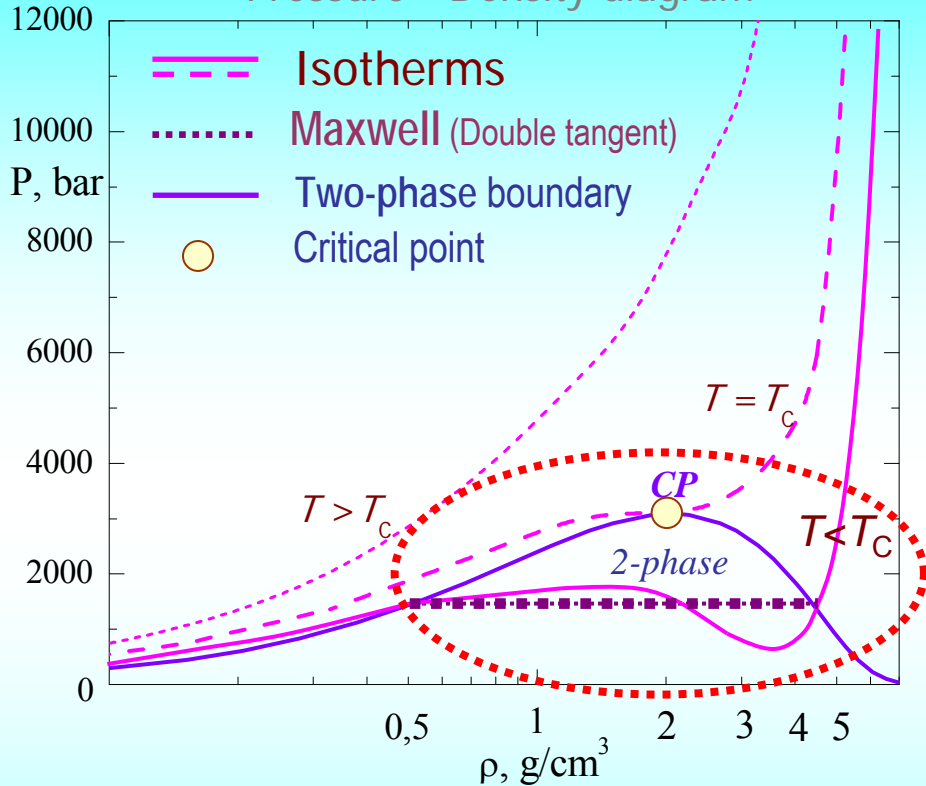


Fig. 7. Coexistence pressure for H–He mixtures for different values of the mixing parameter, for the hydrogen-like plasma phase transition and for the helium-like plasma phase transition.

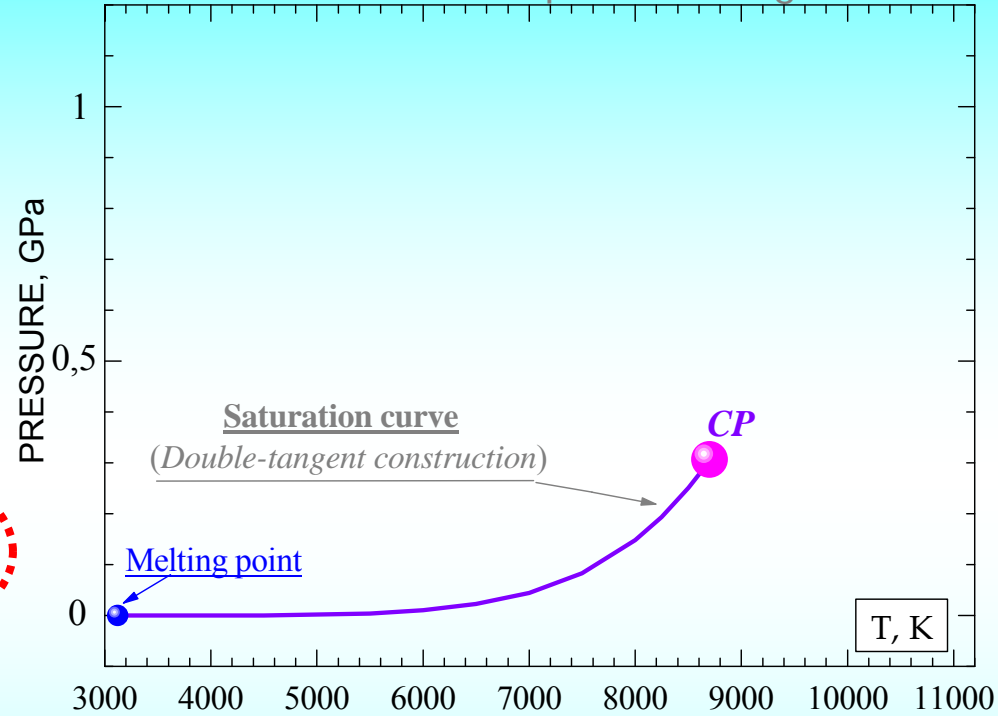
# Standard

## Congruent evaporation in U-O system

Pressure - Density diagram



Pressure - Temperature diagram



- Stoichiometry of coexisting phases are equal:

$$x' = x''$$

It should be

$$x' \neq x''$$

- Van der Waals loops (at  $T < T_c$ ) corrected via the “double tangent construction”

It should be

- Standard phase equilibrium conditions:

$$P' = P'' \quad \parallel \quad T' = T'' \quad \parallel \quad G'(P, T, x) = G''(P, T, x)$$

$$\mu_1'(P, T, x') = \mu_1''(P, T, x'')$$

$$\mu_2'(P, T, x') = \mu_2''(P, T, x'')$$

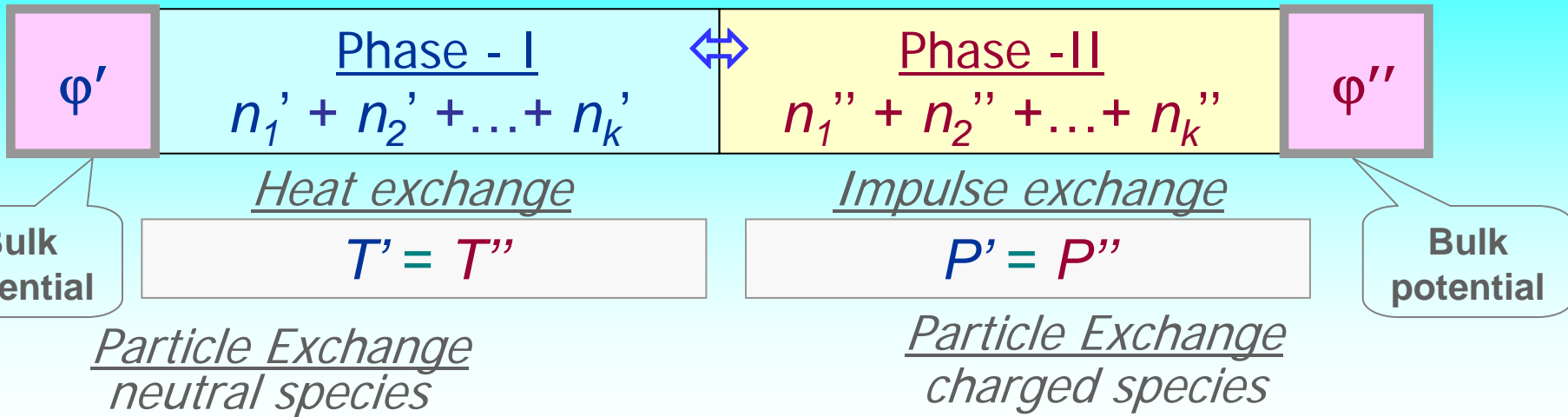
.....

$$\mu_k'(P, T, x') = \mu_k''(P, T, x'')$$

- Standard critical point:

$$(\partial P / \partial V)_T = 0 \quad \parallel \quad (\partial^2 P / \partial V^2)_T = 0 \quad \parallel \quad (\partial^3 P / \partial V^3)_T < 0$$

# Phase equilibrium in reacting **Coulomb** system (Gibbs – Guggenheim conditions)



(Gibbs)

$$\begin{aligned} \mu_1'(P, T, x') &= \mu_1''(P, T, x'') \\ \mu_2'(P, T, x') &= \mu_2''(P, T, x'') \\ &\dots\dots\dots \\ \mu_k'(P, T, x') &= \mu_k''(P, T, x'') \end{aligned}$$

Equilibrium reactions



(reduced number of basic units)

Uranium – Oxygen system

$$\begin{aligned} \mu_U'(P, T, x') &= \mu_U''(P, T, x'') \\ \mu_O'(P, T, x') &= \mu_O''(P, T, x'') \end{aligned}$$

**NB!** - Chemical potentials of charged species are **not equal** (Guggenheim, 1929)

Electro-chemical potentials are equal

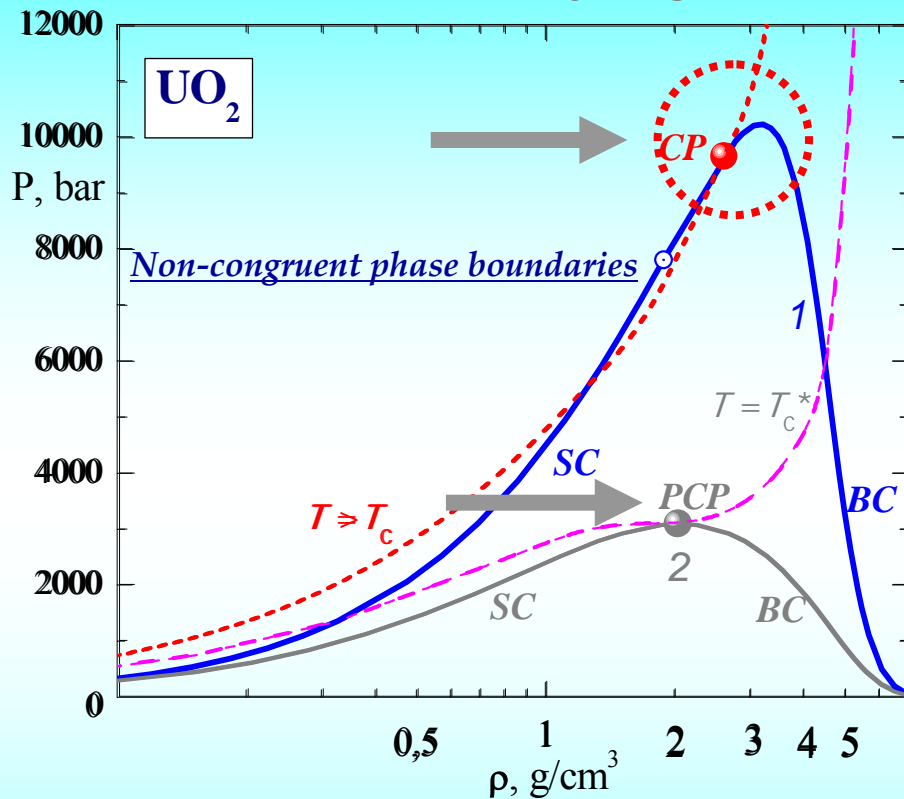
$$\mu_i' + Z_i e \phi' = \mu_i'' + Z_i e \phi'' \Leftrightarrow \Delta\phi(T) \leftarrow \text{Galvani potential}$$

Potential drop at mean-phase interface in equilibrium Coulomb system

$$\begin{aligned} \mu_1'(P, T, x') &= \mu_1''(P, T, x'') + Z_1 e \Delta\phi(T) \\ \mu_2'(P, T, x') &= \mu_2''(P, T, x'') + Z_2 e \Delta\phi(T) \\ &\dots\dots\dots \\ \mu_e'(P, T, x') &= \mu_e''(P, T, x'') - e \Delta\phi(T) \end{aligned}$$

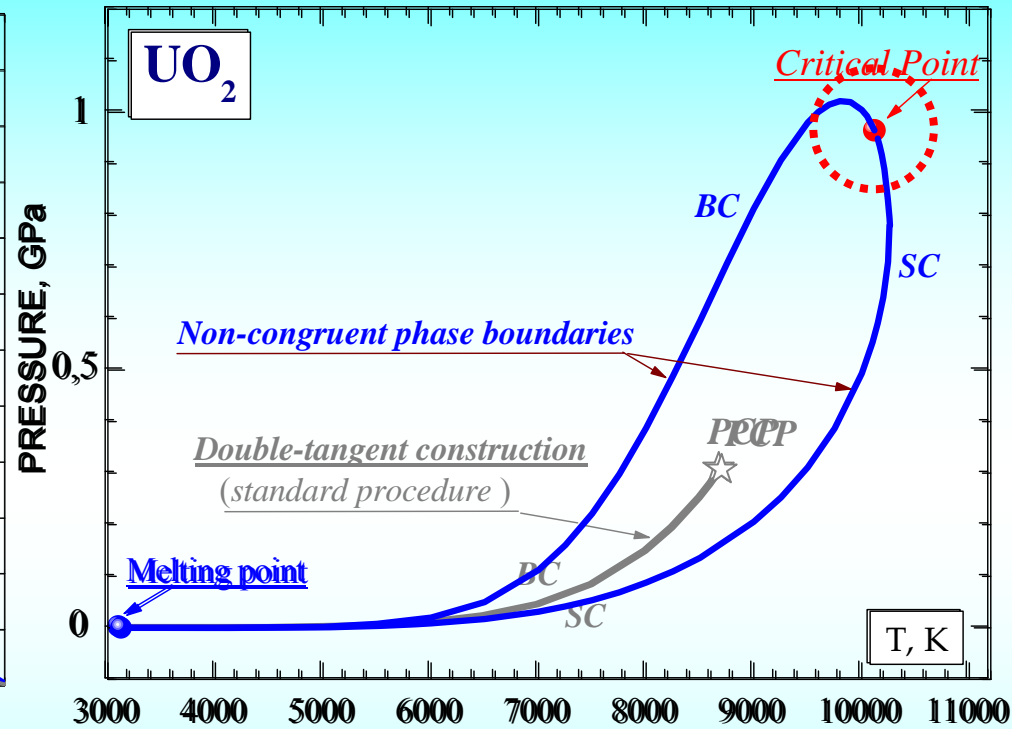
# Non-congruent evaporation in U-O system (Gibbs - Guggenheim conditions)

Pressure - Density Diagram



1 – Non-congruent (total) equilibrium  
2 – Forced-congruent (partial) equilibrium

Pressure - Temperature Diagram



BC – Boiling liquid conditions  
SC – Saturated vapor conditions

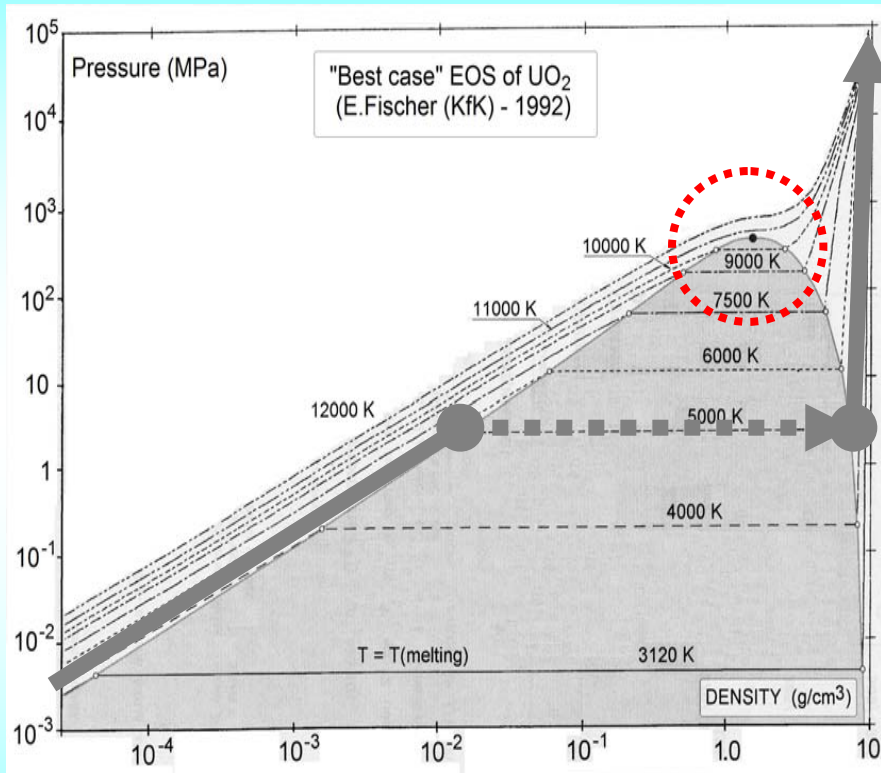
**NB!** 2-dimensional two-phase region instead of standard  $P$ - $T$  saturation curve

**NB!** High pressure level of non-congruent phase decomposition

**NB!** Critical point should be of non-standard type:  $(\partial P/\partial V)_T \neq 0$   $(\partial^2 P/\partial V^2)_T \neq 0$   
It should be instead:  $(O/U)_{\text{liquid}} = (O/U)_{\text{vapor}}$  and  $\{ \partial \mu_i / \partial n_k \}_T \big|_{CP} = 0$

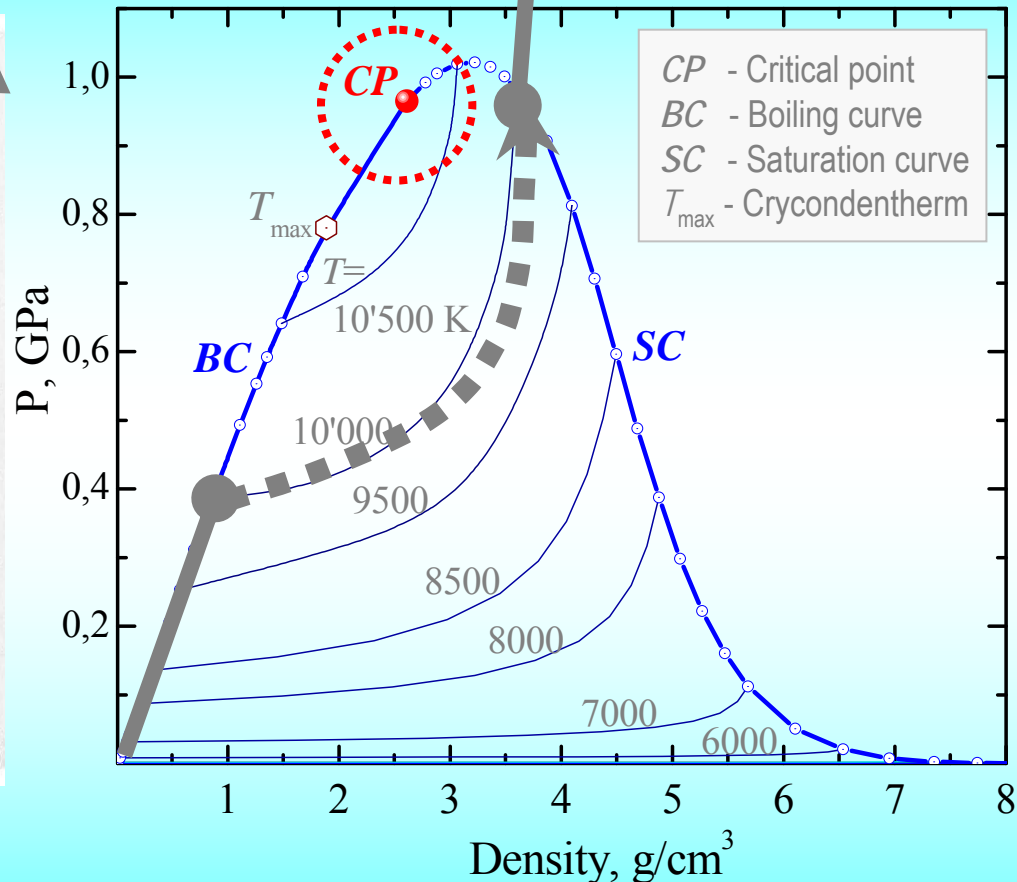
# Isotherms in two-phase region

Standard pressure-density diagram

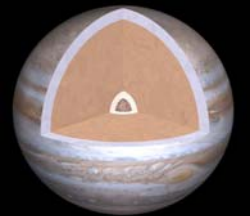


Fischer E.A. *J. Nucl. Sci. Eng.* (1989)

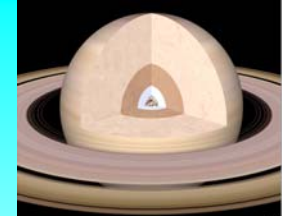
Non-congruent pressure-density diagram



- **Isothermal** phase transition starts and finishes at *different pressures*
- **Isobaric** phase transition starts and finishes at *different temperatures*



