

QCD, heavy ion collisions, condensed matter physics and supercomputers

M.I. Polikarpov, ITEP, Moscow

- Introduction: quarks, gluons and QCD
- Millennium problem: Confinement
- Supercomputers and strong interactions
- Heavy ion collisions and computers
- Graphene and computers

Physics of high energy density in matter

21 - 22 November 2011, FAIR-Russia Research Centre, Moscow

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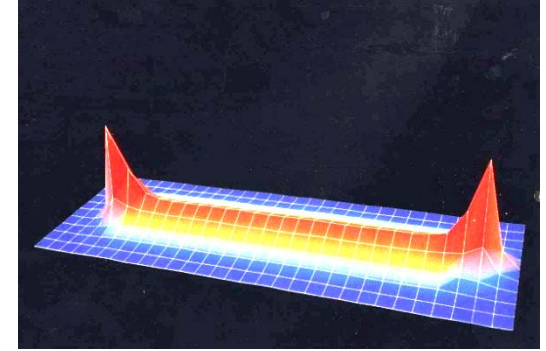
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Physics of high energy density in matter

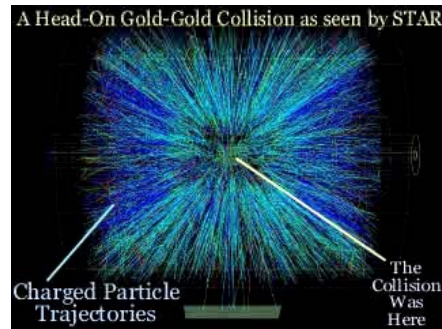
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Three examples of computer simulations of strongly interacting systems

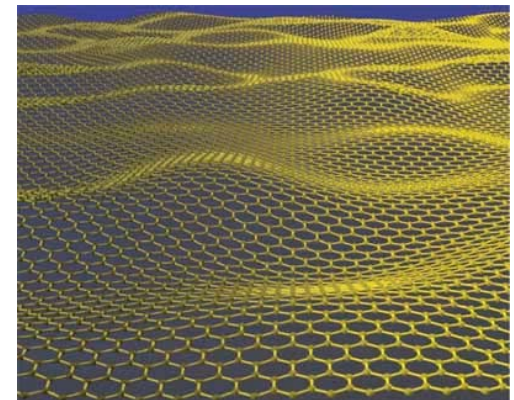
1. Confinement problem in QCD



2. Interference of strong and electromagnetic interactions in heavy ion collisions



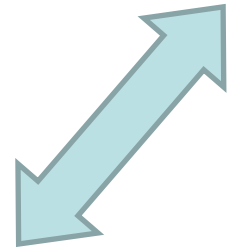
3. Graphene as quantum field theory



Experiment

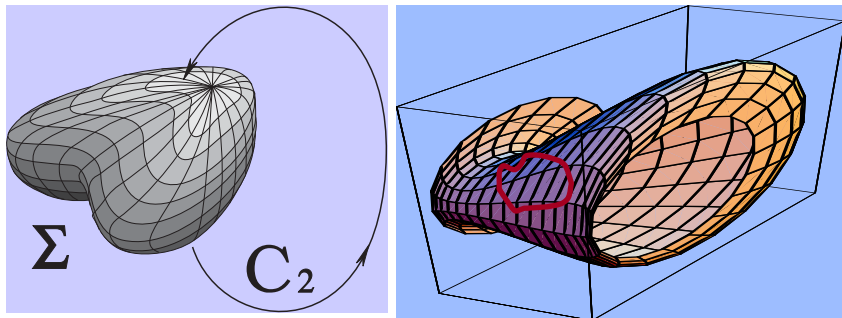
LHC

RHIC



Theory

$$L = -\frac{1}{g^2} \text{Tr} F_{\mu\nu}^2 + \sum_f \bar{\psi}_f (D + m) \psi_f$$



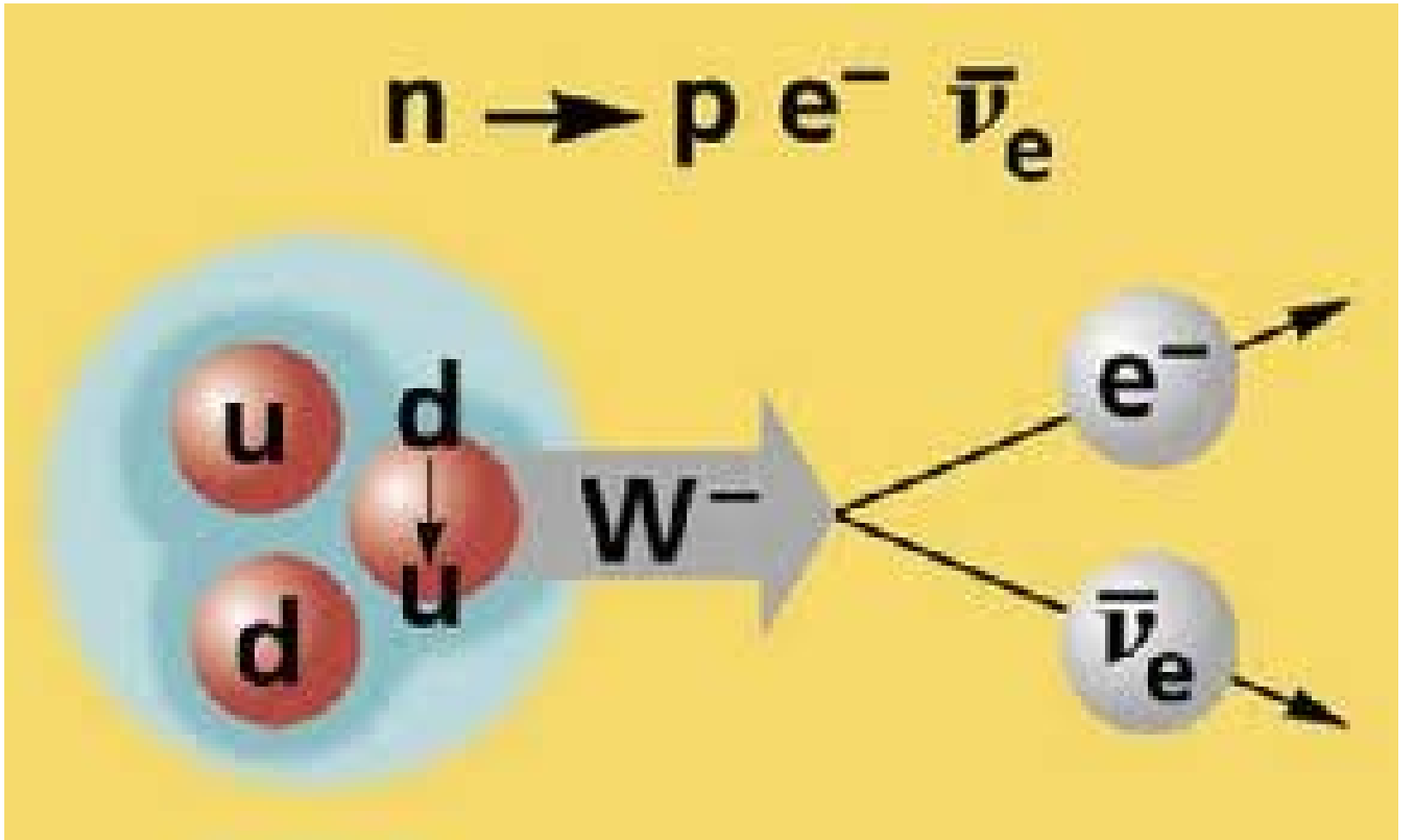
Supercalculations



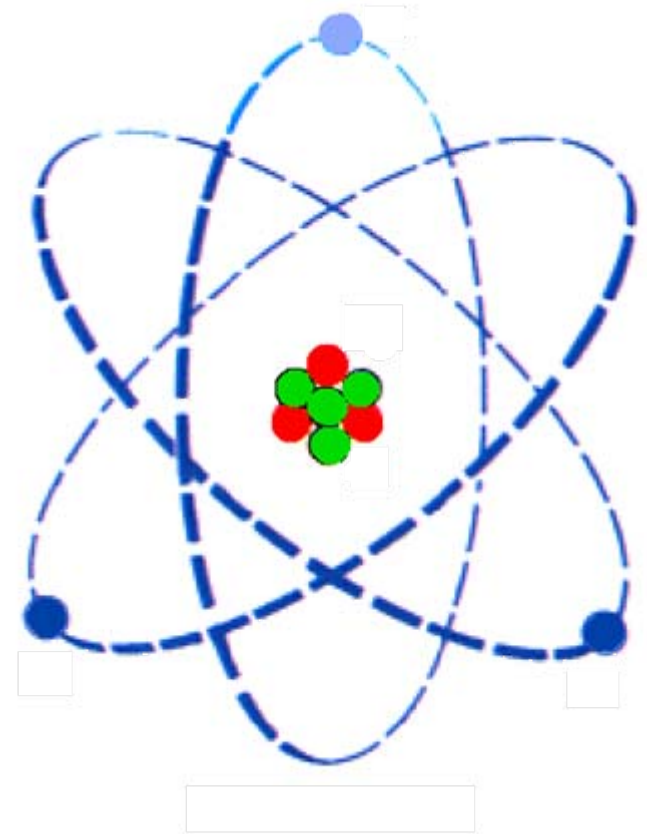
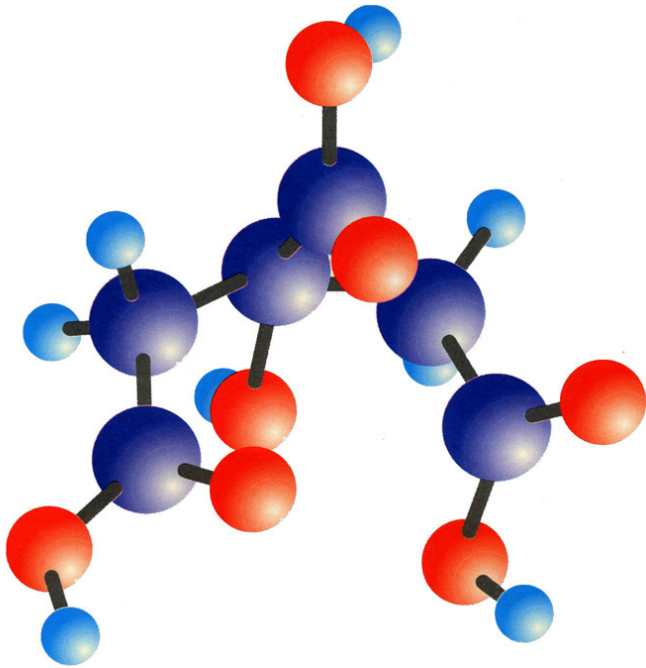
Interactions – 1. Gravity