# Thermodynamics of $H_2 + He$ plasma (planetary science)



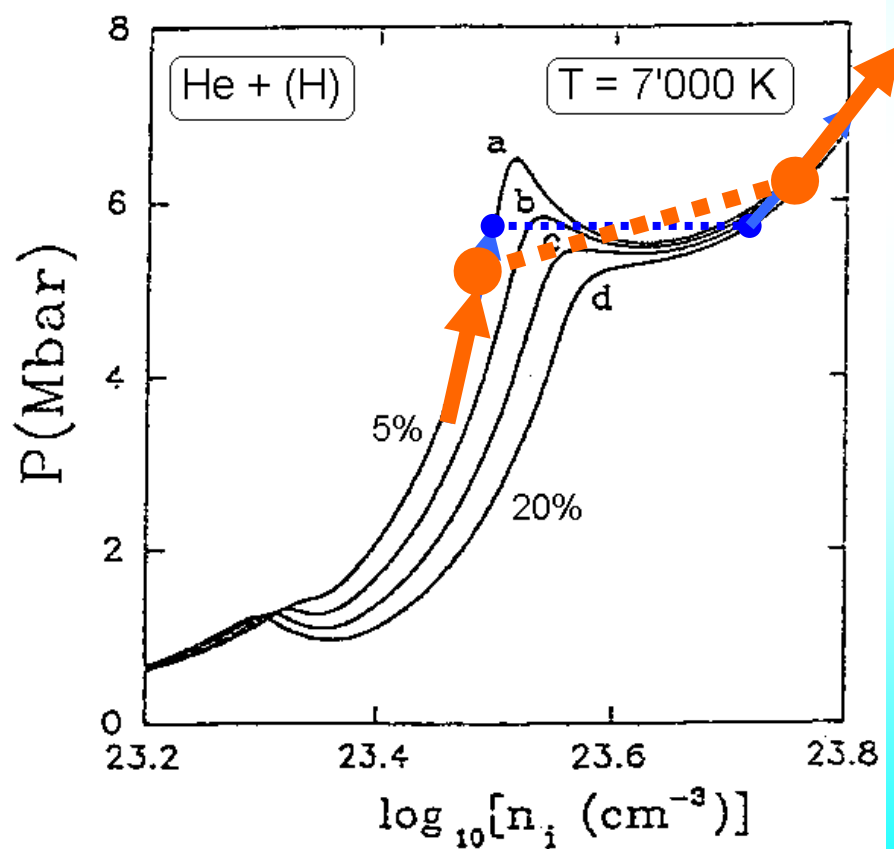
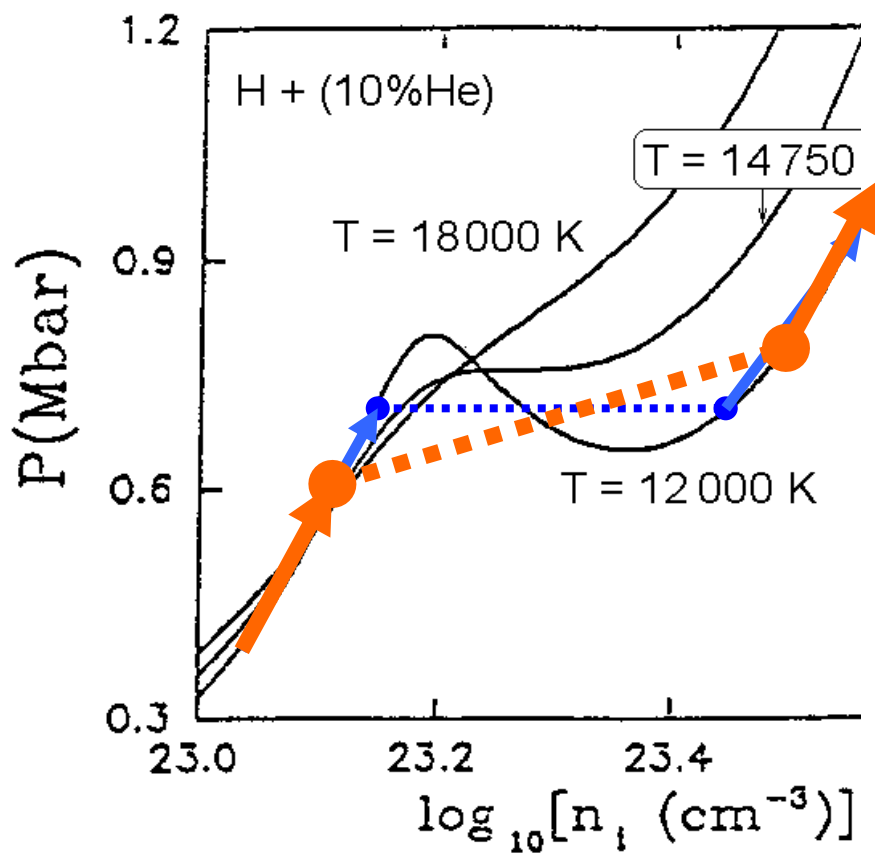
**Forced-Congruent** phase transition in  $H_2 + He$  plasma (*calculated*)

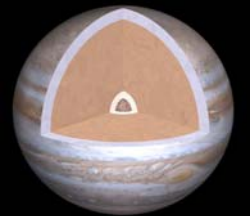
Contrib. Plasma Phys. **35** (1995) 2, 109–125

Plasma Phase Transition  
in Fluid Hydrogen-Helium Mixtures

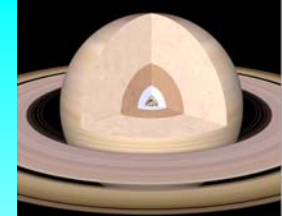
M. SCHLANGES (a), M. BONITZ (b), and A. TSCHTTSCHJAN (b)

**Non-Congruent** phase transition in  $H_2 + He$  plasma (*must be instead!*)





# Thermodynamics of $H_2 + He$ plasma (planetary science)



**Non-Congruent** phase transition in  $H_2 + He$  plasma  
(*must be!*)

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Plasma Phase Transition  
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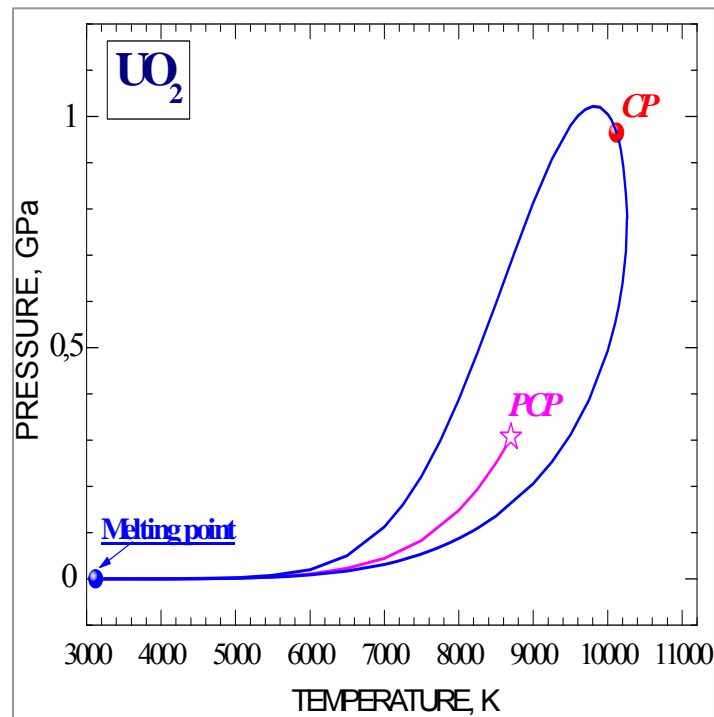
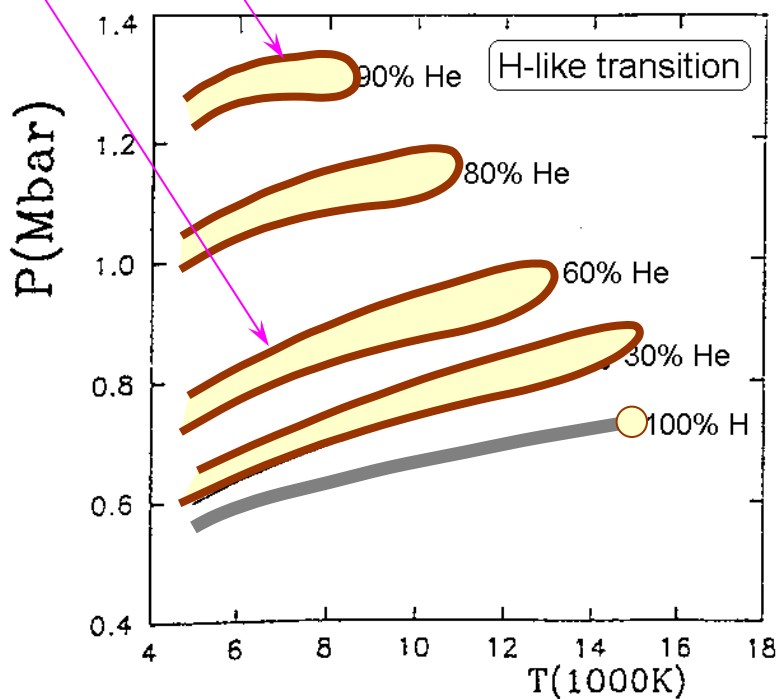


Fig. 7. Coexistence pressure for H–He mixtures for different values of the mixing parameter, for the hydrogen-like plasma phase transition and for the helium-like plasma phase transition.

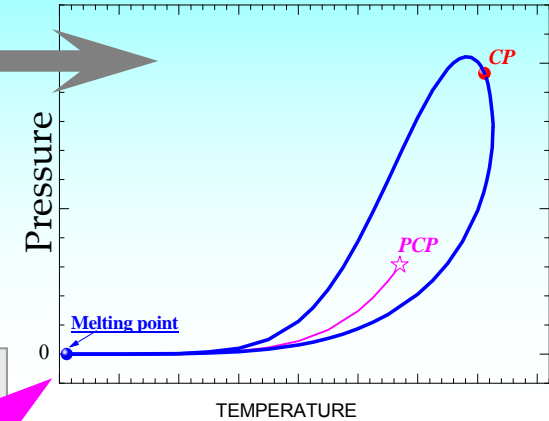


# Main issue from study of non-congruent evaporation in U-O system

## Non-congruence of phase transition in U-O system – – is it an exception or a general rule ?

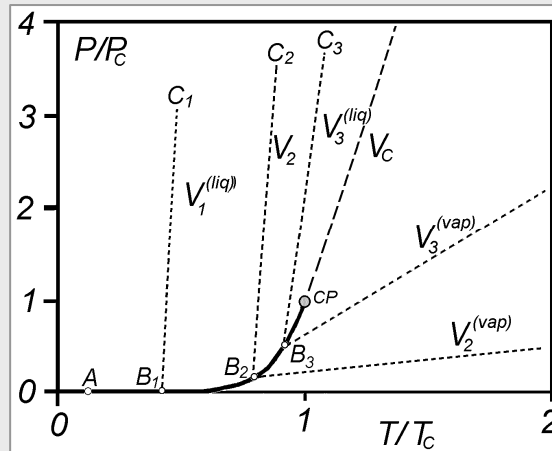
### Basic conclusion:

- Any phase transition in a system of **two** or **more chemical elements** must be **non-congruent**
- **Congruent** phase transition is **exception**



## Evident contradiction

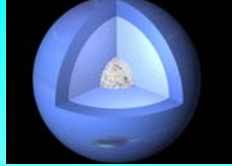
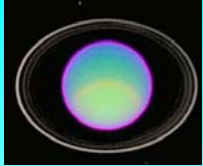
$\text{H}_2\text{O}$ ,  $\text{CO}_2$ ,  $\text{NH}_3$  .....



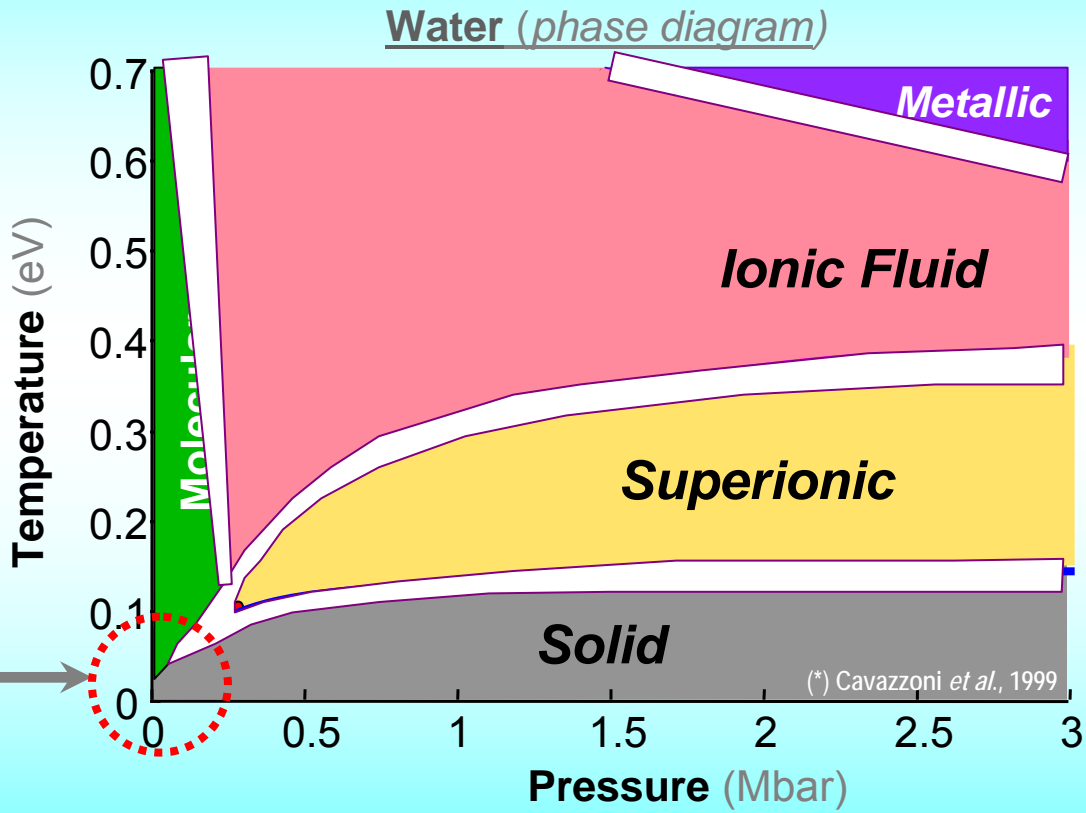
Non-congruence in  $\text{H}_2\text{O}$  etc... – what does it mean ?

**BASIC STATEMENT:**

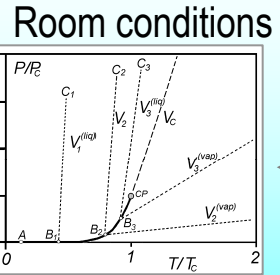
Any phase transition in a system of **two or more chemical elements** must be **non-congruent**



# Neptune and “hot-water” extrasolar planets



GJ436b  
 Star: - Gliese 436 (RD)  
 $M \sim 22 M_{\odot}$   
 $R \sim 4 R_{\odot}$   
 $\Delta T \sim 2,6$  days (!)  
 $T_{\text{surface}} \sim 500$  K  
 Main Comp-t. – H<sub>2</sub>O  
 = <<> =  
 (Discovered – 2007)



Ab initio calculations  
 Cavazzoni, *et al.* *Science* (1999)  
 Mattsson & Desjarlais (*Sandia Lab.*): *High energy-density water: DFT/QMD simulations* (2007)

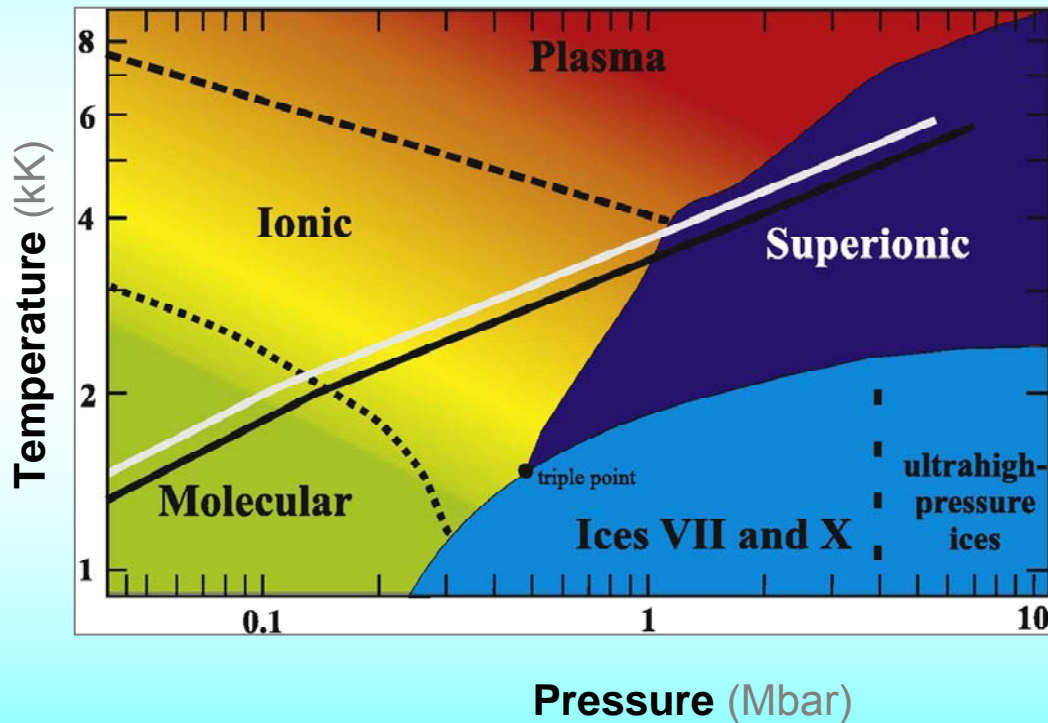
Any phase transition in **high-T\_high-P** water must be **non-congruent**

## BASIC STATEMENT:

Any phase transition in a system of **two or more chemical elements** must be non-congruent

# Neptune and “hot-water” extrasolar planets

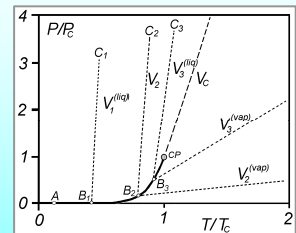
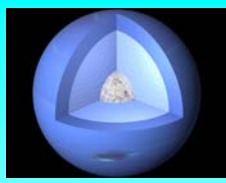
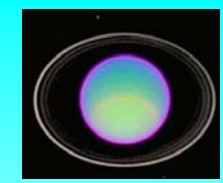
Water (phase diagram - 2011)



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 $\Delta T \sim 2,6$  days (!)  
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Main Comp-t. –  $\text{H}_2\text{O}$   
= <<> =  
(Discovered – 2007)

Ab initio calculations

R.Redmer, T.Mattsson, N.Nettelman, M.French, *Icarus* (2011)



# Cassini-Huygens

MISSION TO SATURN & TITAN

Giant planets evolution problem

## Hypothetical phase transitions in H<sub>2</sub>/He mixture

after Chabrier G., Saumon D., Hubbard W., Lunine J. (SCCS-1992, Rochester)

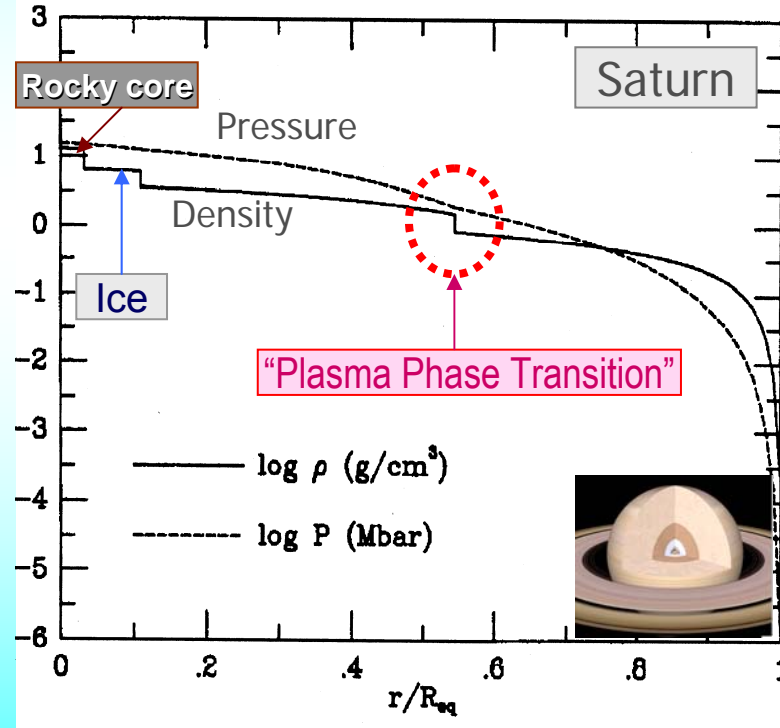
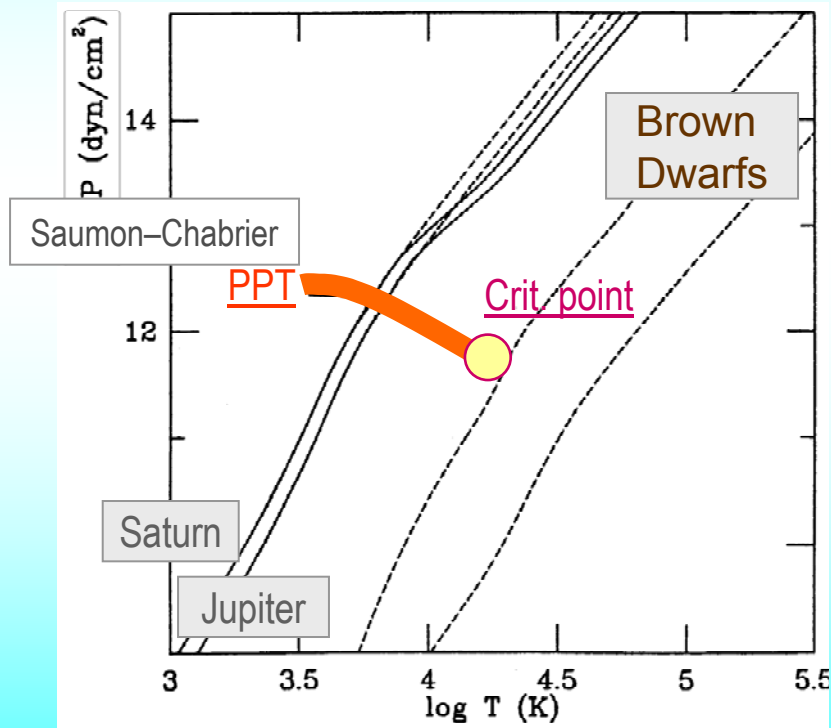