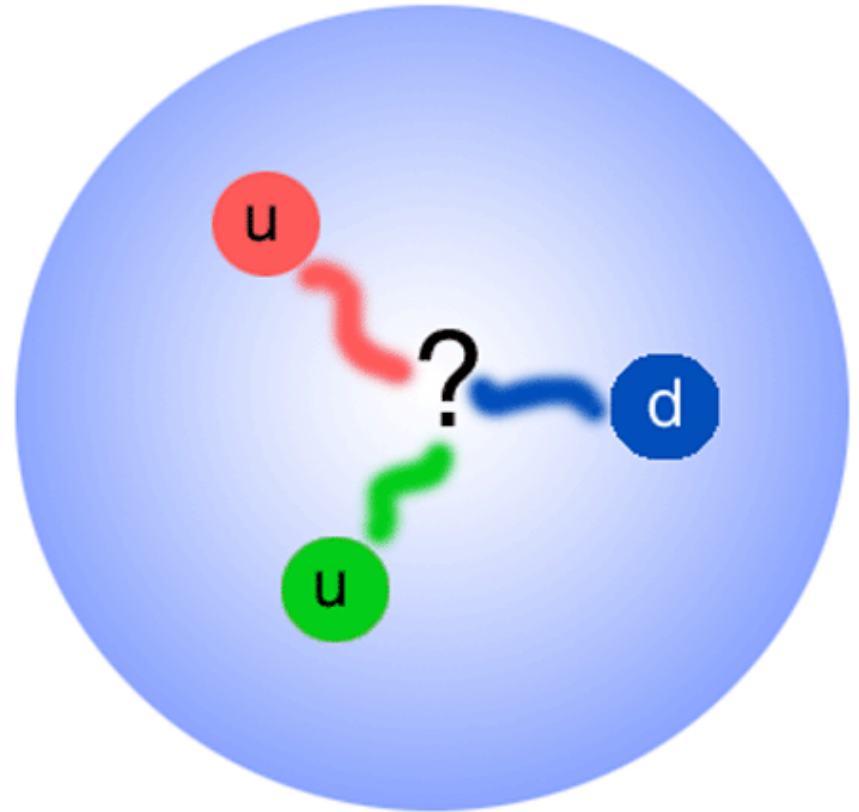
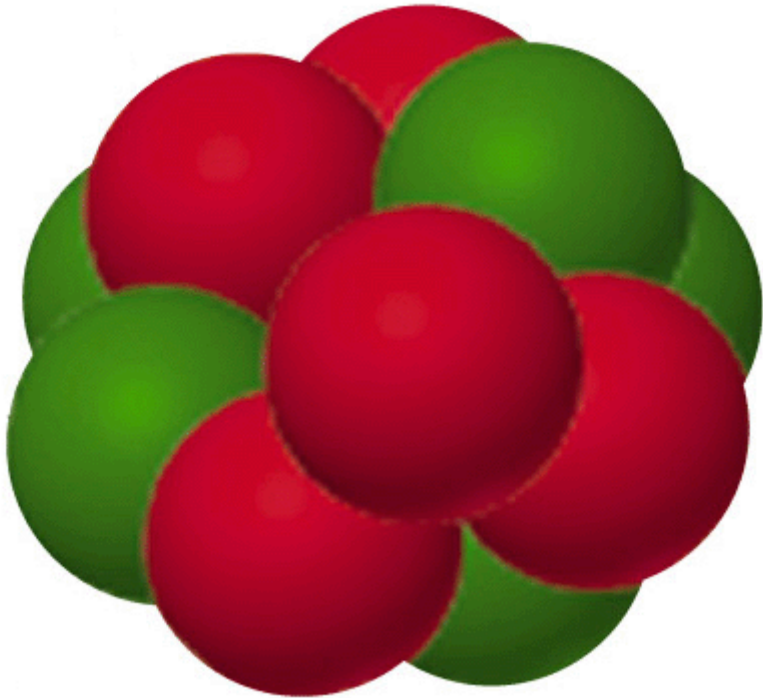
Interactions – 2. Weak



Interactions – 3. Electromagnetism



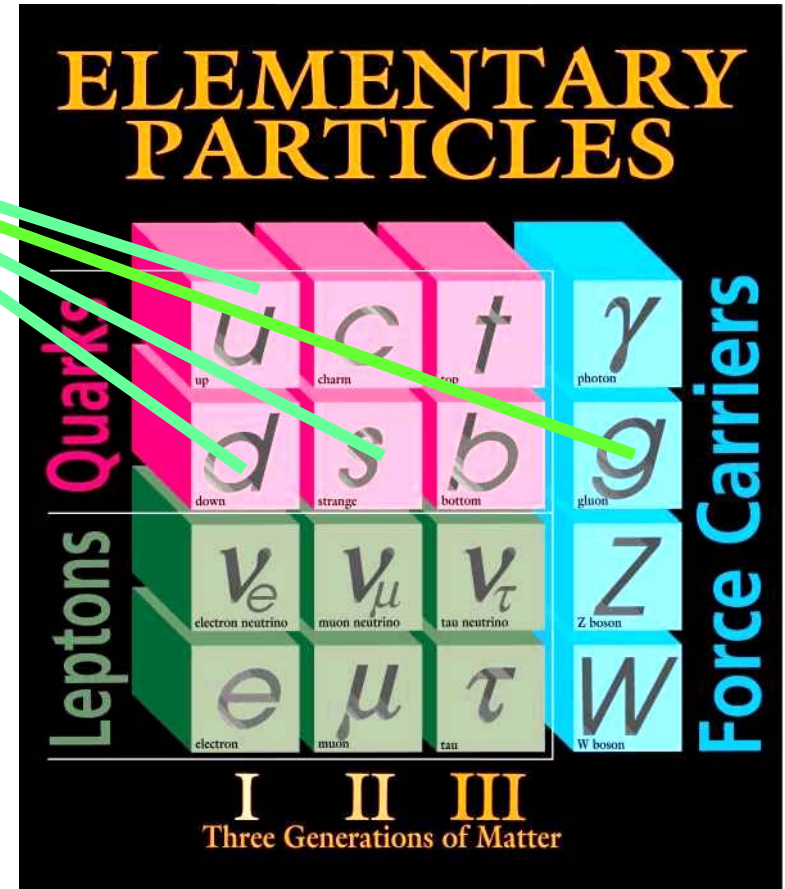
Interactions – 4. Strong



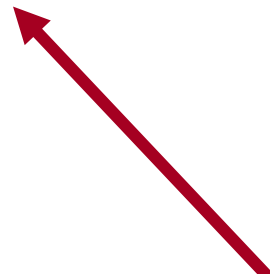
Main problems of strong interaction theory, QCD

Derive from QCD Lagrangian

$$L = -\frac{1}{g^2} \text{Tr} F_{\mu\nu}^2 + \sum_f \bar{\psi}_f (D + m)\psi_f$$



- (1) Hadron spectrum,
- (2) Matrix elements,
- (3) Phase diagram
- (4) Explain color confinement

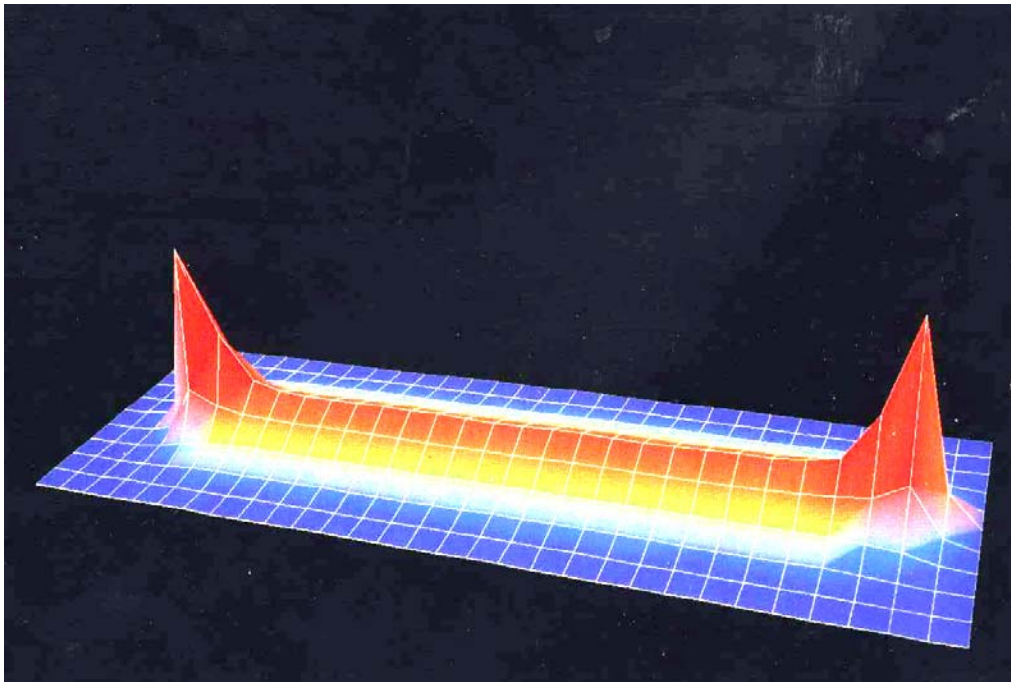


http://www.claymath.org/millennium/Yang-Mills_Theory/ (1 000 000 \$US)

Color confinement

(Why we do not observe free quarks and gluons?)

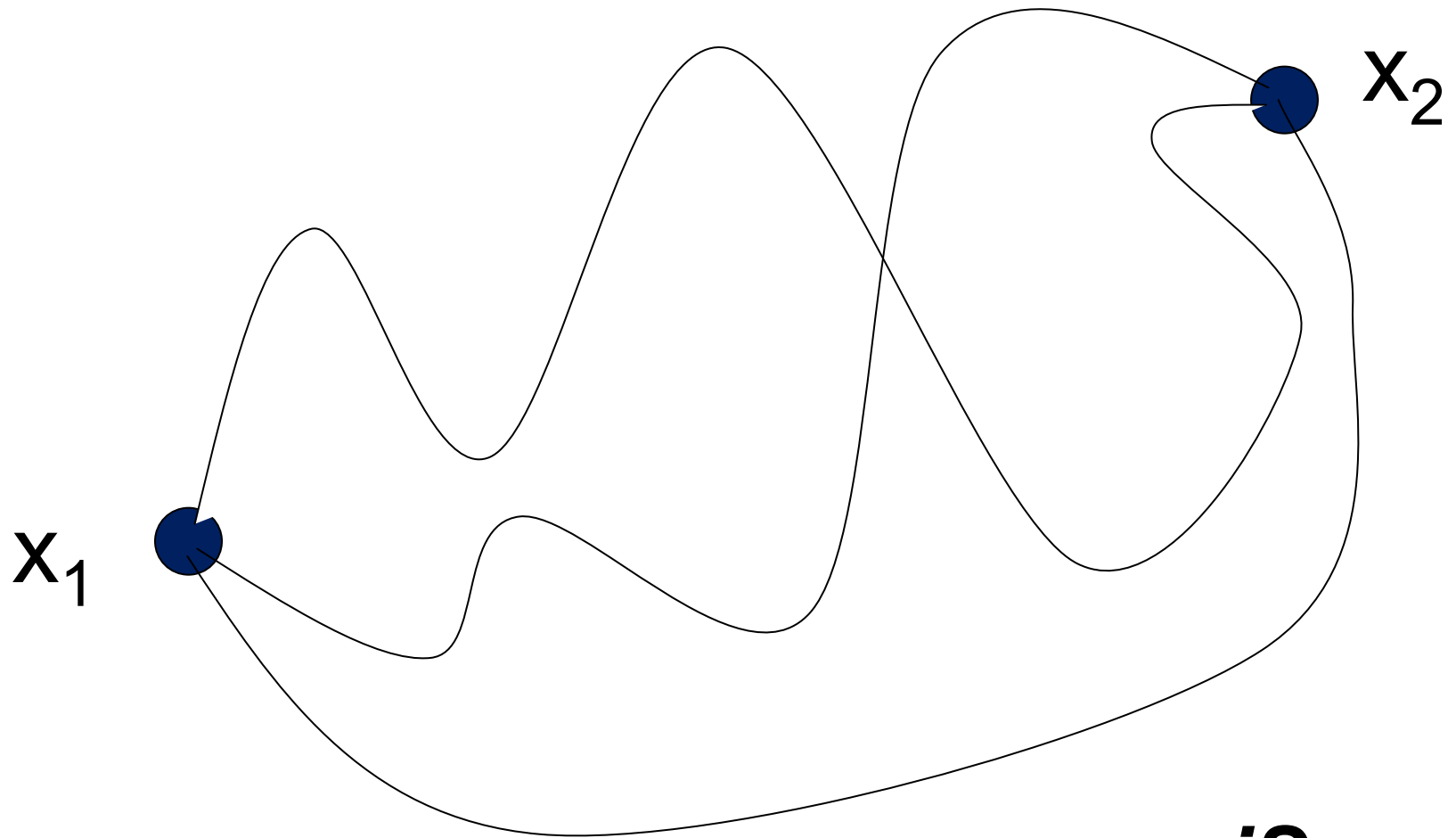
The main difficulty is the absence of first-principle nonperturbative methods in QCD. Computers can prove confinement “numerically”