Fig. 1. Pressure and density profiles of optimized models of Jupiter (top panel) and Saturn (bottom panel), plotted as a function of mean radius. Discontinuities in the density clearly mark the boundaries of the four layers of the models: rocky core, ice mantle, metallic and molecular

# Cassini-Huygens

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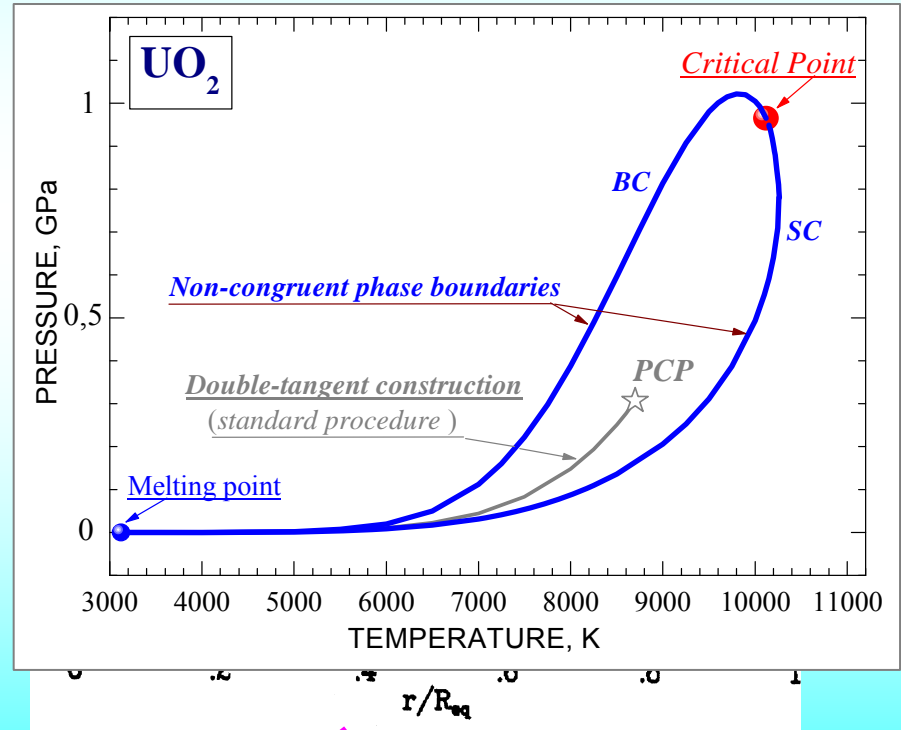
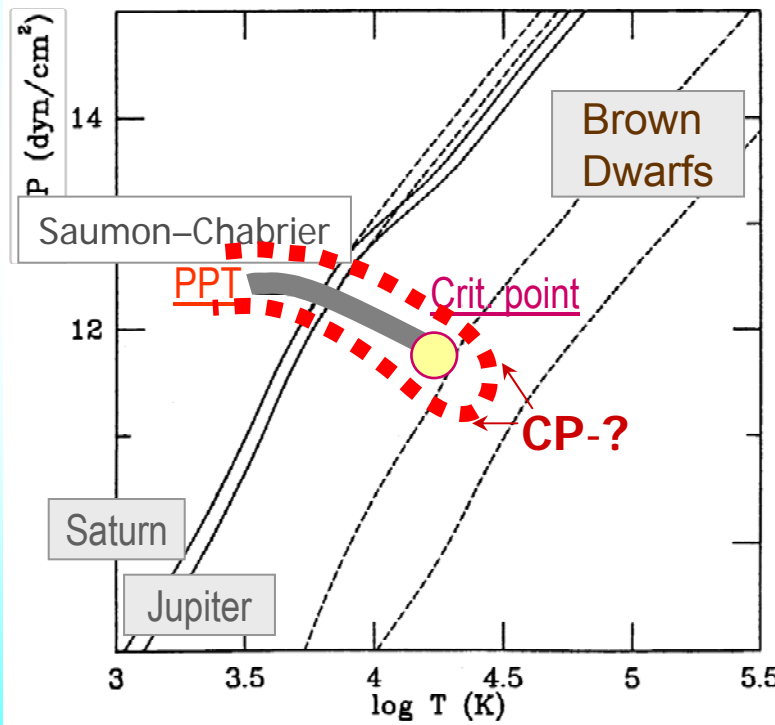


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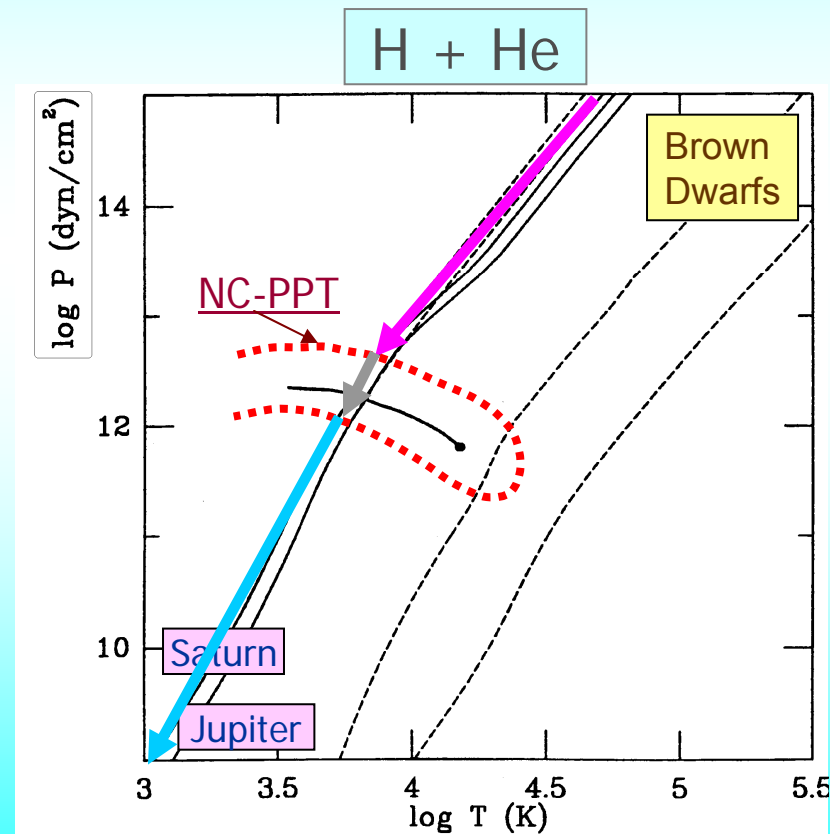
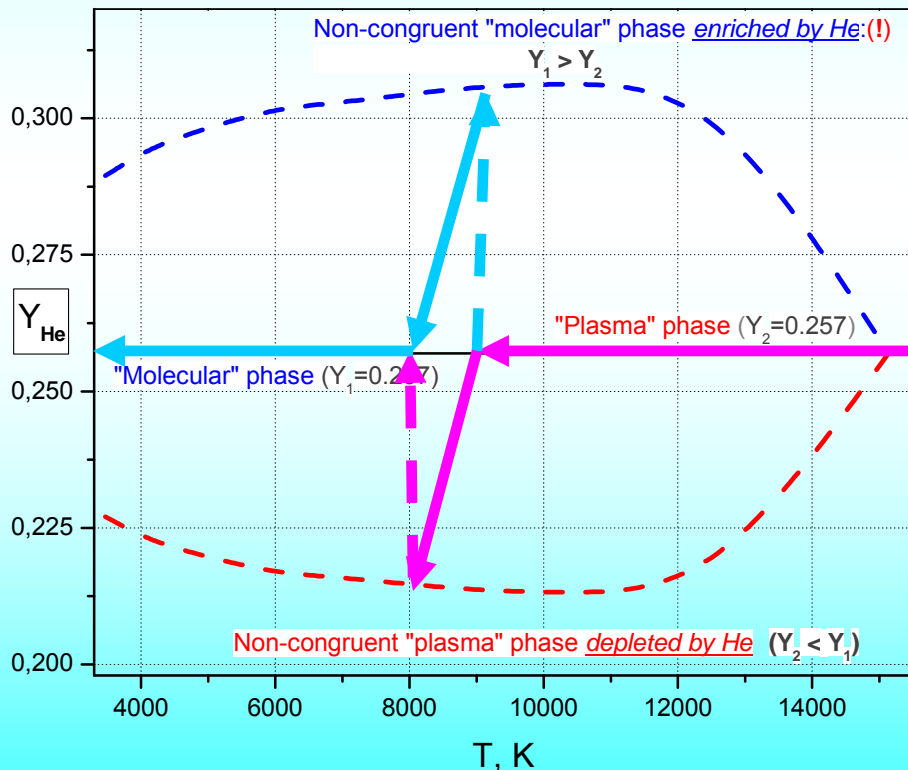
# Estimated non-congruence for plasma phase transition in H<sub>2</sub>/He mixture of Jupiter and Saturn

(with Artem Ukrainets)

(PPT-variant of Saumon, Chabrier and Van Horn – 1995)

## Assumptions:

- Helium is not ionized.
- Atomic helium interacts with neutral hydrogen species only (H<sub>2</sub> and H).
- Interaction of atomic helium with charged species are low and repulsive.



**A. Ukrainets & I. Iosilevskiy**

in "Physics of matter under extreme conditions",  
Ed. V.Fortov, Moscow, IPCP (2005) 116. (in Russ.)

# Estimated non-congruence for the plasma phase transition in H<sub>2</sub>/He mixture of Jupiter and Saturn

(PPT-variant of Saumon, Chabrier and Van Horn – 1995)

## Question:

- Is the estimated helium enrichment (depletion) negligible or noticeable? (or may be even significant ?)

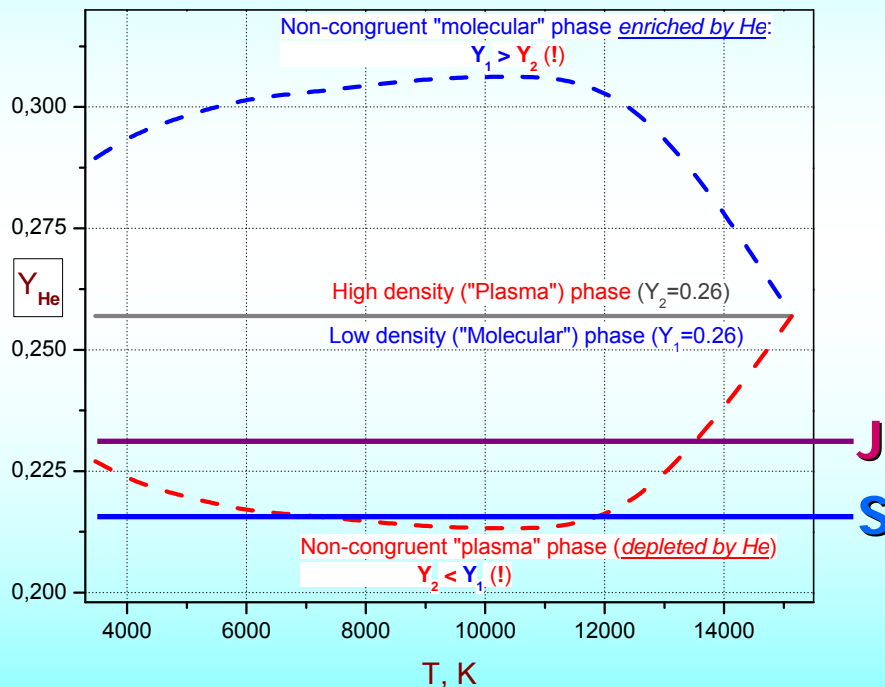
## Phase Separation in Giant Planets:

Jonathan J. FORTNEY, William B. HUBBARD

*Icarus*, 164 (1) 2003

### Atmospheric elemental abundances in Jupiter and Saturn (mass fractions)

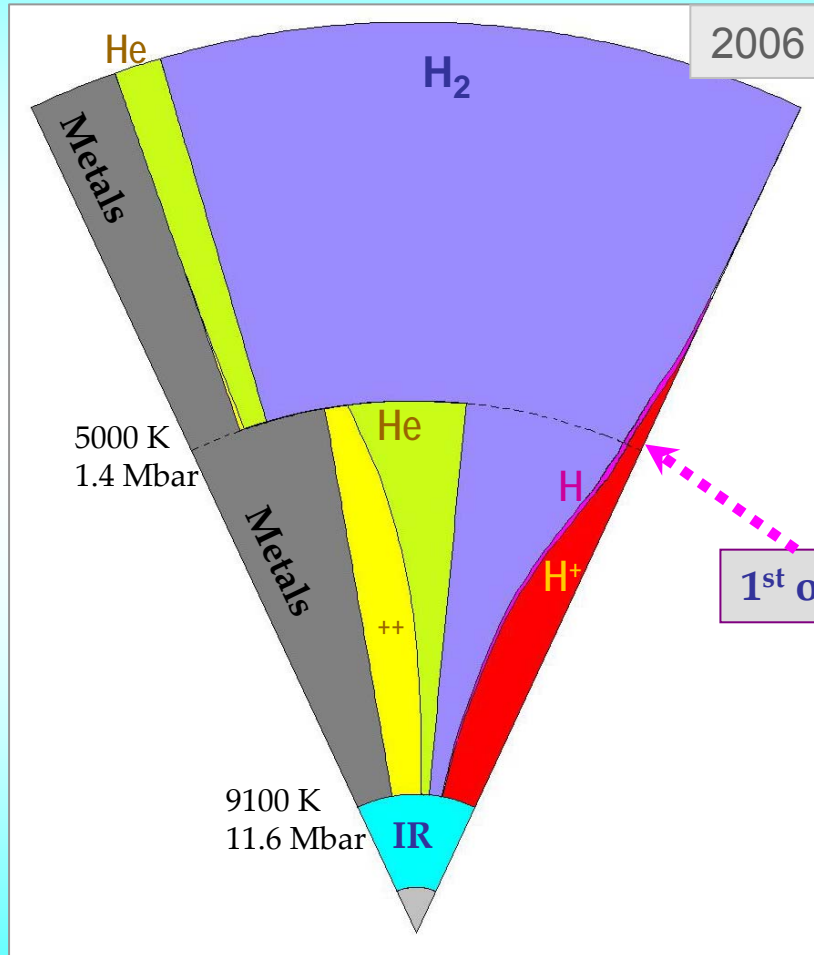
Element	SOLAR	JUPITER <i>Galileo</i>	SATURN <i>Voyager</i>	SATURN <b>revised</b>
H	0.736	0.742	0.92	0.76
<b>He</b>	<b>0.249</b>	<b>0.231</b> ± 0.04	<b>0.06</b> ± 0.05	<b>0.215</b> ± 0.035



- \* Provided estimation of the non-congruence for PPT in version of Saumon and Chabrier approves full-size calculation of this effect.
- \* The same is true for all other variants of predicted hypothetical phase transitions in pure hydrogen and helium when they being transformed into H<sub>2</sub>/He mixture.

# Giant planets interior composition

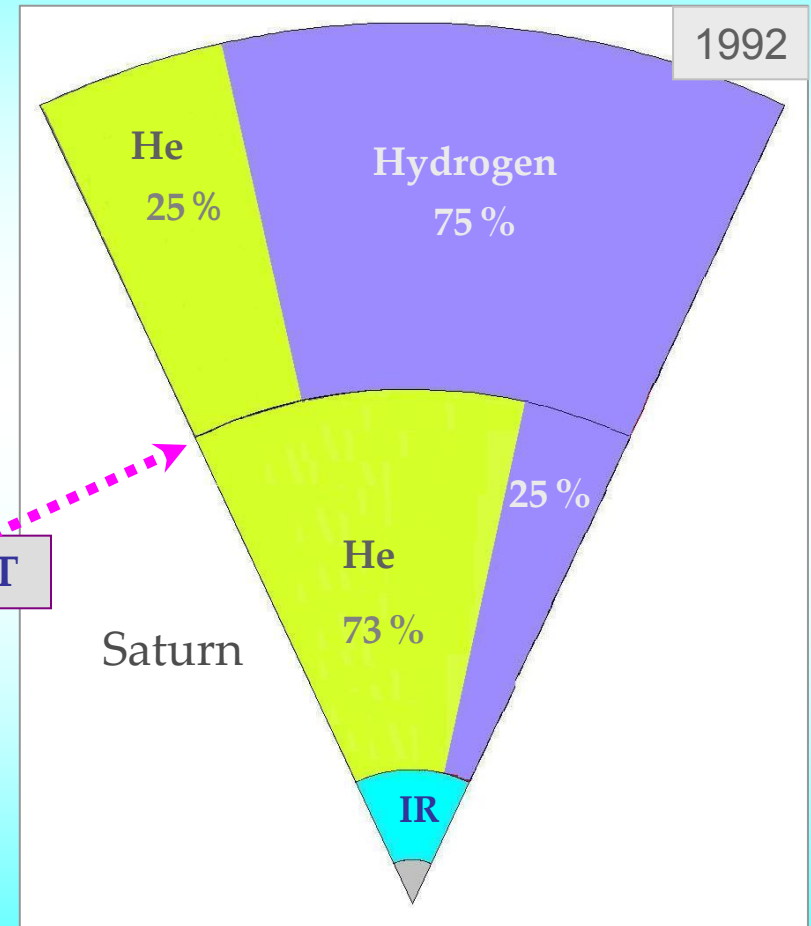
## Saturn interior composition



After N. Nettelmann, R. Redmer, *et al.*,  
PNP-12, Darmstadt, 2006)

## Optimized models of Jupiter and Saturn

(D. Saumon, G. Chabrier, W. Hubbard, J. Lunine)



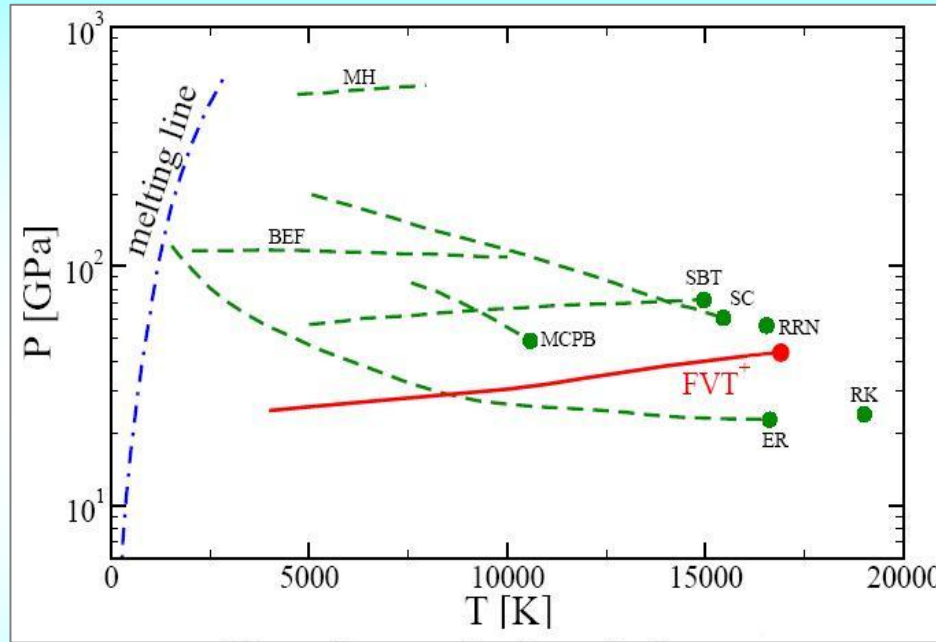
GIANT PLANETS AND THE PLASMA PHASE TRANSITION  
D. Saumon, G. Chabrier, W. B. Hubbard, and J. I. Lunine