**Force between
quark and
antiquark is 12
tons!!!**

<http://www.claymath.org/millennium>

Quantum mechanics of a particle



The weight of each trajectory is e^{iS}

Quantum field theory

$$A_{\mu}(x) = A_{\mu}(x, y, z, t)$$

$$-\infty < A_{\mu}(x) < +\infty$$

$$Z = \int \int \int \dots \int \int \int \int DA_{\mu}(x) e^{iS[A_{\mu}]}$$

Methods

- Imaginary time $t \rightarrow it$

$$Z = \int D\varphi \exp\{i S[\varphi]\} \longrightarrow Z = \int D\varphi \exp\{-S[\varphi]\}$$

- Space-time discretization

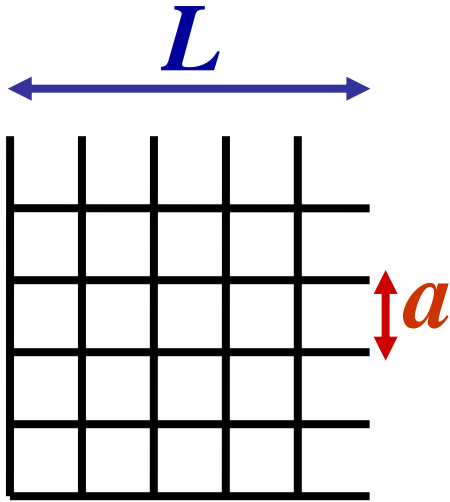
$$D\varphi(x) \Rightarrow \prod_x d\varphi_x$$

$$Z = \int \prod_x d\varphi_x \exp\{-S[\varphi]\}$$

- Thus we get from functional integral the partition function for statistical theory in four dimensions

INTRODUCTION

Three limits



Lattice spacing

Lattice size

Quark mass

$$a \rightarrow 0$$

$$L \rightarrow \infty$$

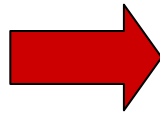
$$m_q \rightarrow 0$$

Typical values

$$a \approx 0.1 \text{ fm}$$

$$L \approx 2 \div 4 \text{ fm}$$

$$m_q \approx 100 \text{ Mev}$$



Extrapolation

+

Chiral perturbation
theory

Typical multiplicity of integrals

For lattice L^4

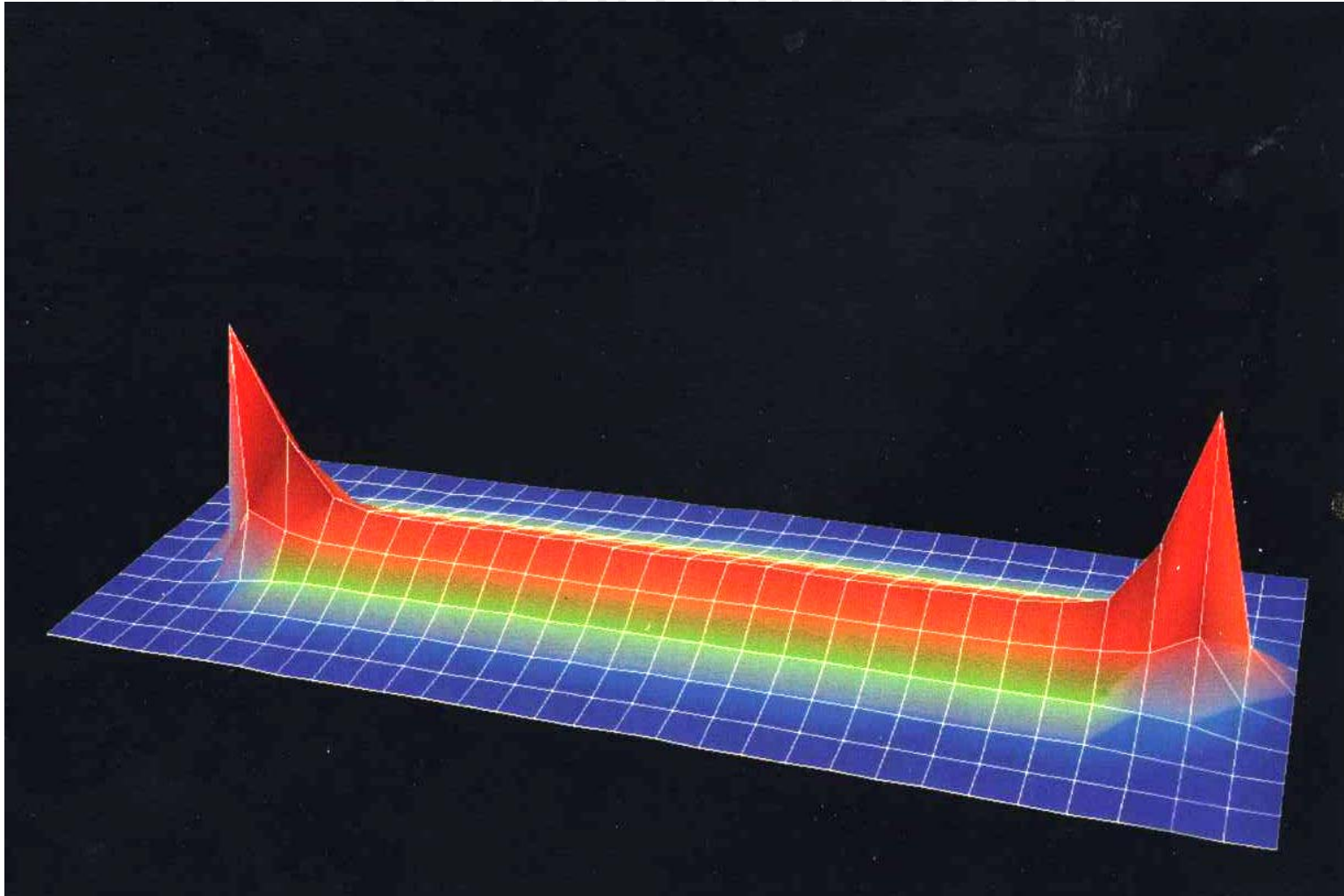
($L=48$, $L^4=5,308,416$)

- **The multiplicity of integrals over gluon fields is $32L^4$ ($L=48$, $32L^4=169,869,312$)**
- **For quark fields we work with matrices $12L^4 \times 12L^4$ ($L=48$, $12L^4=63,700,992$)**

$$\int d\psi d\bar{\psi} \exp\{\bar{\psi} M \psi\} = \det M$$

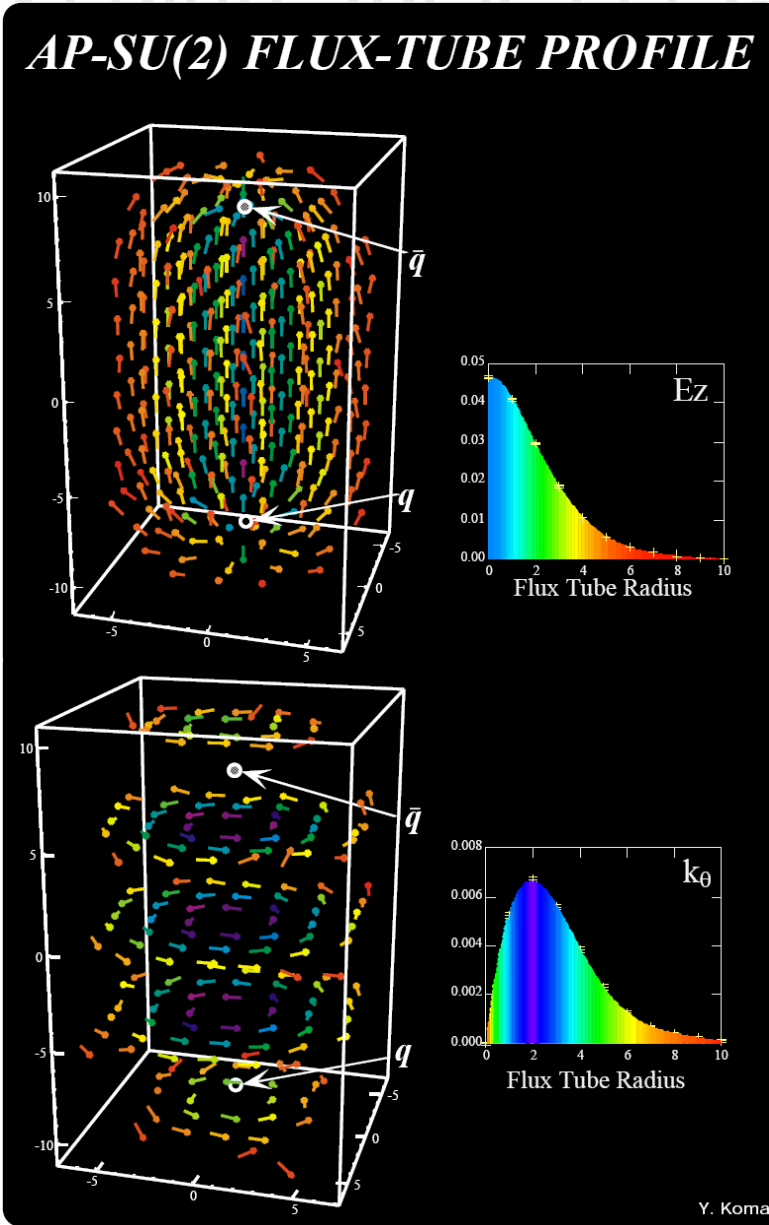
SU(2) glue SU(3) glu

The force between quark and antiquark is 12 tons!!!

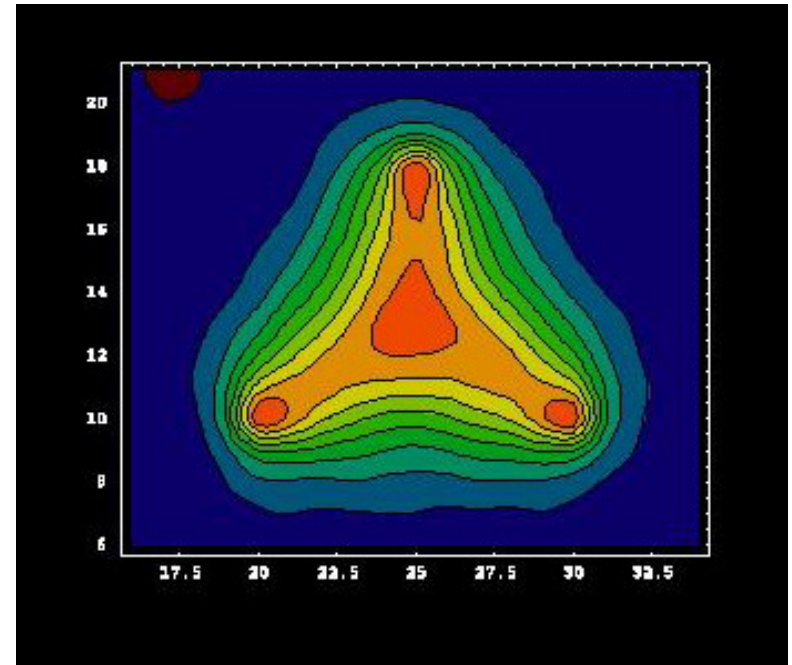
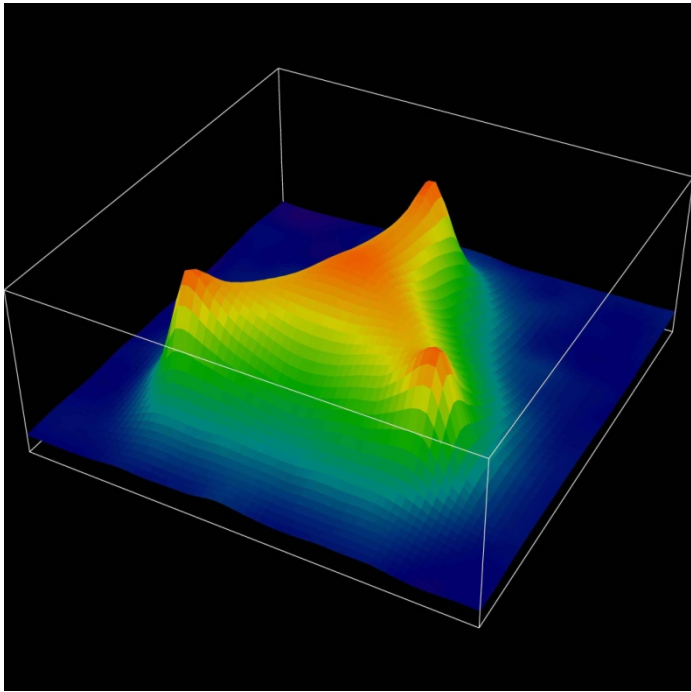