# Предсказания плазменных фазовых переходов

## Модельные подходы (1970 – 2007)

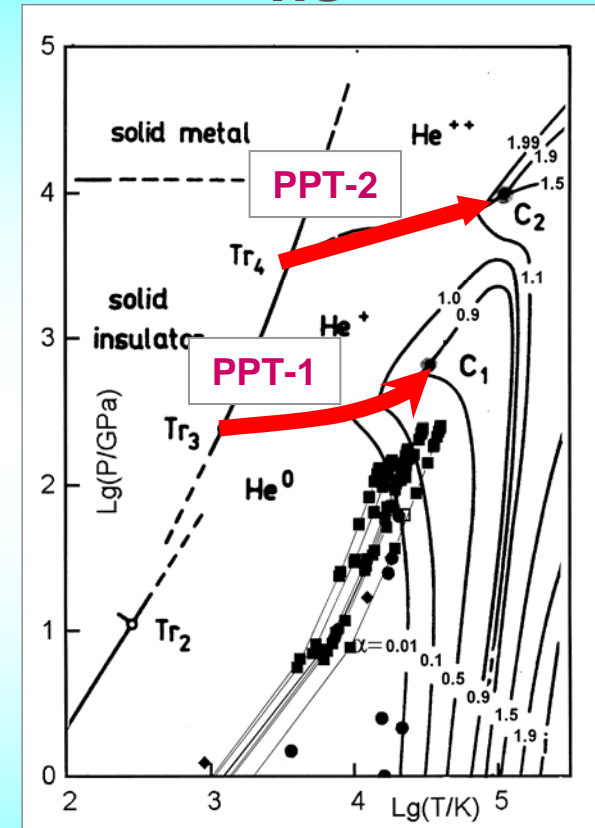
Н



Варианты границ плазменного фазового перехода в водороде  
(модельные подходы 1970 - 2007)

Holst B., Nettelmann N., Redmer R.,  
*Contrib. Plasma Phys.* **47**, (2007)

He

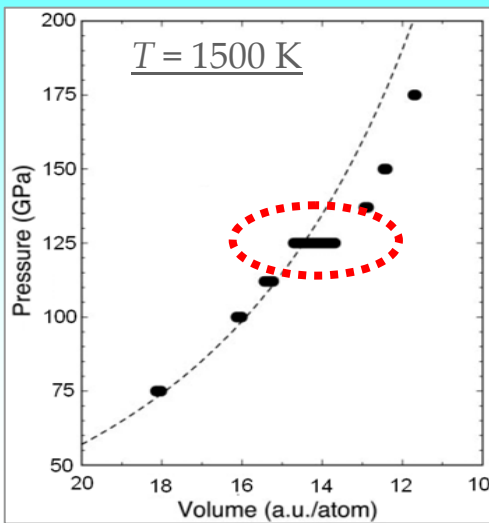


Два отдельных плазменных перехода в гелии  
(на  $1^{\text{й}}$  и  $2^{\text{й}}$  ионизации)

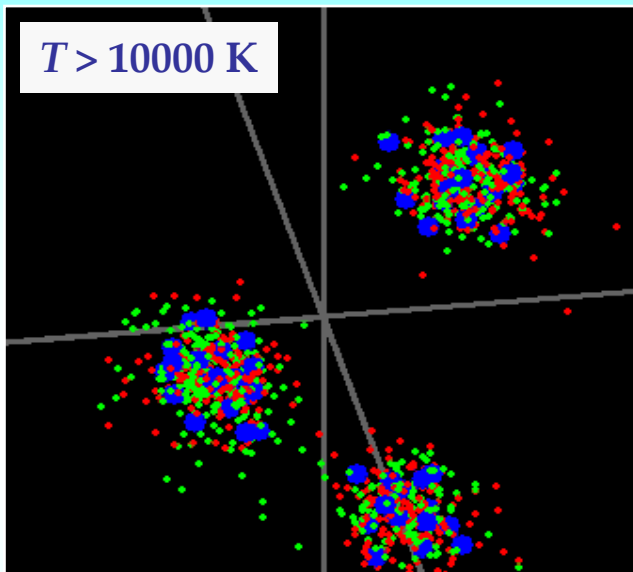
Ebeling, Foerster *et al.* (1991)

# Фазовый переход в плазме водорода уверенно предсказывается различными вариантами первопринципных подходов

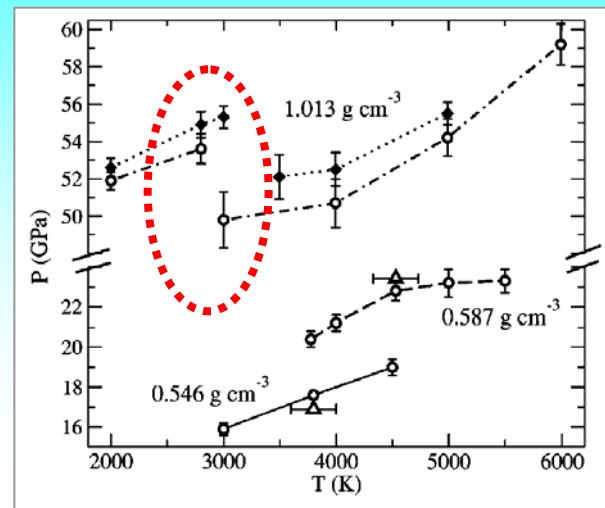
## Quantum Numerical Simulations



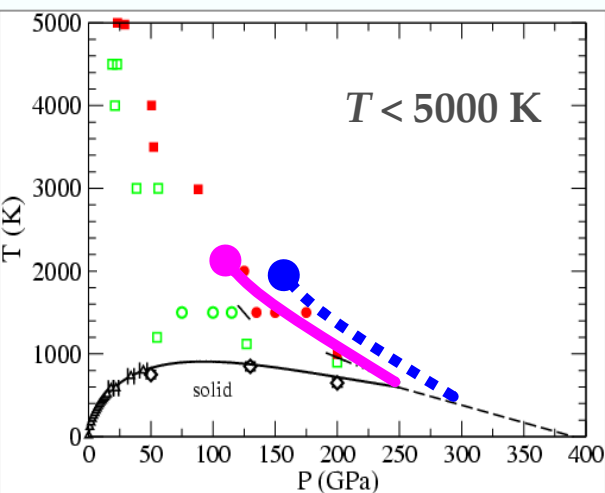
DFT + MD / Scandolo (2003)



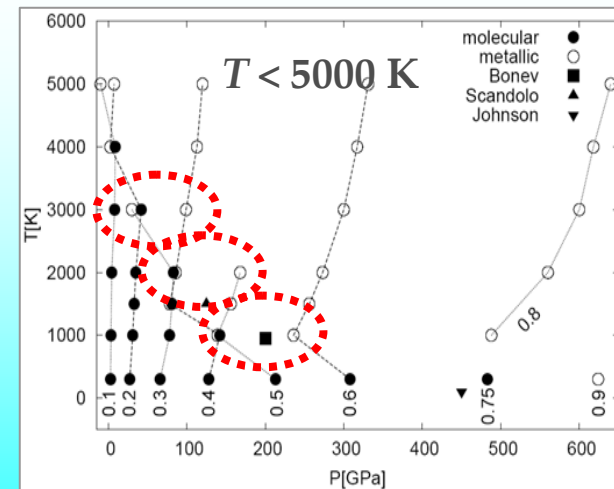
Phase Transition in Hydrogen Plasma  
 V.Filinov, V.Fortov, M.Bonits, P.Levashov  
 Письма ЖЭТФ 74 (2001)  
 Phys. Lett. A 274 (2000)  
 = «» =  
 Path Integral Monte-Carlo



DFT + MD / Bonev, Militzer, Galli (2004)



DFT + MD / Bonev, Militzer, Galli.



DFT + MD / Morales M. et al. (2010) /  
 Lorenzen W. et al. PRB (2010)

Wave-Packets + MD  
 Erlangen University, Phys.Rev.E (2007)

# Theoretical predictions of "dissociative" fluid-fluid phase transition in liquid hydrogen

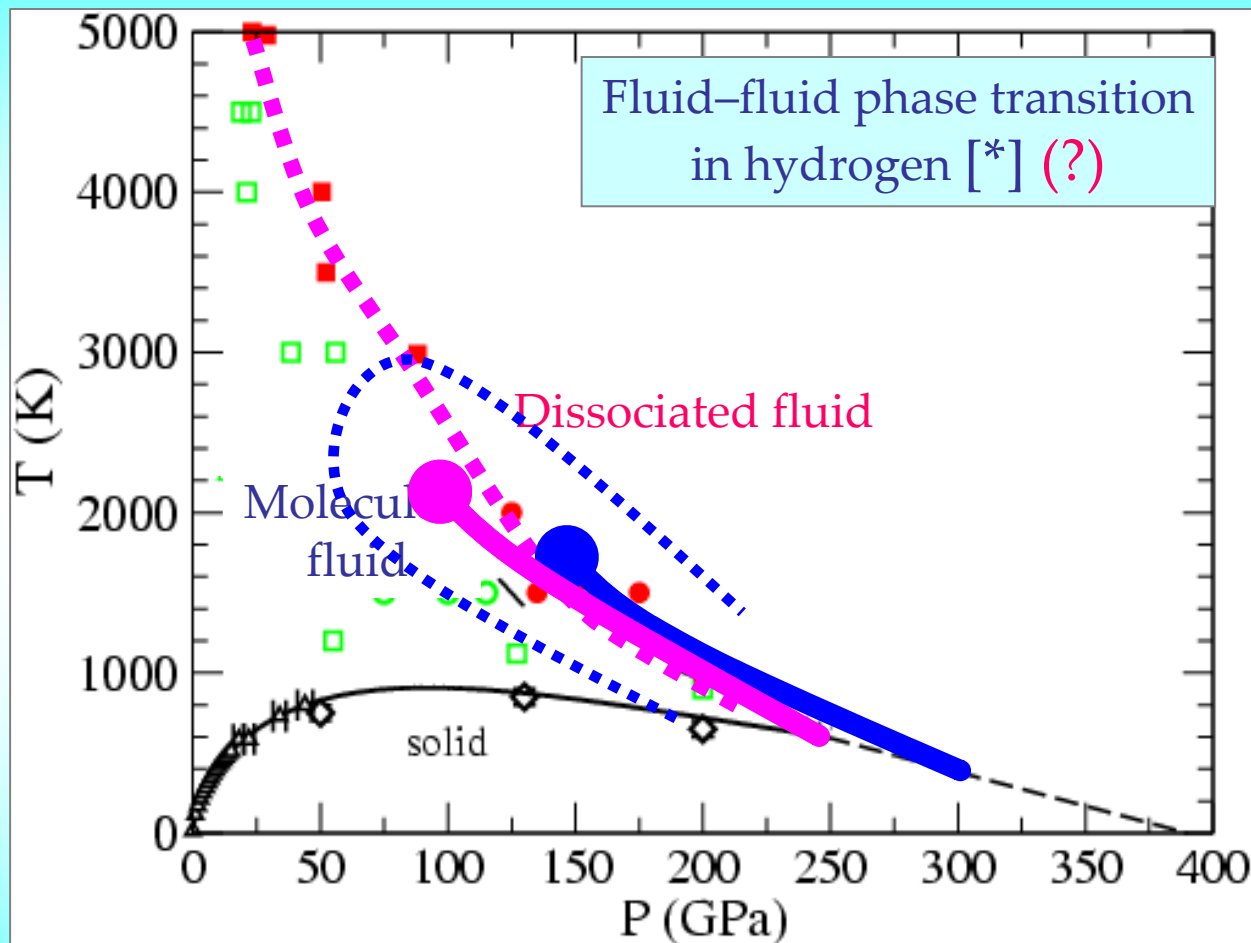
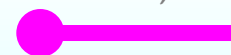
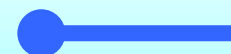


Figure from:  
Giulia Galli,  
SCCS-2005,  
Moscow

Morales *et al*, 2010



Lorenzen *et al*, 2010



➔ H + He

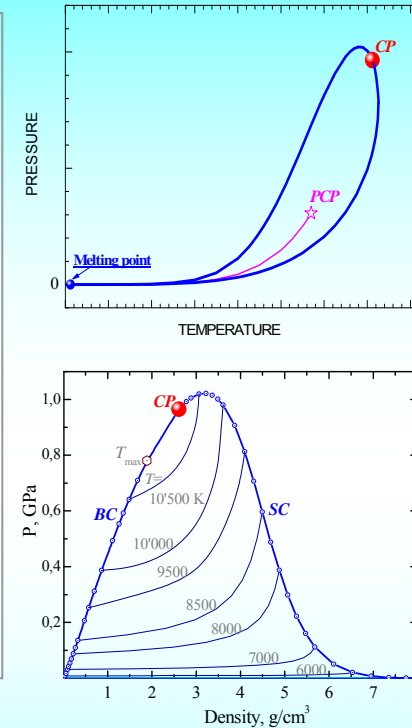
**DFT/MD:** Scandolo S. *PNAS* 100, (2003) // Bonev S., Militzer B., Galli G. *PRB* 69 (2004)  
**WPMD :** Jakob B. *et al.* *PRE* (2007) // **DFT/MD:** Morales M. *et al.* *PNAS* 107, (2010)/  
**DFT/MD:** Lorenzen W. *et al.* *PRB* (2010)

# Hypothetical non-congruent phase transitions

(*short list*)

## Terrestrial applications:

- **Uranium- and Plutonium-bearing compounds:**
  - $UO_2$ ,  $PuO_2$ ,  $UC$ ,  $UN$ , ... etc.,
- **Metallic alloys:** ( $Li-K-Na$ ,...etc.)
- **Oxides:** ( $SiO_2$ ...etc.)
- **Hydrides of metals** ( $LiH$ ... etc.)
- **Ionic liquids and molten salts:**
  - alkali halides ( $NaCl$  ... etc.), ammonium halides ( $NH_4Cl$  ... etc.)...
- **“Dusty” and Colloid plasmas:**  
(Coulomb system of macro-ions  $+Z$  and micro-ions:  $+1, -1$ )



## Non-Congruence in Cosmic Matter:

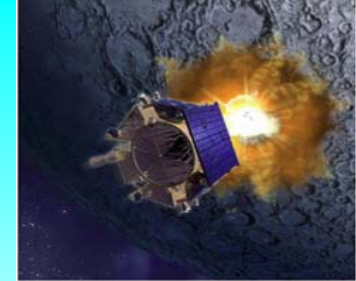
- **Plasma and Dissociative Phase Transitions in mixtures:**  $H_2$  /  $He$  /  $H_2O$  /  $NH_3$  /  $CH_4$   
in **Giant Planets, Brown Dwarfs and Extra-Solar Planets,**
- **Phase Transitions in White Dwarfs,**
- **Phase Transitions in Neutron Stars,**
- **Phase Transitions in “Strange” Stars** (quark-hadron transition ... etc.)

The question is:

What kind of phase transition one can expect  
in high- $T$ \_high- $P$  complex plasma ?



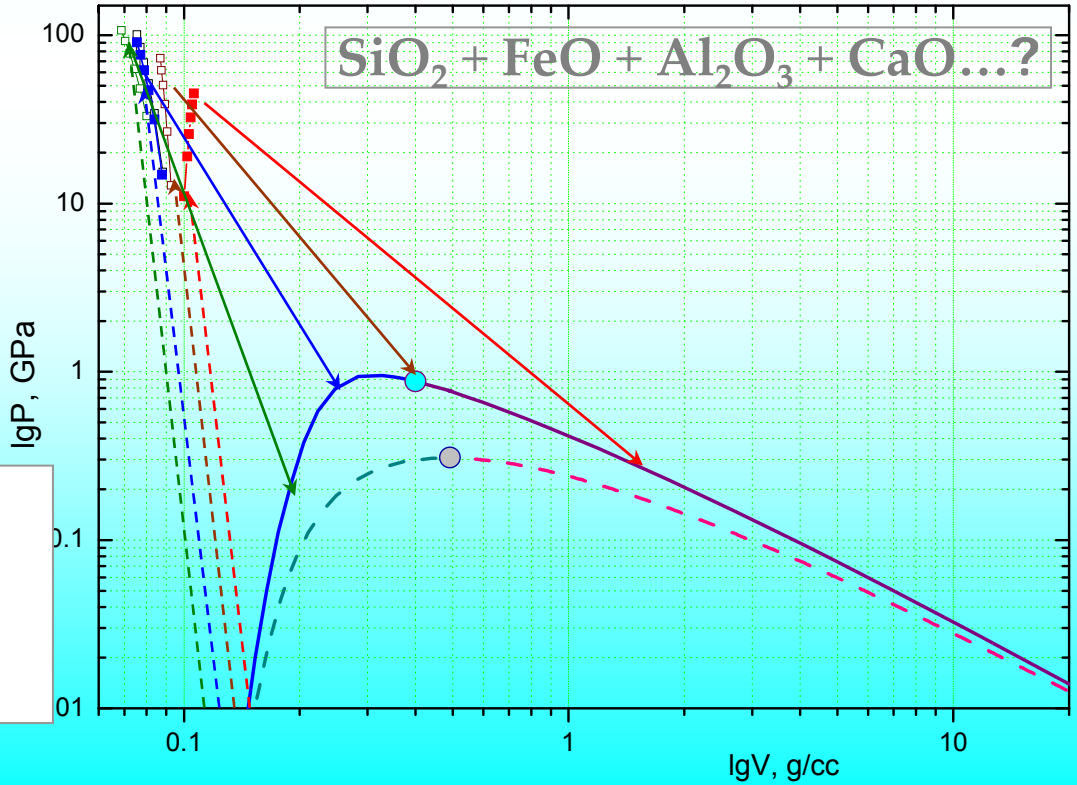
Natural and artificial bombarding of lunar surface



Launch – April 24, 2009  
 Impact velocity ~ 9'000 km/h ⇔ Impact plume ~ 50 km high

What kind of phase transition one can expect in high- $T$ \_high- $P$  complex plasma?  
 $\text{SiO}_2 + \text{FeO} + \text{Al}_2\text{O}_3 + \text{CaO}$   
 $T \sim eV$  &  $P \sim GPa$

1<sup>st</sup> Stage – strong shock compression  
2<sup>nd</sup> Stage – free quasi-isentropic expansion



**NB !**  
 Any phase transition in such mixture must be *non-congruent*

The question is open



**Exploration of the Moon Continues!**

**LCROSS** Lunar CRater Observation and Sensing Satellite

What kind of phase transition one can expect in high- $T$ \_high- $P$  complex plasma?  
 $\text{SiO}_2 + \text{FeO} + \text{Al}_2\text{O}_3 + \text{CaO}$   
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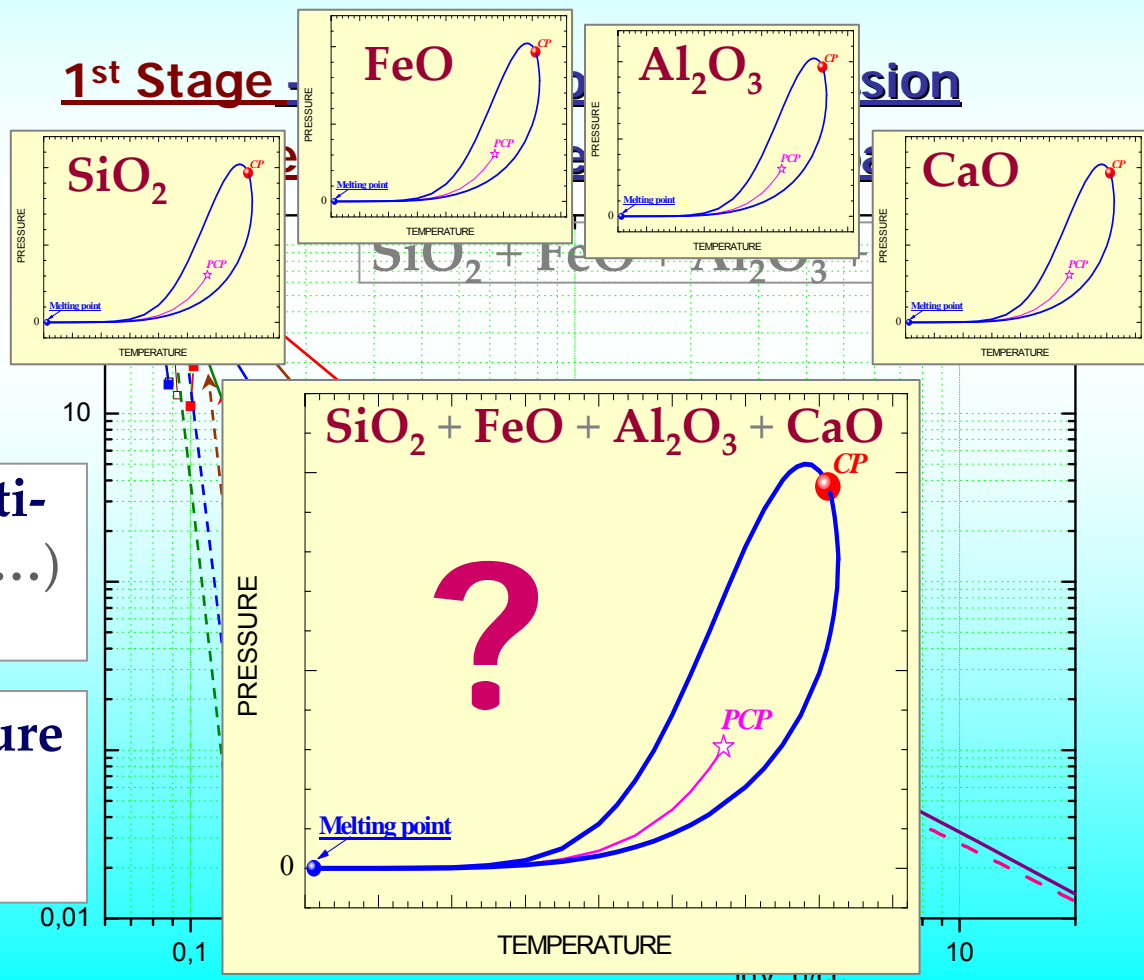
, 2009 // Impact – 9 October 2009  
 10 km/h  $\Leftrightarrow$  Impact plume  $\sim$  50 km high