SU(2) glue

SU(2) glue 2+1 QCD (2+1)QCD



SU(2) glue SU(3) glue 2qQCD (2+1)QCD
Three body forces!



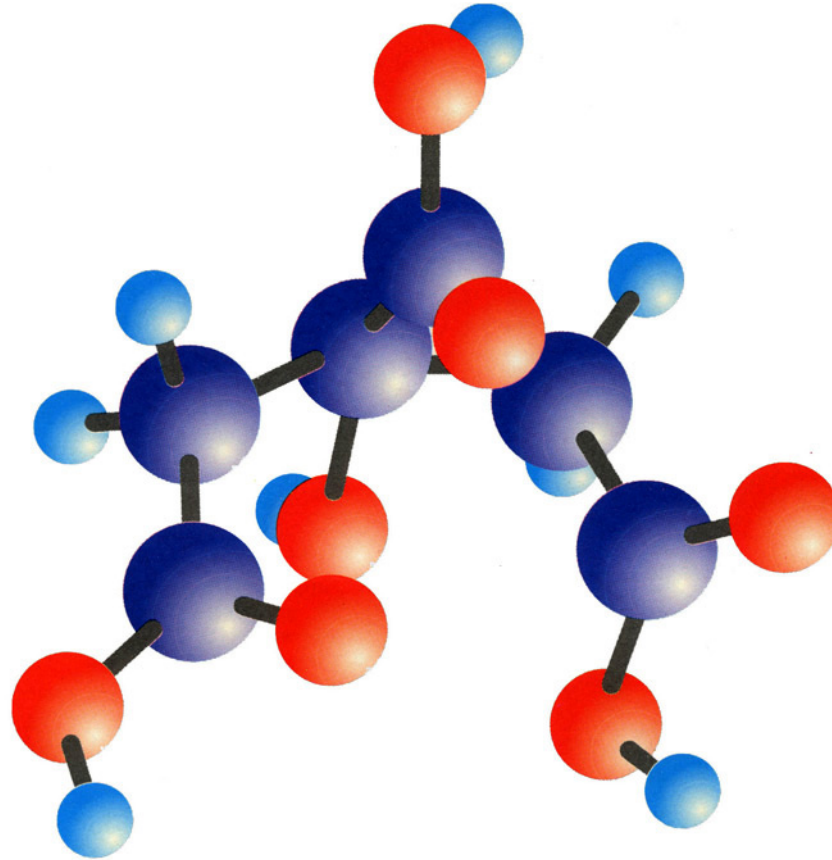
$$V(r_1, r_2, r_3) \neq V(r_1 - r_2) + V(r_2 - r_3) + V(r_3 - r_1)$$