The question is open

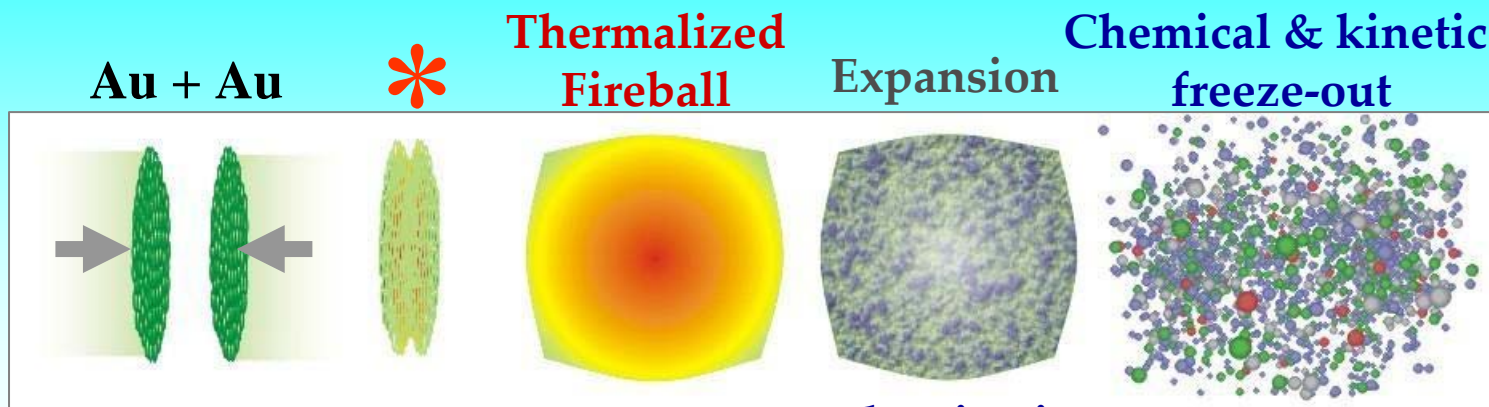
**NB !**

Phase transition in each constituent ( $\text{SiO}_2$ ,  $\text{FeO}$ ,  $\text{Al}_2\text{O}_3$ ,  $\text{CaO}$ ...) must be *non-congruent* !

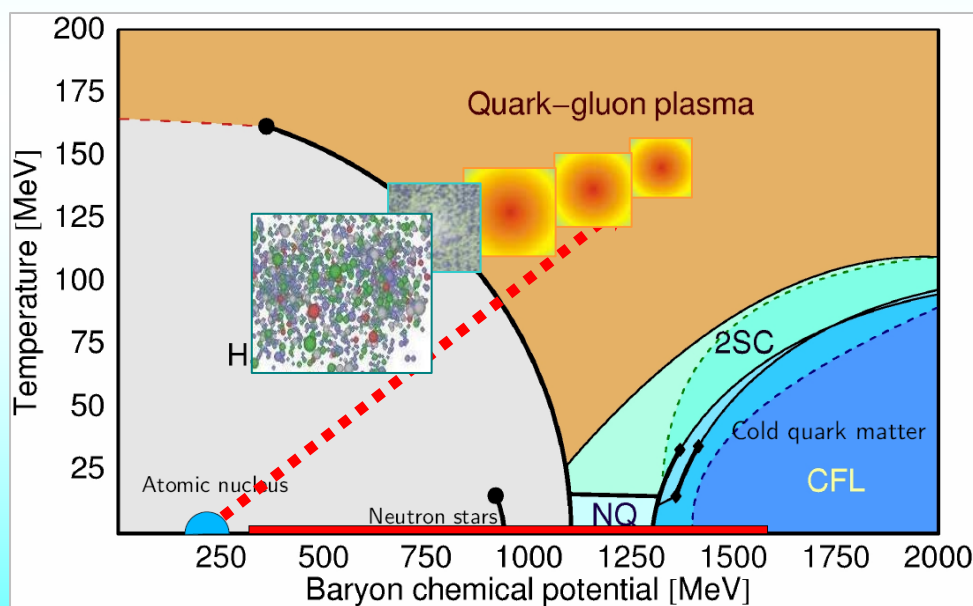
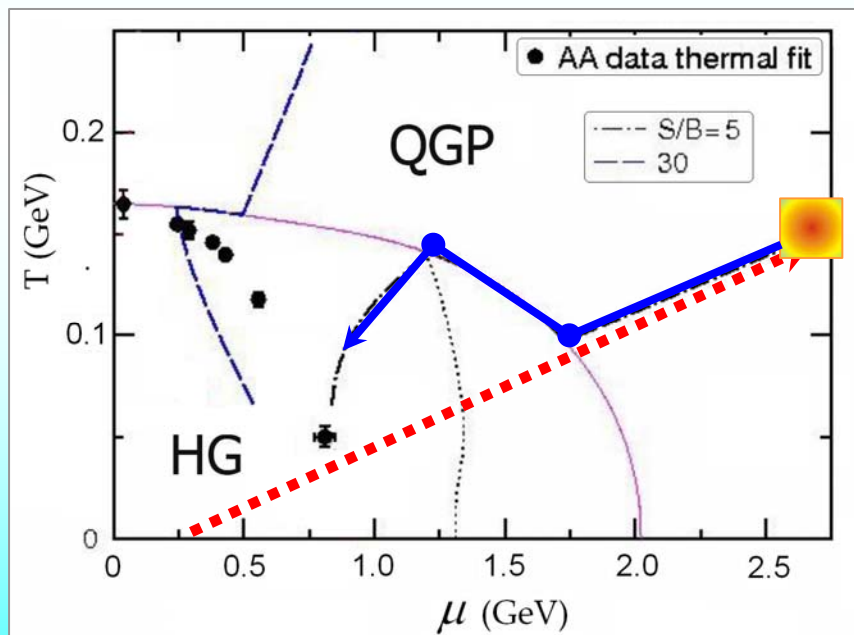
Phase transitions in the mixture must be *non-congruent* moreover !



# Impact *and* fireball hydrodynamics *in* HIC



## Hadronization



L.Satarov, M.Dmitriev, I.Mishustin //arXiv: 0901.1430v1

After David Blaschke, WEHS Seminar, Bad Honnef, 2007

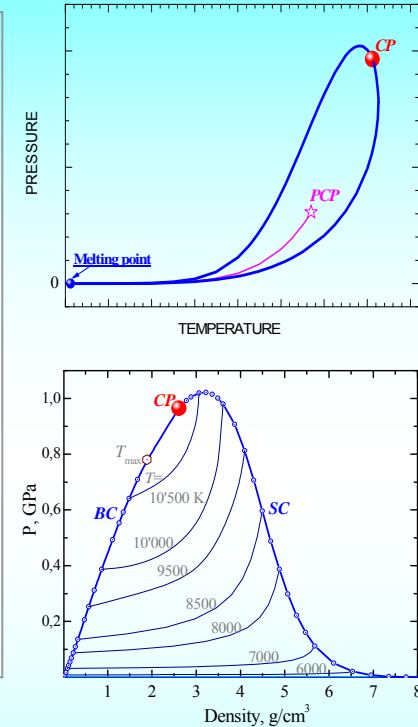


# Hypothetical non-congruent phase transitions

(*short list*)

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(Coulomb system of macro-ions  $+Z$  and micro-ions:  $+1, -1$ )



## Non-Congruence in Cosmic Matter:

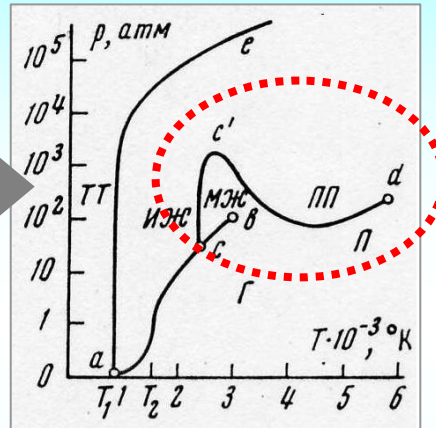
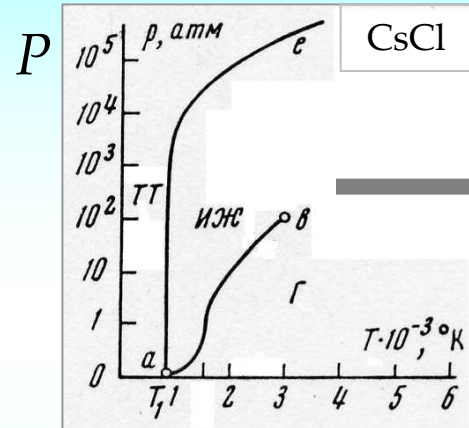
- **Plasma Phase Transitions in mixture:**  $H_2$  /  $He$  /  $H_2O$  /  $NH_3$  /  $CH_4$   
in **Giant Planets, Brown Dwarfs and Extra-Solar Planets,**
- **Phase Transitions in White Dwarfs,**
- **Phase Transitions in Neutron Stars,**
- **Phase Transitions in "Strange" Stars** (quark-hadron transition ... etc.)

# Non-congruence of hypothetical "plasma phase transition" in molten salts

Zeigarnik V, Kobzev G., Kurilenkov Yu., Norman G. *High Temp.* 10 (1972)

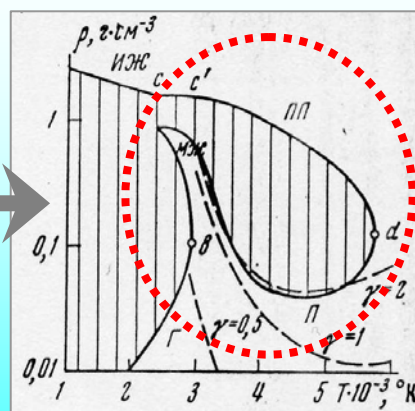
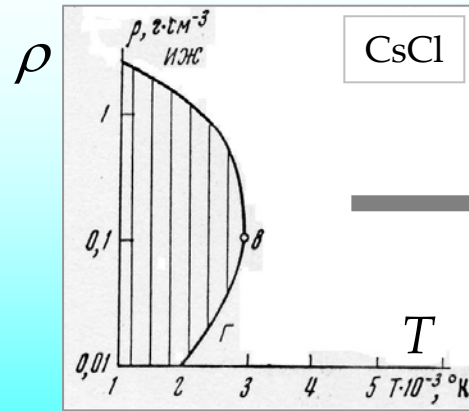
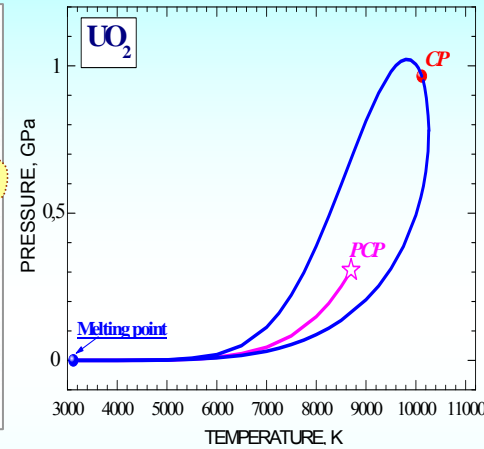
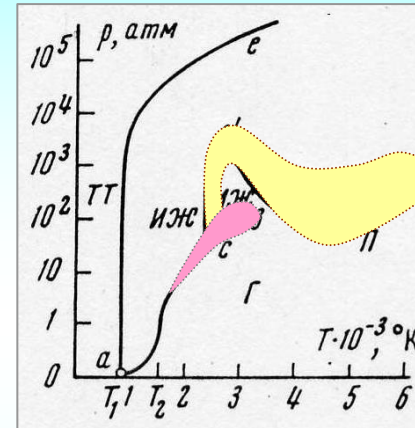
Ordinary phase transitions

+ Plasma phase transition



Basic conclusion:

Any phase transition in a system of **two or more chemical elements** must be **non-congruent**



The ordinary gas-liquid phase transition in CsCl must be **non-congruent** -

Hypothetical "plasma phase transition" in CsCl must be **non-congruent** even more -

Рис. 1. Диаграмма состояния  $P - T$  для CsCl

$a, b, c, d$  — тройные и критические точки; однородные фазы: ТТ — твердое тело; Г — газ, ИЖ — ионная жидкость; МЖ — молекулярная жидкость; П — плазма, ПП — плотная плазма.  $T_1$  — температура плавления;



# Non-congruence in exotic situations



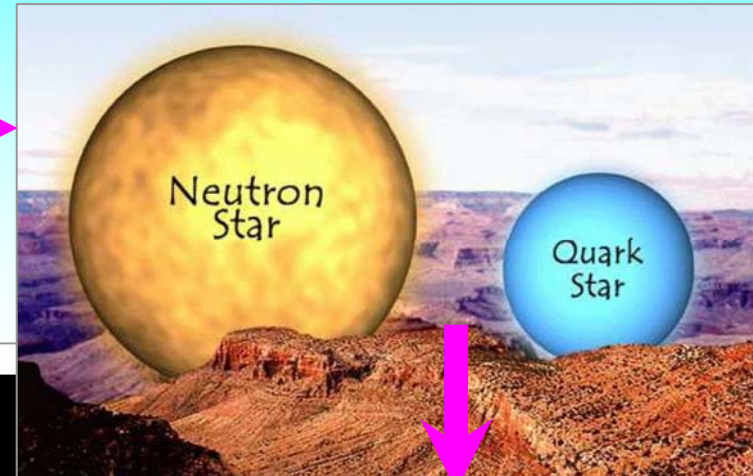
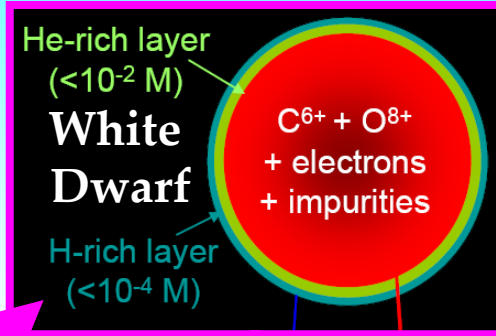
*(di scussi on)*

**Non-congruence *in* compact stars  
*and* supernova explosions**

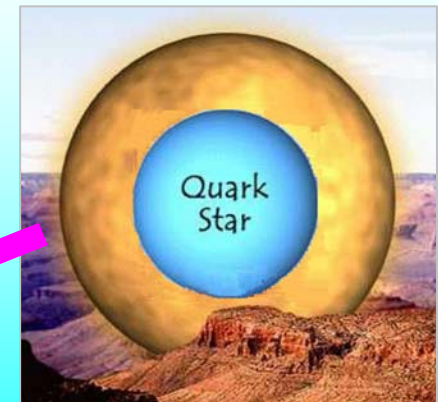
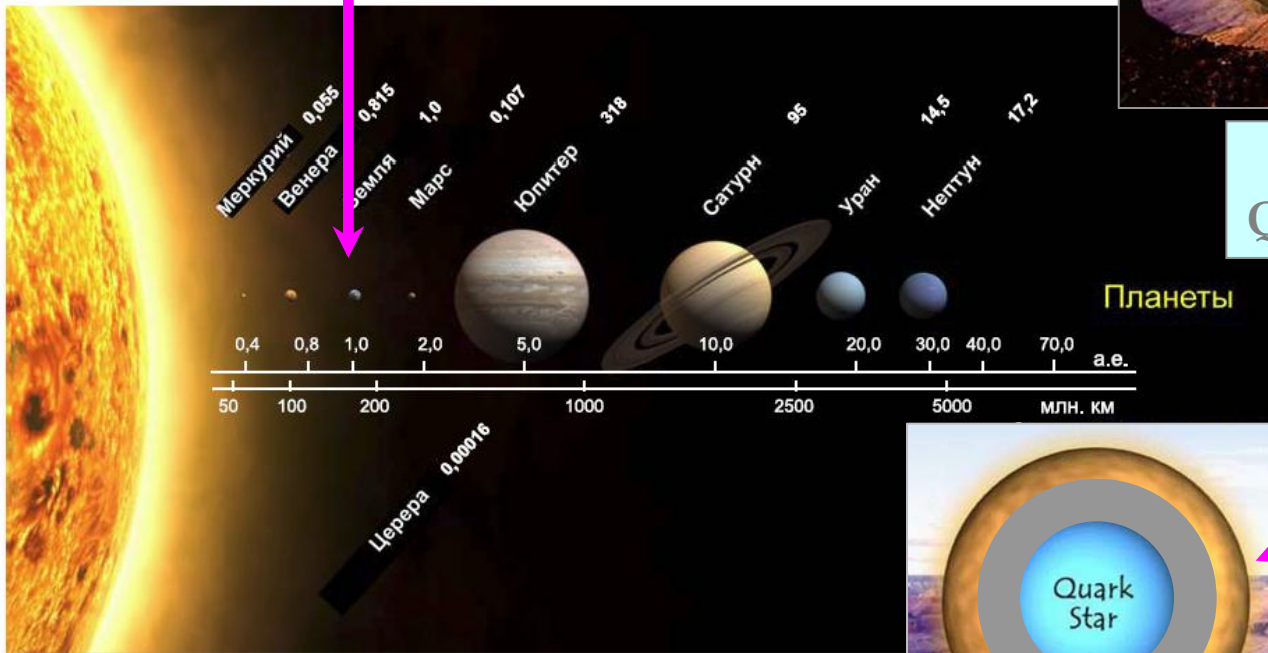
# Compact stars

White dwarfs, Neutron stars, "Strange" (quark) stars, Hybrid stars

Neutron and "Strange" Stars



Hybrid Stars  
Quark core + Hadron crust



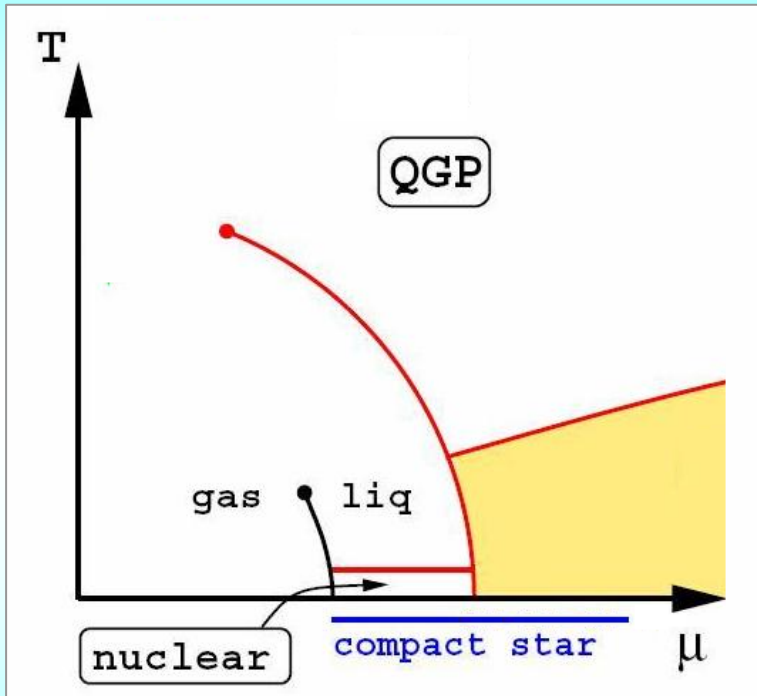
$\leftarrow R \sim 10 \text{ km} \rightarrow$

Hybrid Stars - II  
Quark core + Hadron crust + Mixed phase

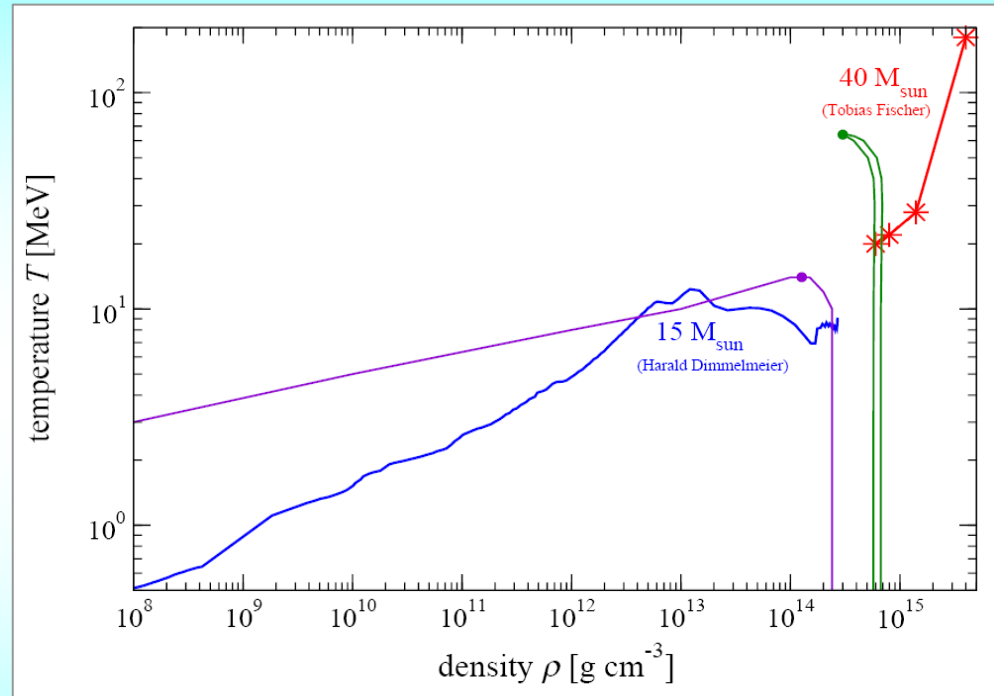


# Hypothetical non-congruence in compact stars and supernova explosions

Phase Diagram



Supernova Collapse in the Phase Diagram



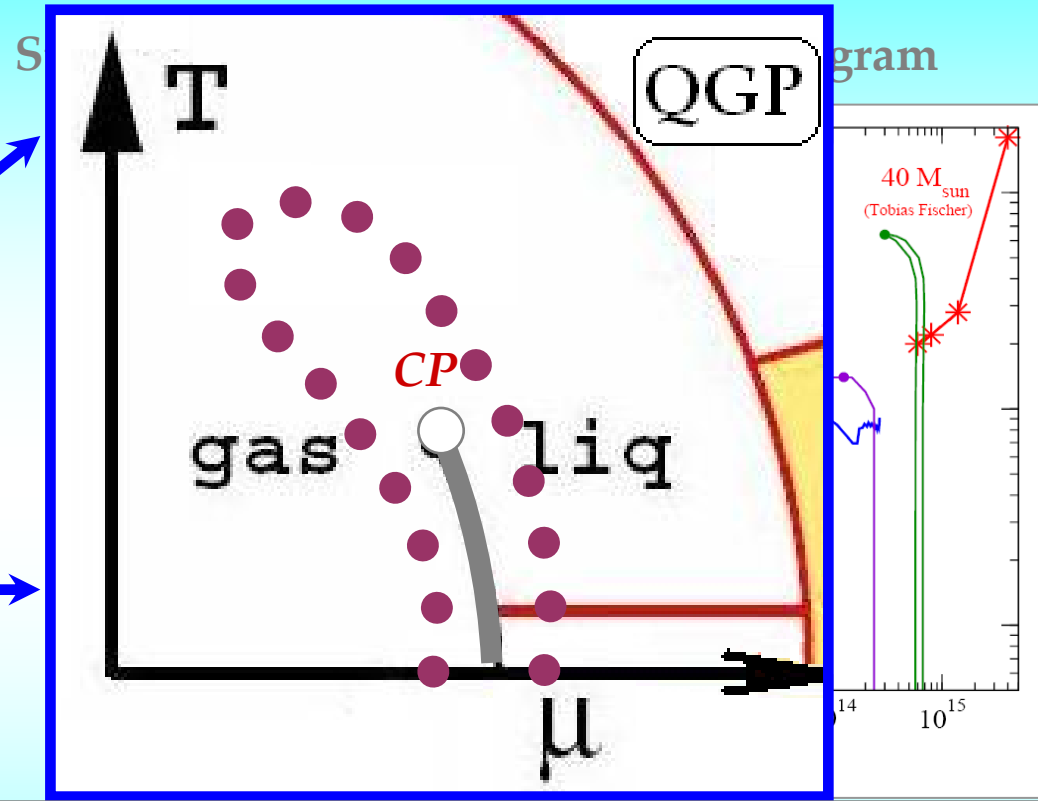
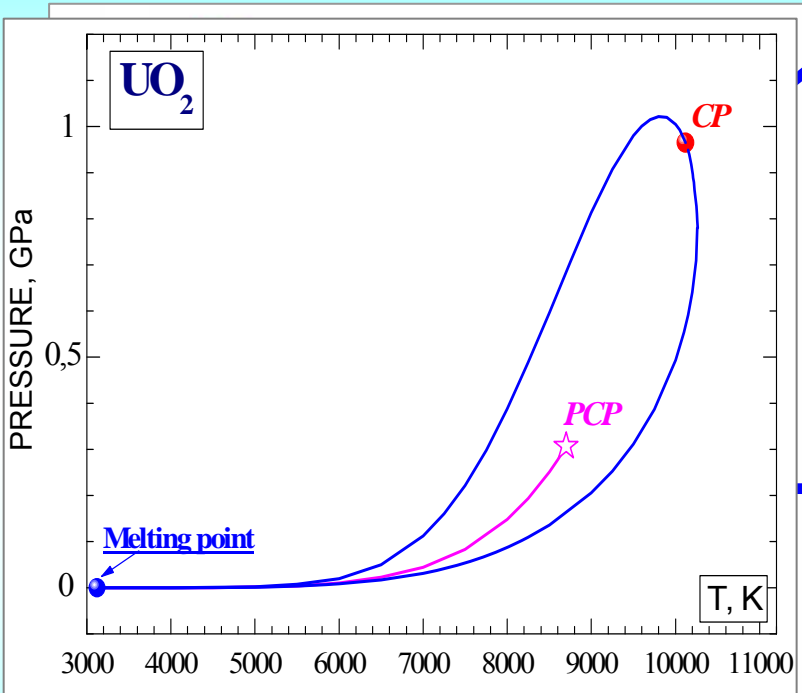
(after D. Blaschke, "Extreme Matter", Elbrus-2010)

- "Gas-Liquid" phase transitions
- Quark-Hadron phase transitions

(di scussi on)

# Hypothetical non-congruence in compact stars and supernova explosions

Phase Diagram



"Gas-liquid" PT in "low-density" nuclear matter

Ensemble:  $p + n + N(A, Z)$

Equilibrium:  $N(A, Z) = Zp + (A - Z)n$

*No electrons  
No Coulomb effects*

2-dimensional system  $\{p+n\}$

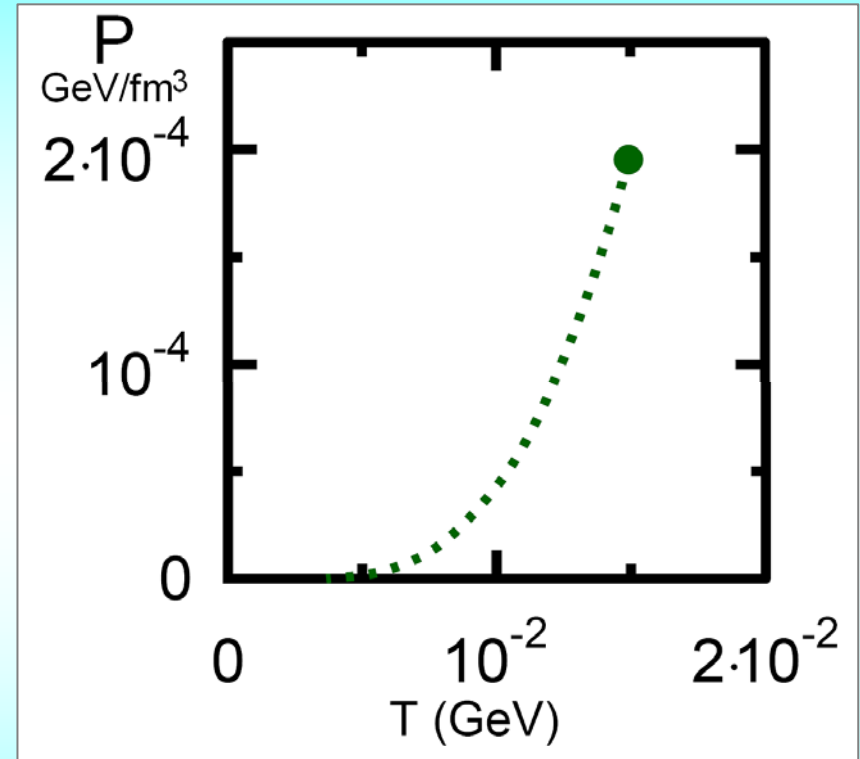
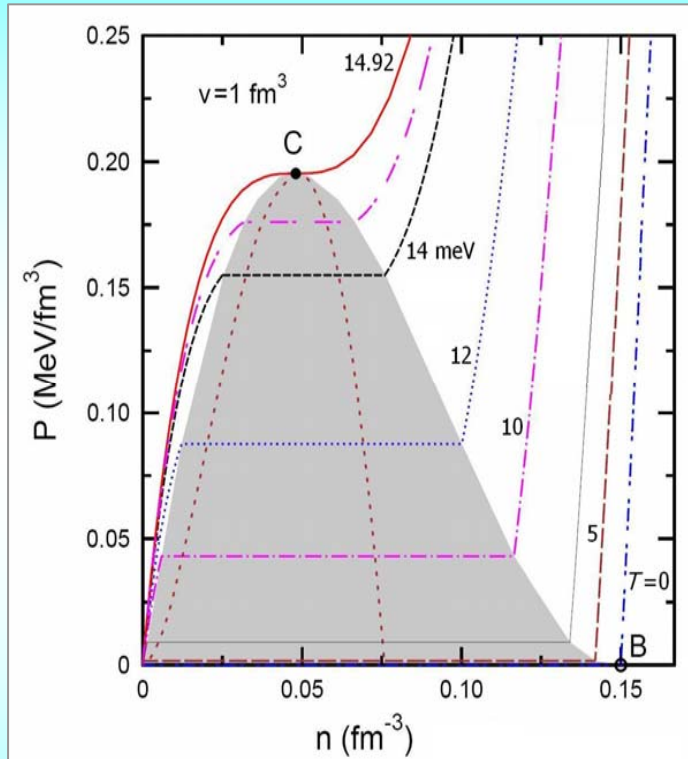


**Non-congruent PT**

*(di scussion)*

# "Gas-liquid" PT *in* "low-density" nuclear matter

Phase diagram of symmetric  $p$ - $n$ - $N(A,Z)$  nuclear matter

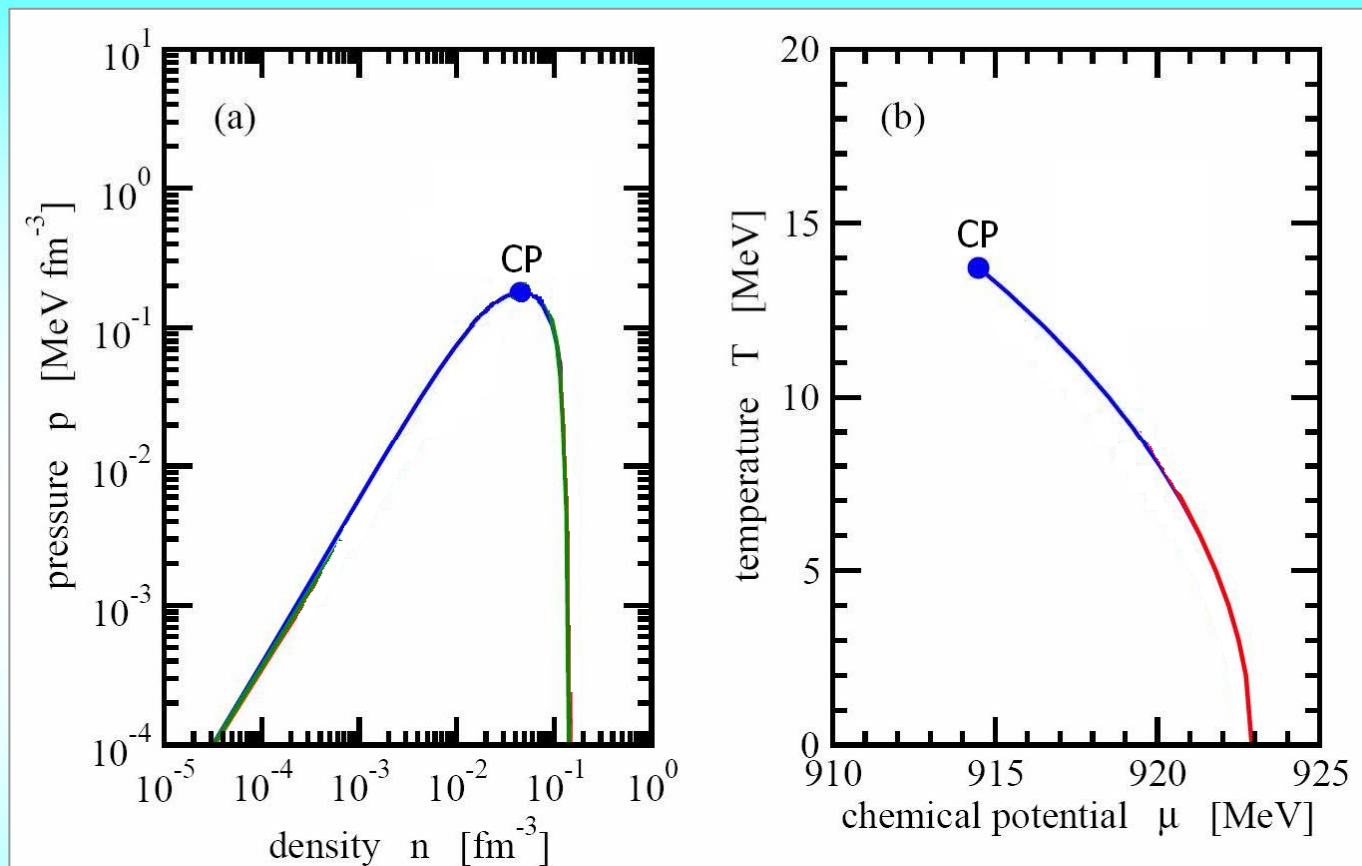


Satarov L., Dmitriev M., Mishustin I.  
*Phys. At. Nucl.* (2009)

## Evident contradiction

*Calculated phase transitions are of ordinary VdW type (congruent) !*

# "Gas-liquid" PT *in* "low-density" nuclear matter (*di scussi on*)



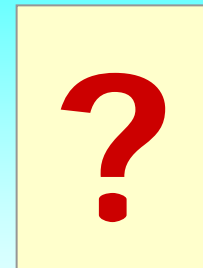
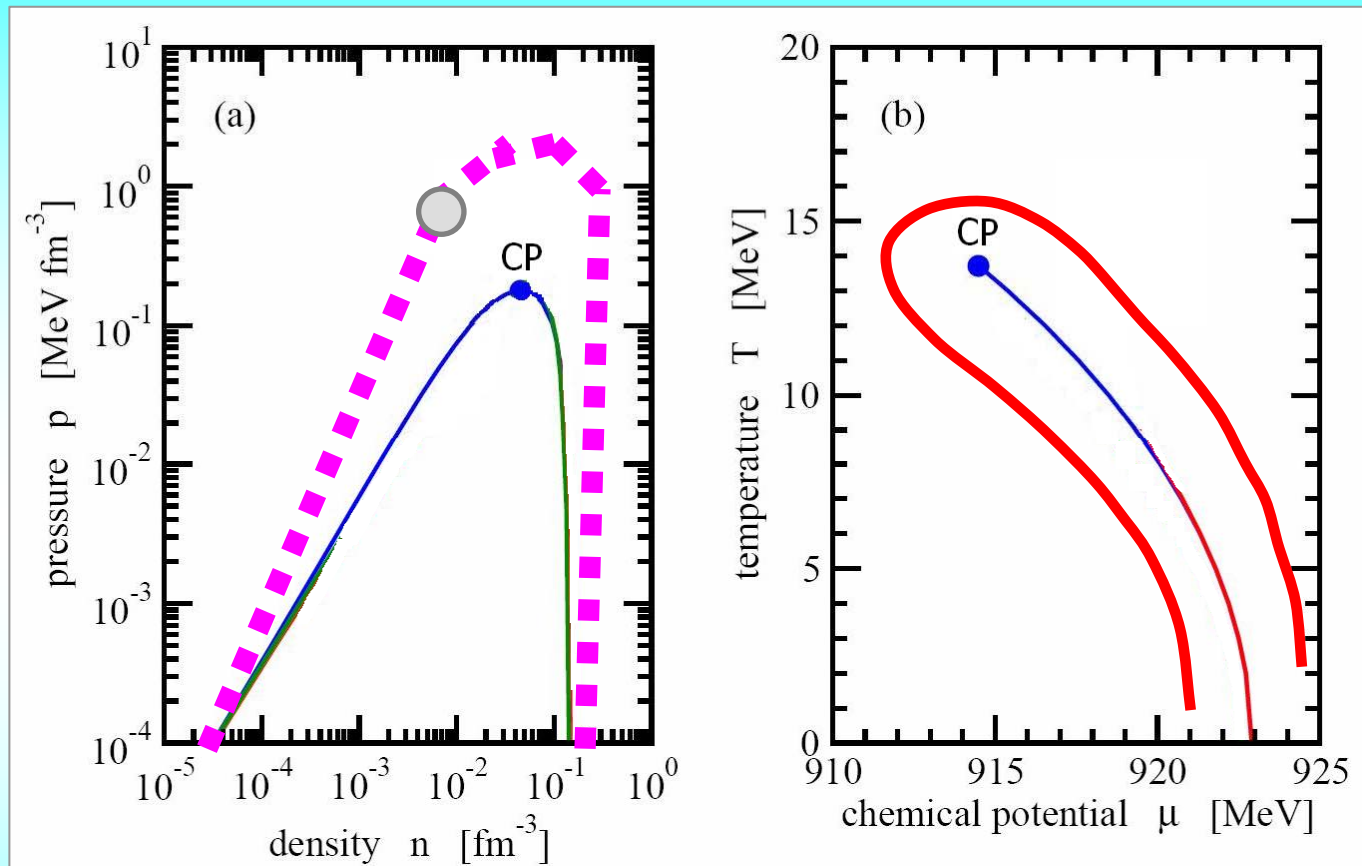
S. Typel, G. Röpke, D. Blaschke *et al.* *Phys. Rev. C*, **81** (2010)

## Evident contradiction

*Calculated phase transitions are of ordinary VdW type (congruent) !*



# "Gas-liquid" PT *in* "low-density" nuclear matter (*di scussi on*)



S. Typel, G. Roepke, D. Blaschke *et al.* *Phys. Rev. C*, **81** (2010)

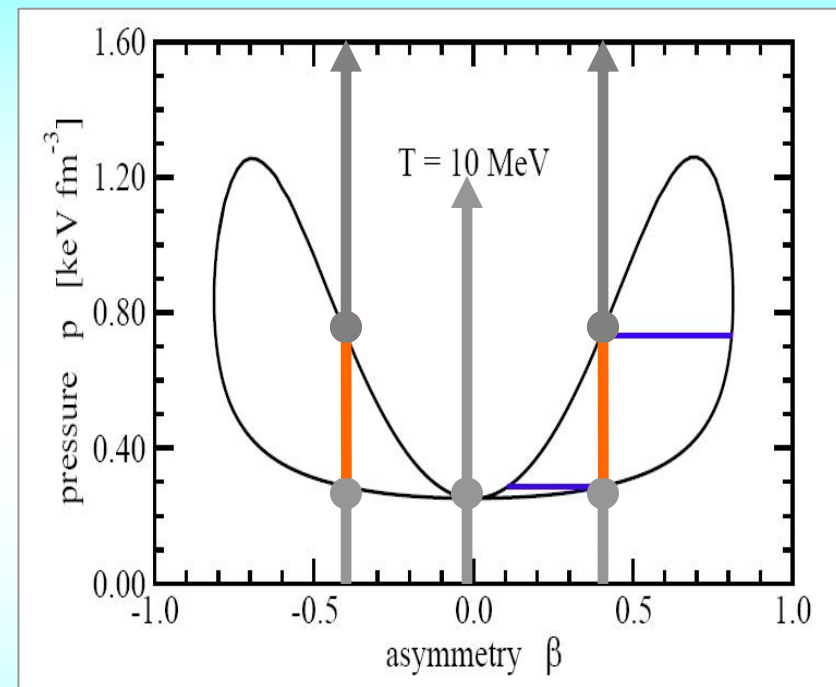
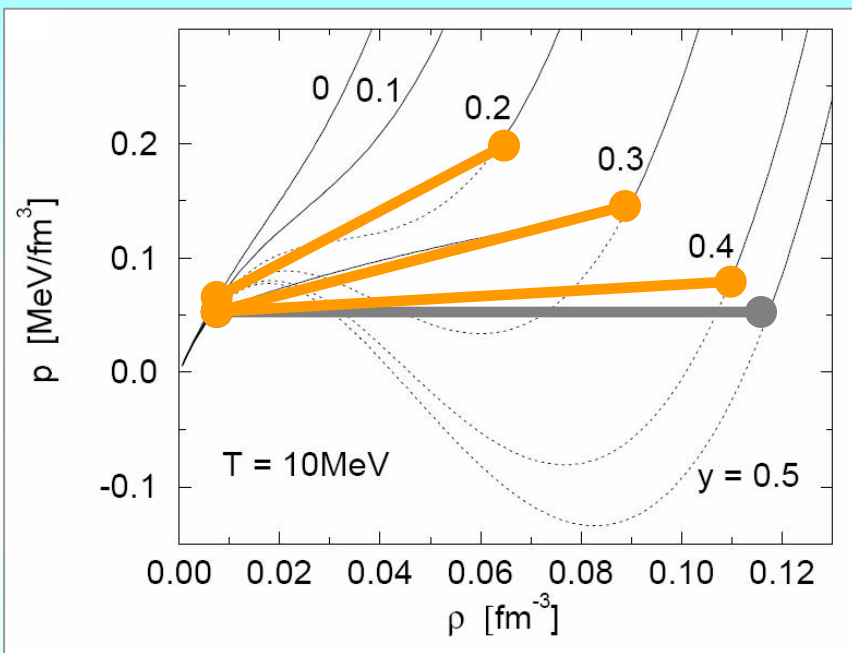
Phase transition in **symmetric**  $p$ - $n$ - $N(A,Z)$  nuclear matter is **congruent**

**Aseotropic** composition

# "Gas-liquid" PT *in* "low-density" nuclear matter

(*di scussi on*)

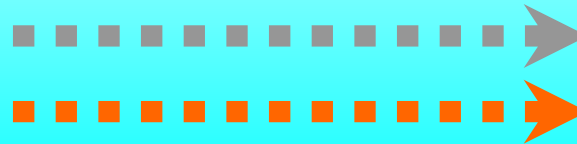
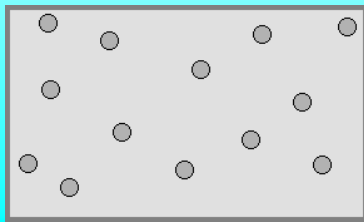
Phase transition in **non-symmetric**  $p$ - $n$ - $N(A,Z)$  nuclear matter is **non-congruent** !



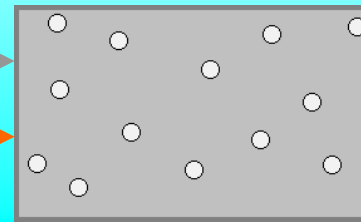
Muller H., Serot B., *Phys. Rev. C* **52** (1995)  
nucl-th/9505013

(after S. Typel, HIC for FAIR, Prerow-2009)

"Dew" point

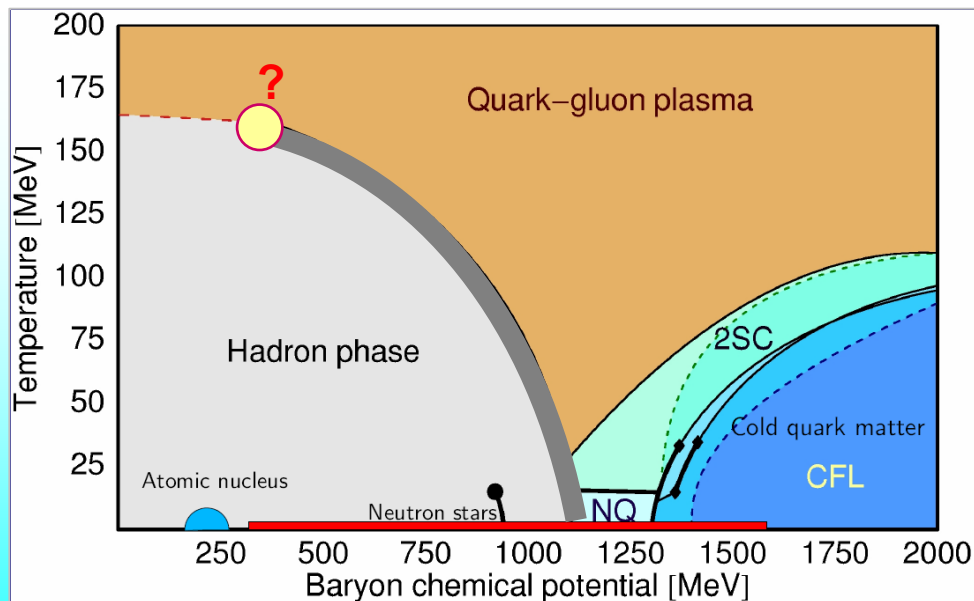


"Bubble" point



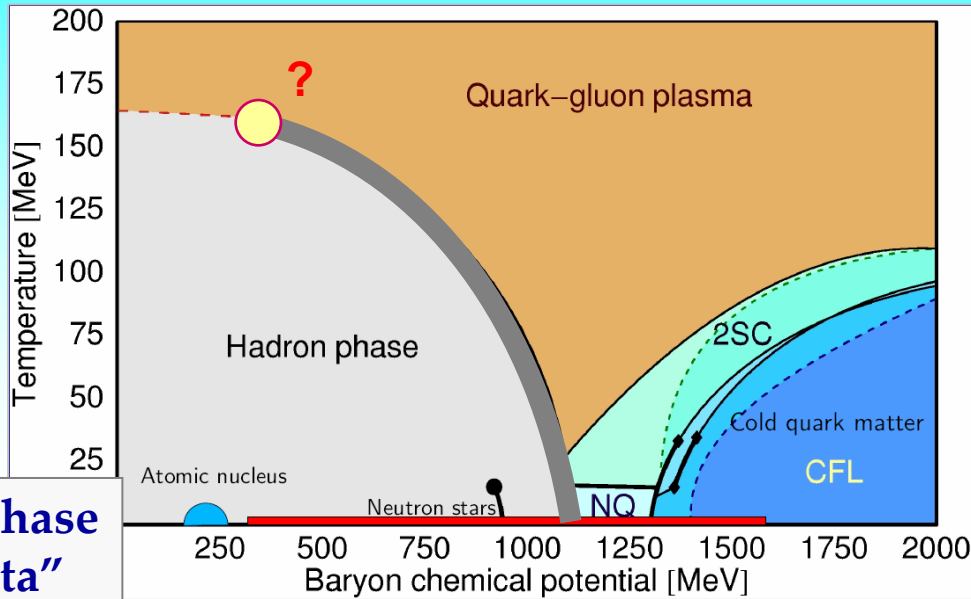
(*di scussi on*)

## Quark-hadron phase transition



# Hypothetical quark-hadron phase transition

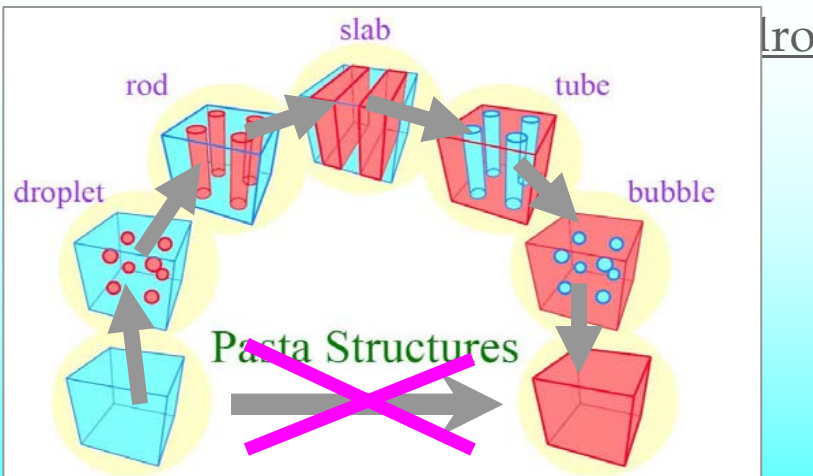
is it CONGRUENT or NON-CONGRUENT ?



Sequence of five  
(or more ?)  
mini-phase transitions !

Uniform (nucleons) →  
→ Drops → Rods →  
→ Slabs → Bubbles →  
→ Uniform (quarks)

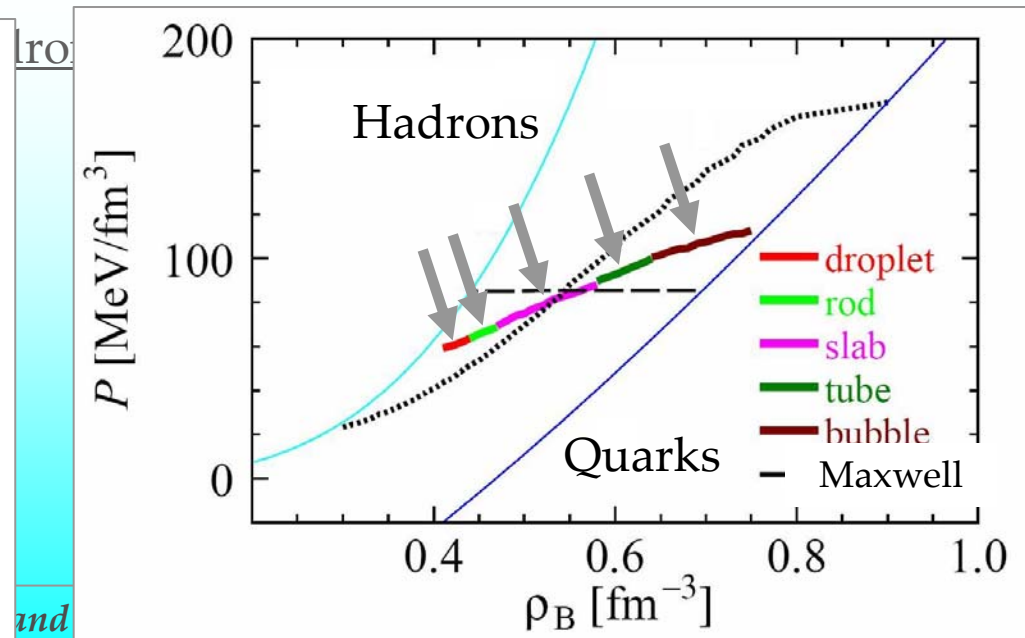
Structured Mixed Phase  
Concept ↔ "Pasta"



Schematic picture of pasta structures. Phase transition from blue phase (left-bottom) to red phase (right-bottom) is considered.

Pasta structures in compact stars  
/arXiv:nucl-th/0605075v2 /2006/

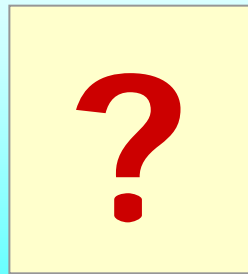
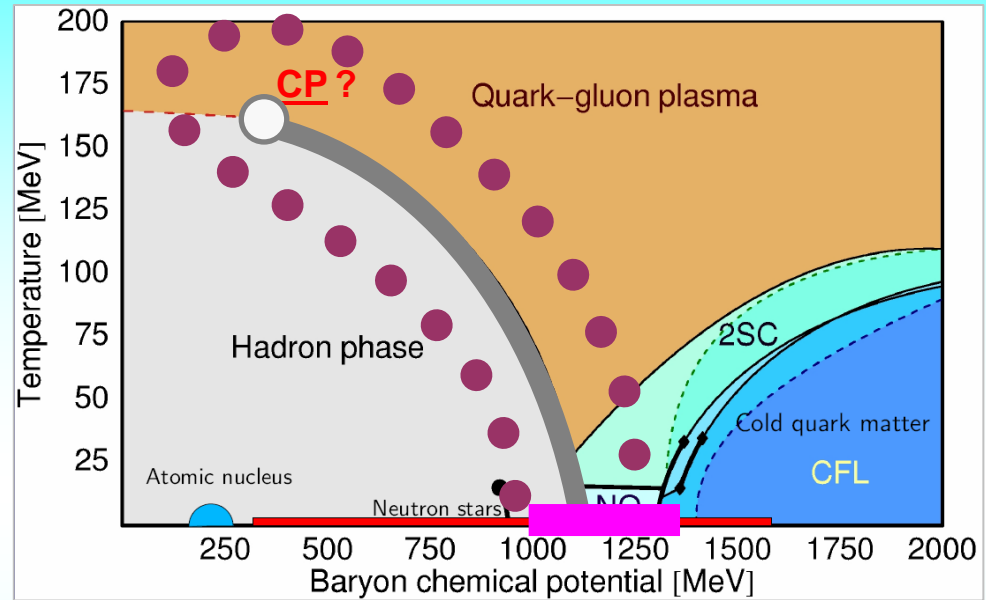
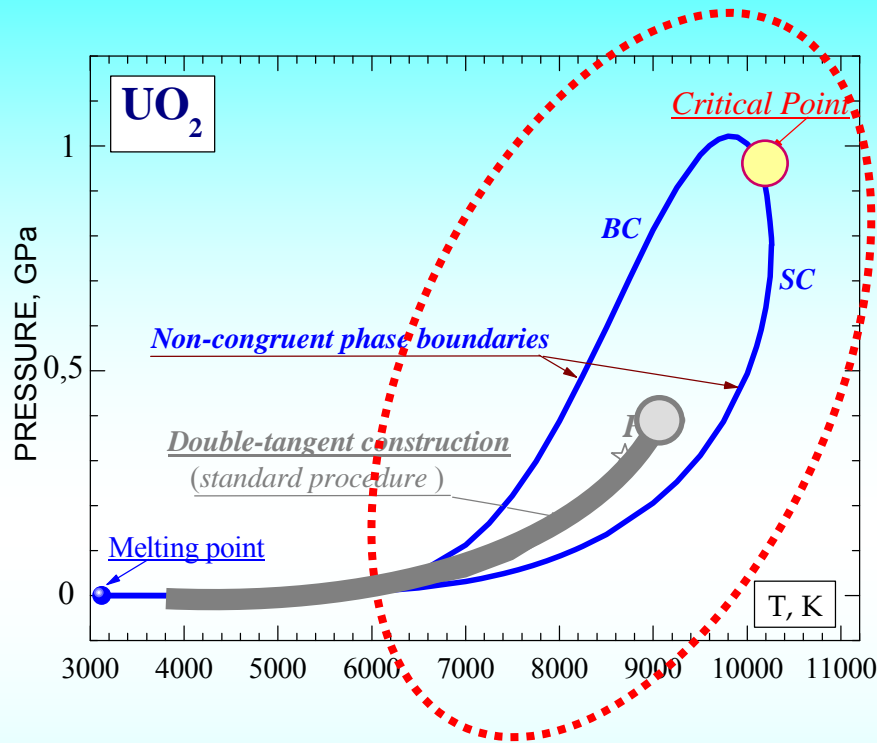
Maruyama T., Tatsumi T., Endo T., Chiba S.

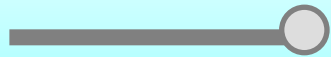



and

# Hypothetical phase transitions in ultra-dense matter: are they CONGRUENT or NON-CONGRUENT ?

Phase diagram of quark-hadron matter

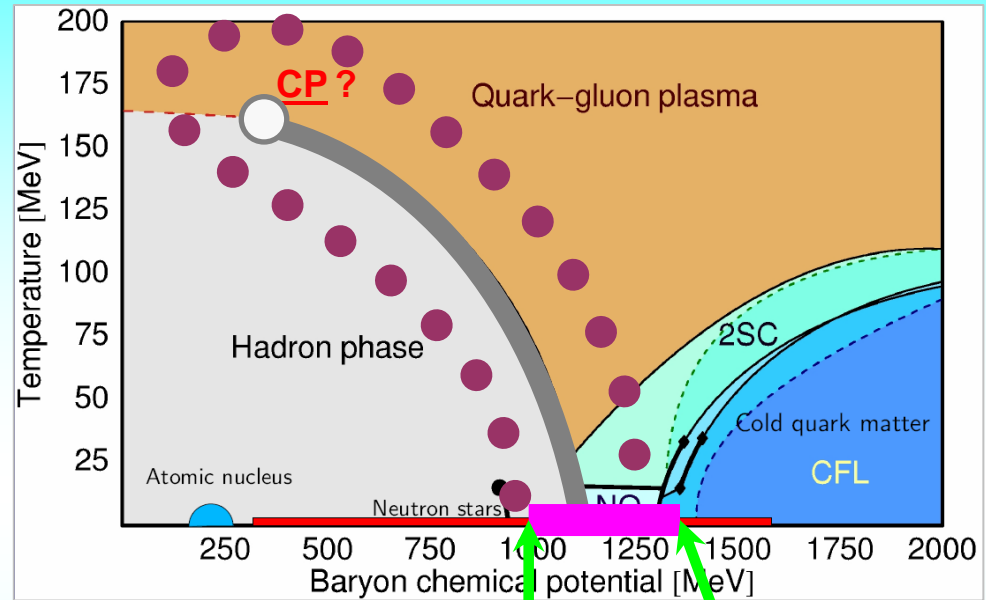
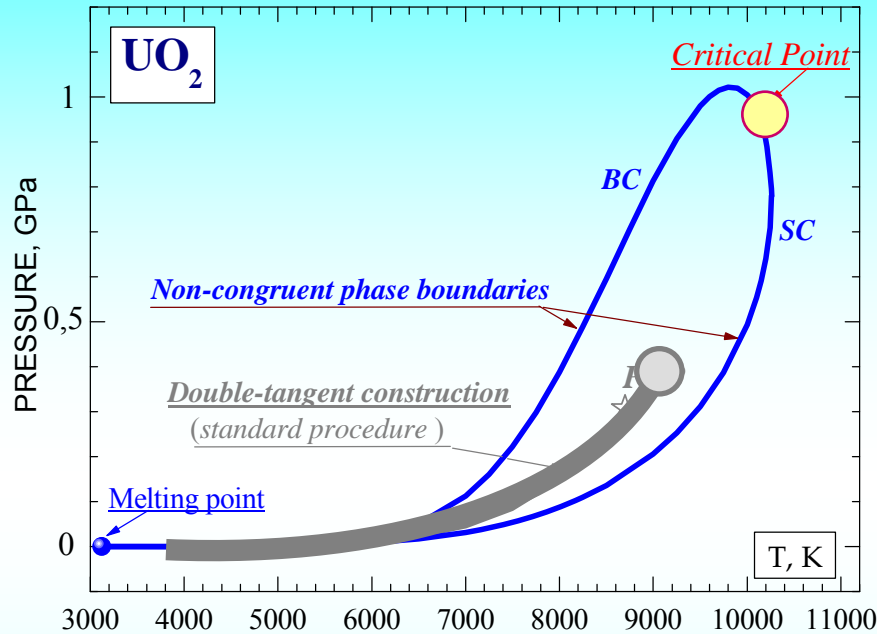


-  - Forced-congruent phase transition
-  - Non-congruent phase transition

I.Iosilevskiy: "Physics of Neutron Stars", St.-Pb. Russia, 2008 //  
EMMI-Workshop\_Max Born Symposium, Wroclaw, 2009 // [arXiv:1005.4192](https://arxiv.org/abs/1005.4192)

# Hypothetical phase transitions in ultra-dense matter: are they CONGRUENT or NON-CONGRUENT ?

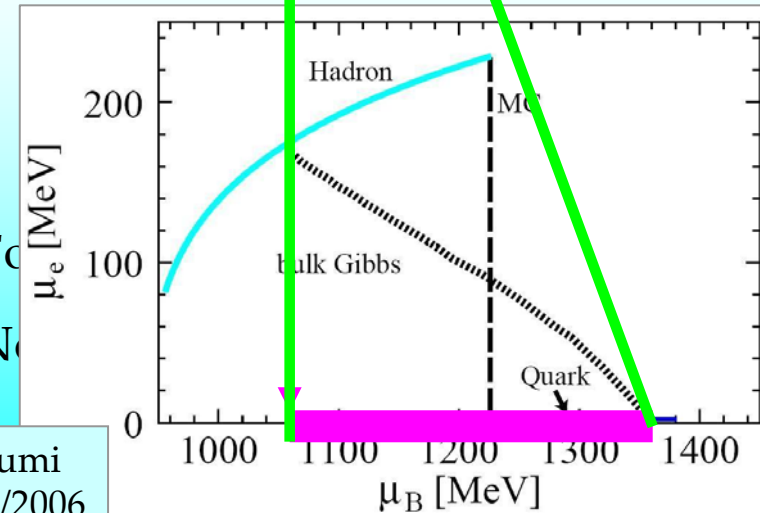
Phase diagram of quark-hadron matter



**NB !**

Supposed gap in chemical potential in **Non-Congruent** scenario for phase transition is in agreement with "mixed phase" calculations at  $T = 0$  !

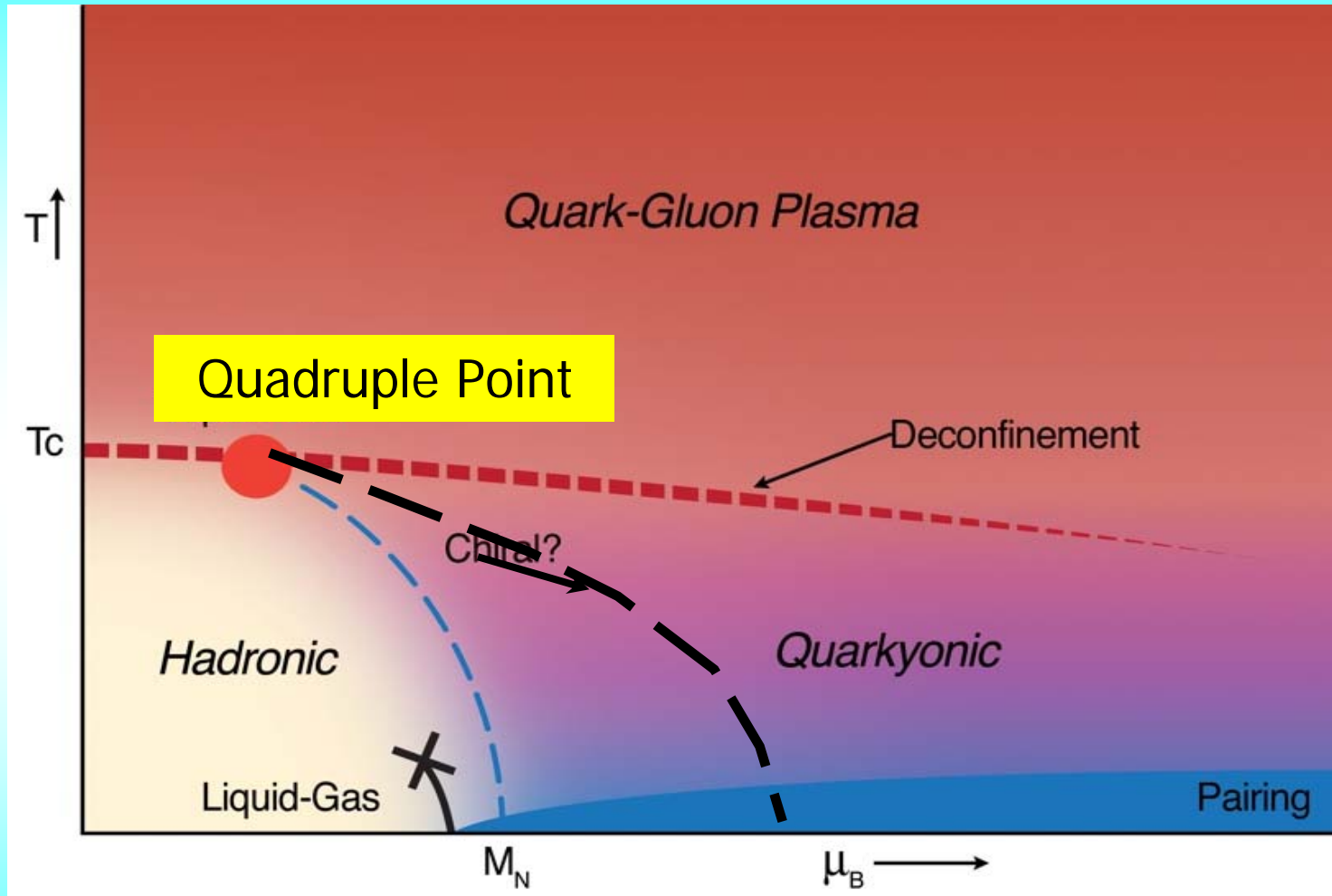
○ -  $F_C$   
■ -  $N_C$



I.L.I. /

T. Endo, T. Maruyama, S. Chiba, T. Tatsumi  
(mixed phase calculations / arXiv:0601017v1/2006)

# Hypothetical phase transitions in ultra-dense matter: are they CONGRUENT or NON-CONGRUENT ?

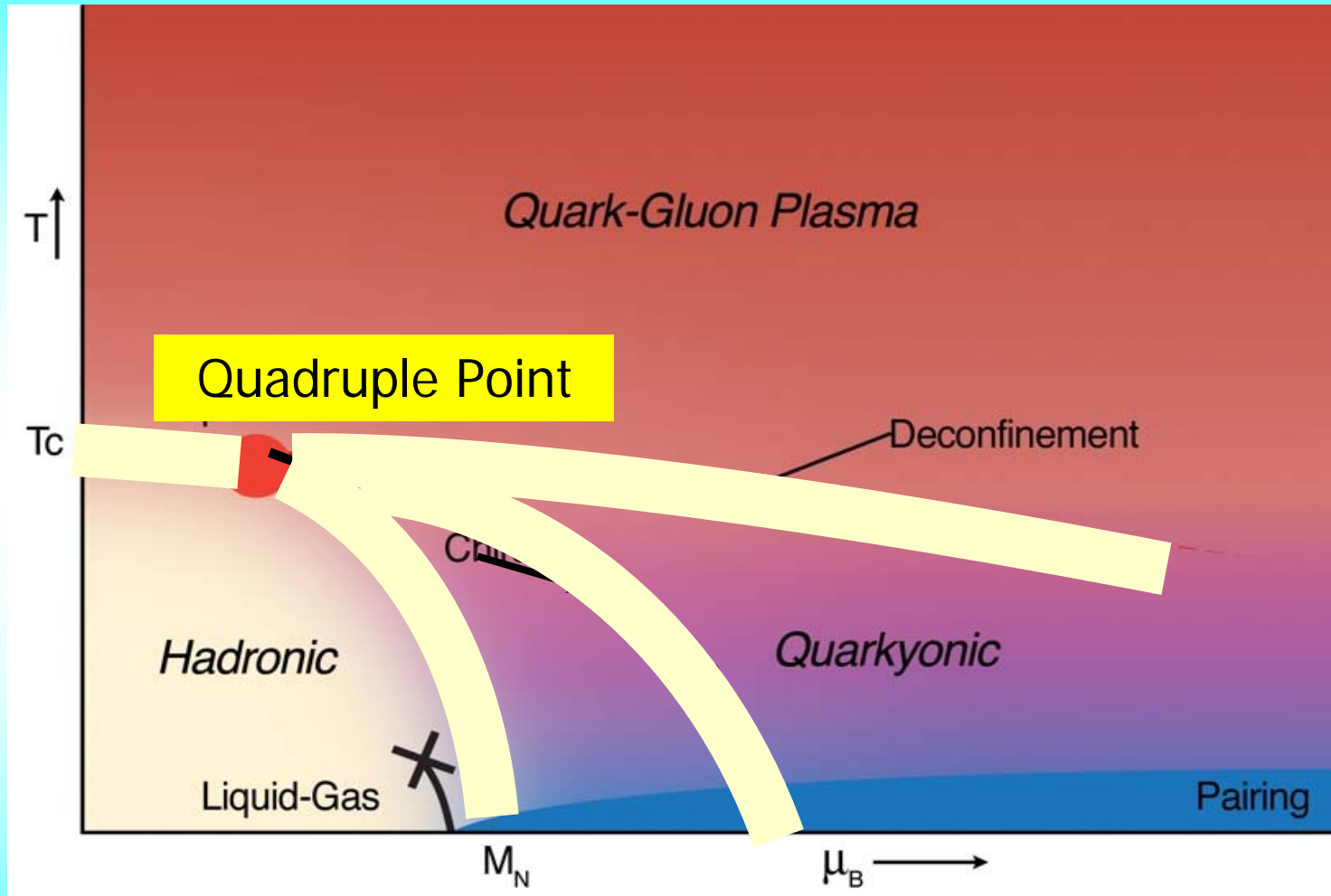


Hypothetical phase diagram with Triple or Quadruple Point

R. Pisarski & L. McLerran: EMMI-Wroclaw /2009/, QCD-Bad Honnef /2010/

# Hypothetical phase transitions in ultra-dense matter:

are they CONGRUENT or **NON-CONGRUENT** ?



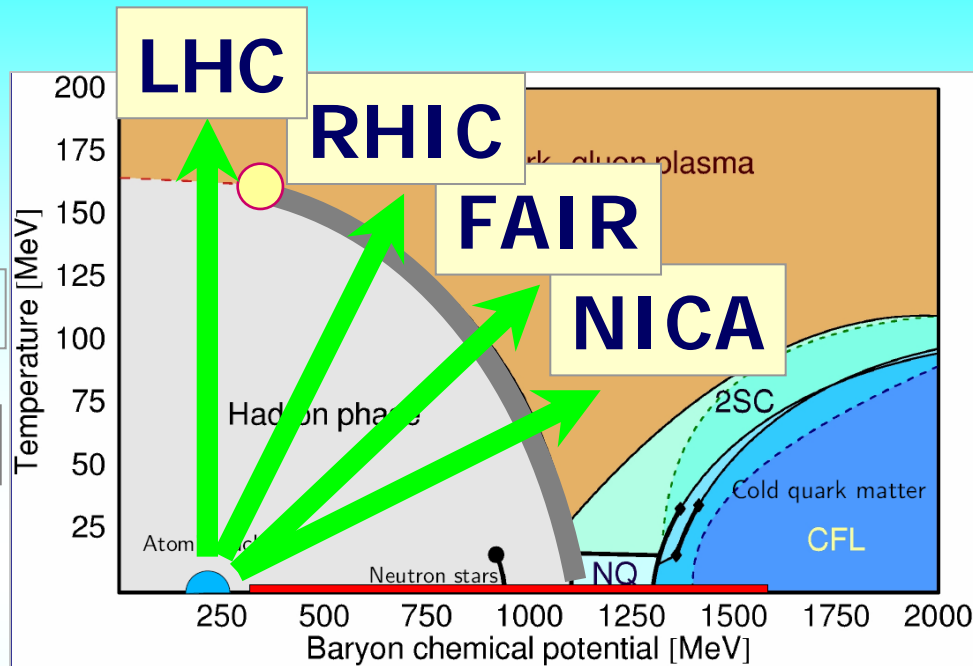
What is this – **Triple** and **Quadruple** points in **Non-Congruent** phase transition ?

I.Iosilevskiy: EMMI-Wroclaw /2009/, QCD-Bad Honnef /2010/



# Hypothetical phase transitions in ultra-dense matter

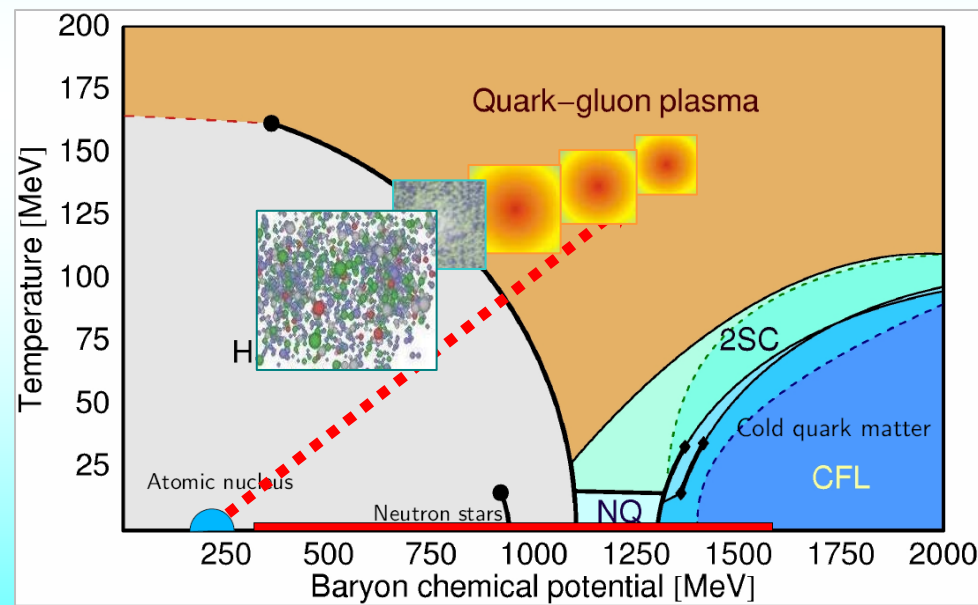
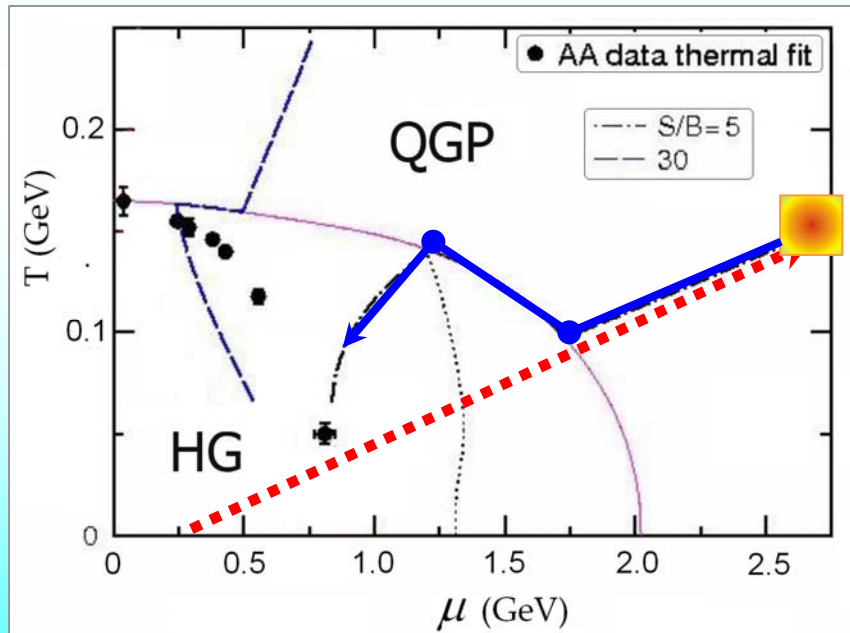
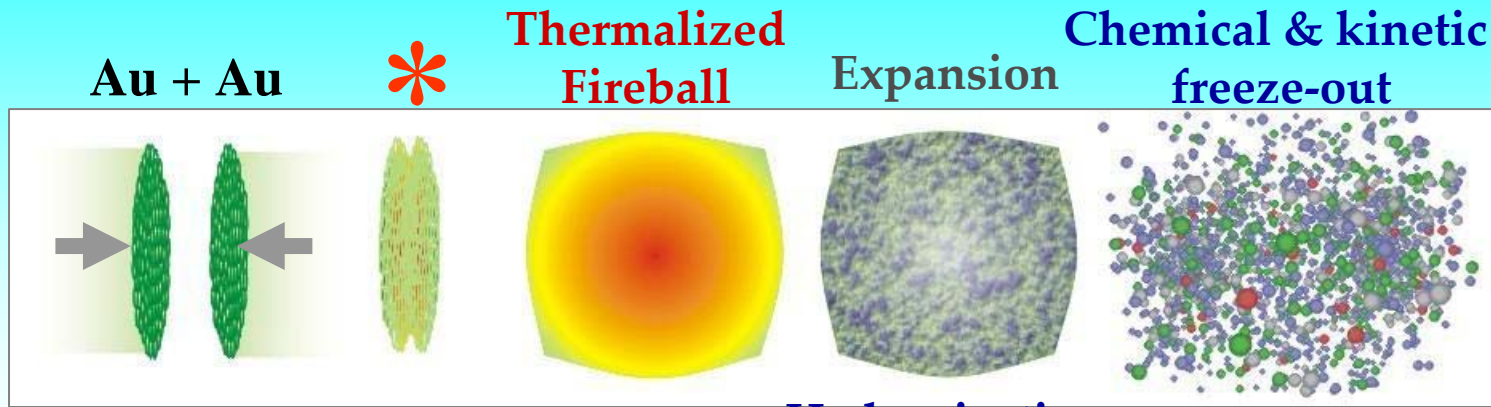
are they CONGRUENT or NON-CONGRUENT ?



Quark-Hadron Phase Diagram

The problem of non-congruence for Quark-Hadron phase transition is relevant to physics of super-colliders !

# Impact *and* fireball hydrodynamics *in* HIC



L.Satarov, M.Dmitriev, I.Mishustin //arXiv: 0901.1430v1

Isentropic expansion of "QGP-Fireball" (schematic)  
/Iosilevskiy: EMMI Workshop, Wroclaw, 2009/

# Conclusions *and* Perspectives

- **Non-congruent** phase transition is **general** phenomenon

- **Non-congruent** phase transition is **universal** phenomenon

- **Non-congruent** phase transition is **interesting** phenomenon

- It is **promising** to investigate non-congruent phase transitions **experimentally**, in particular with **intense laser** and **heavy ion** heating

- It is **promising** to investigate non-congruent phase transitions in **direct numerical simulations** ("numerical experiment") DFT/MD, PIMC, WP/MD...

- If one takes into account hypothetical **non-congruence** of **phase transitions** in **astrophysical** objects (*planets, compact stars etc.*) he should **revise** totally the **scenario** of all phase transformations in these objects

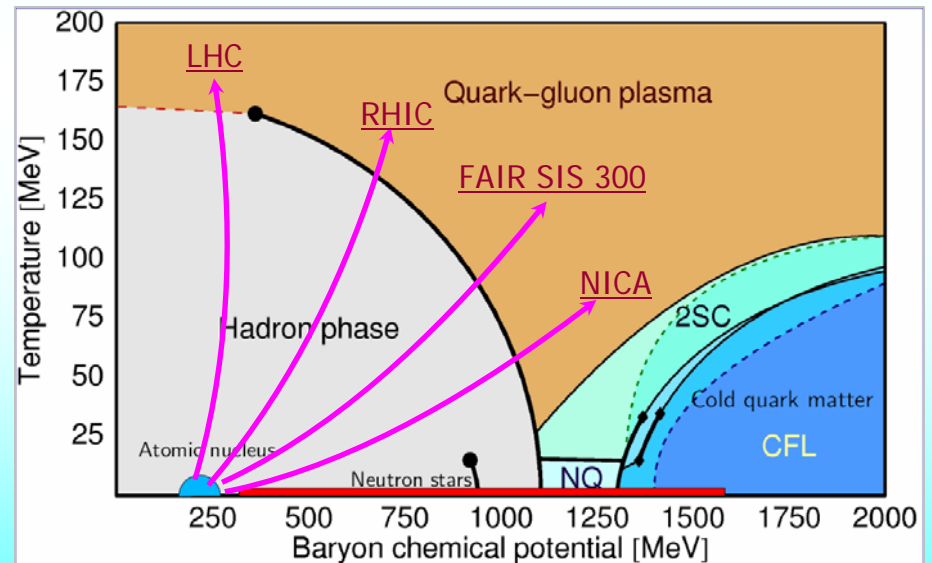
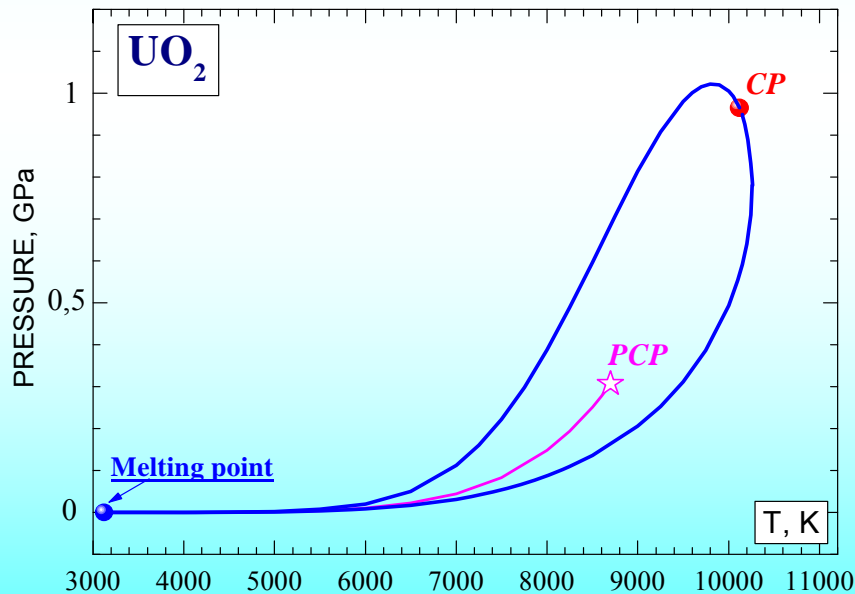
# Cassini-Huygens

MISSION TO SATURN & TITAN



## Non-Congruent Phase Transitions in Cosmic Matter and Laboratory

# Thank you!



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“Physics of Extreme States of Matter” and “Physics of Compressed Matter and Interiors of Planets”

**Extreme Matter Institute - EMMI**

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