← 1 M →

The origine of the mass

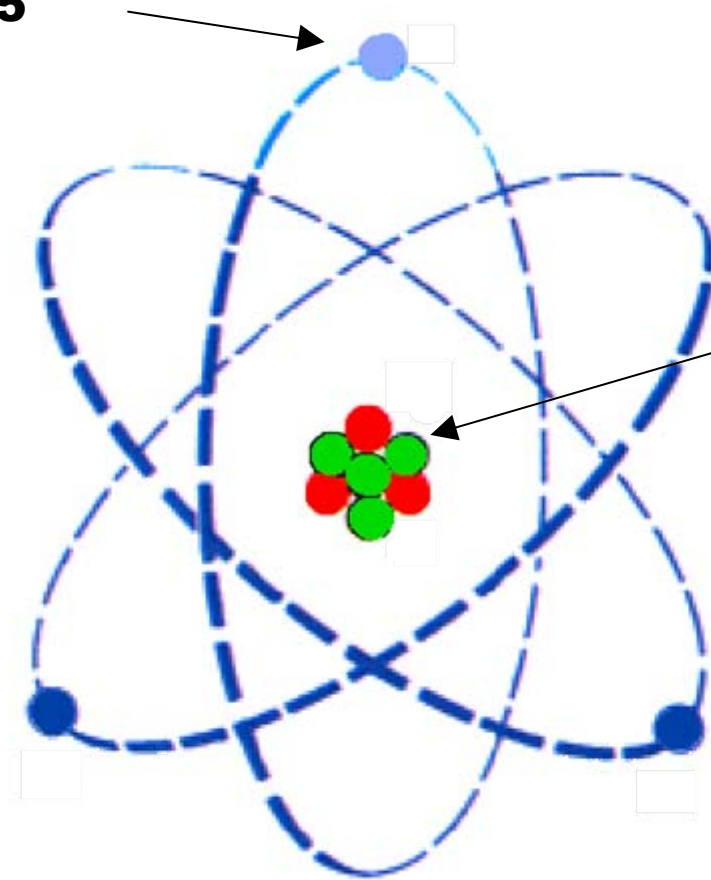


← $10^{-8..10}$ M →



$\longleftrightarrow 10^{-10} \text{ M} \longrightarrow$

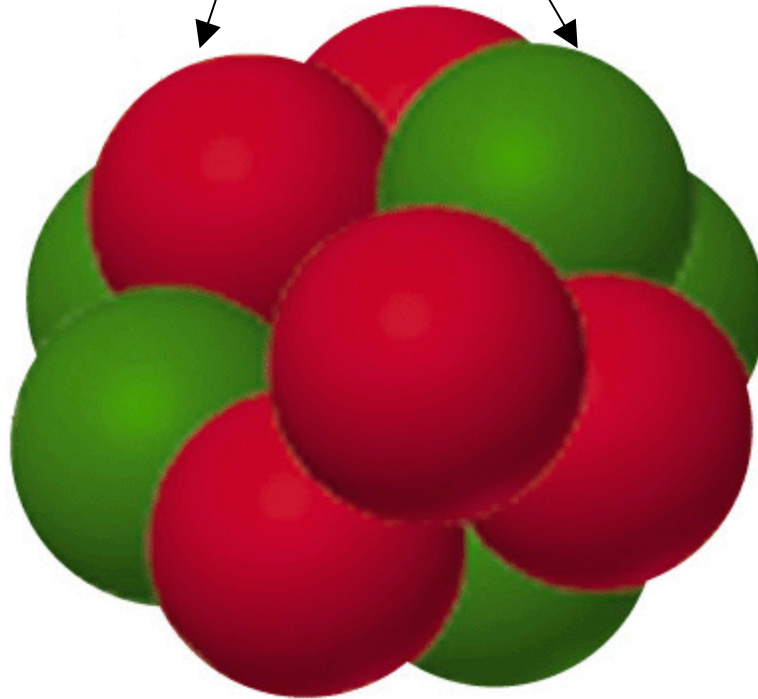
$m_e \approx 0.5$
MeV



$m_n \approx 1000$
MeV

← $10^{-14..15}$ M →

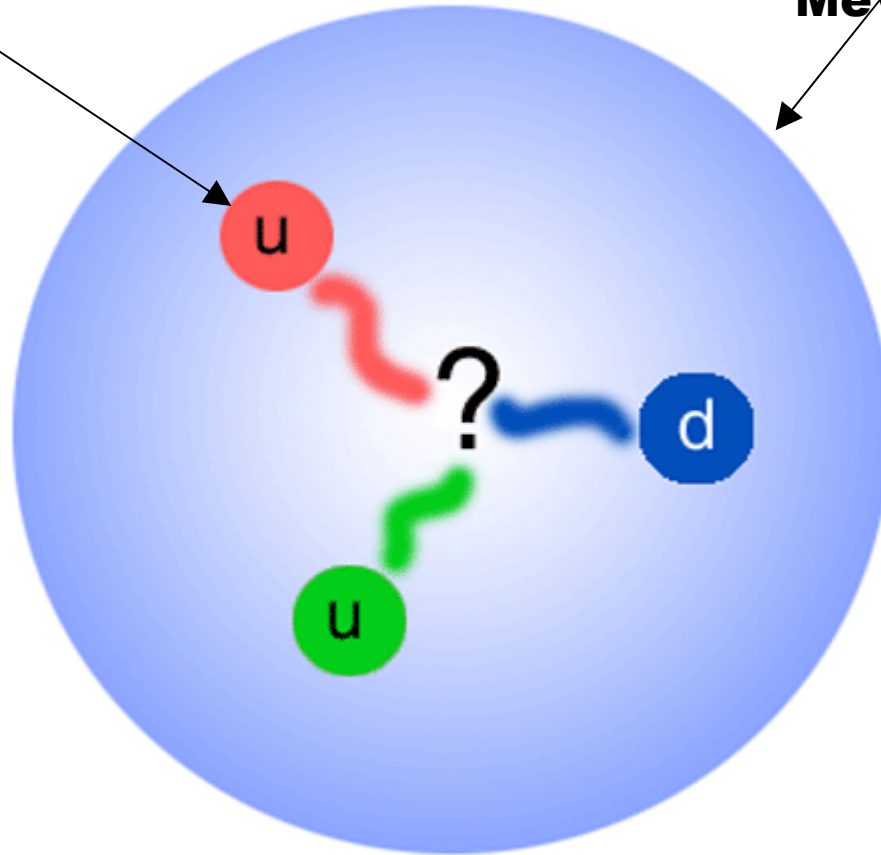
$m_p \approx m_n$



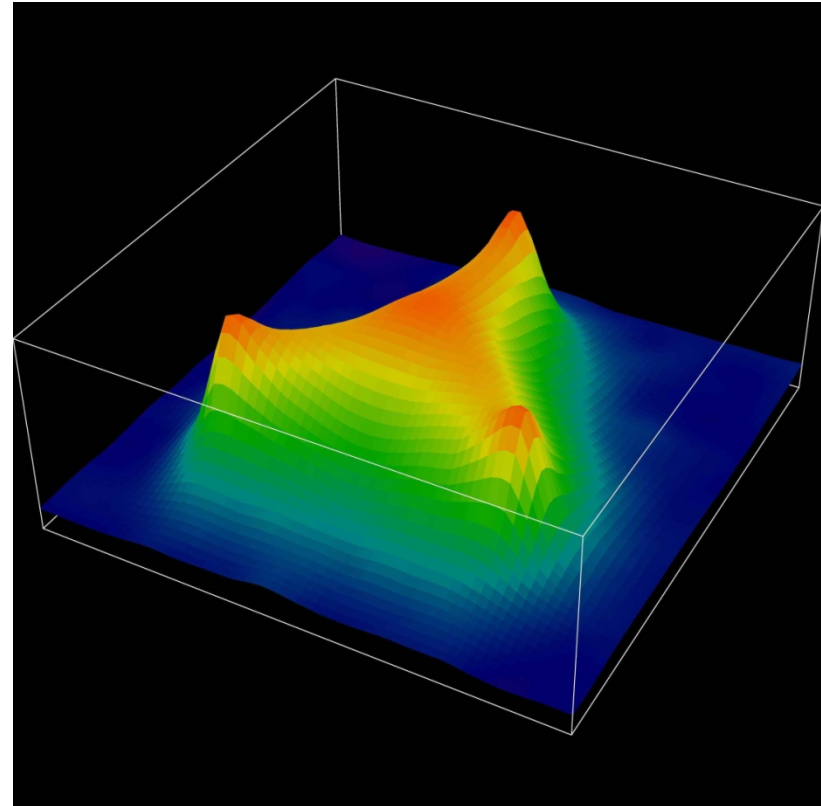
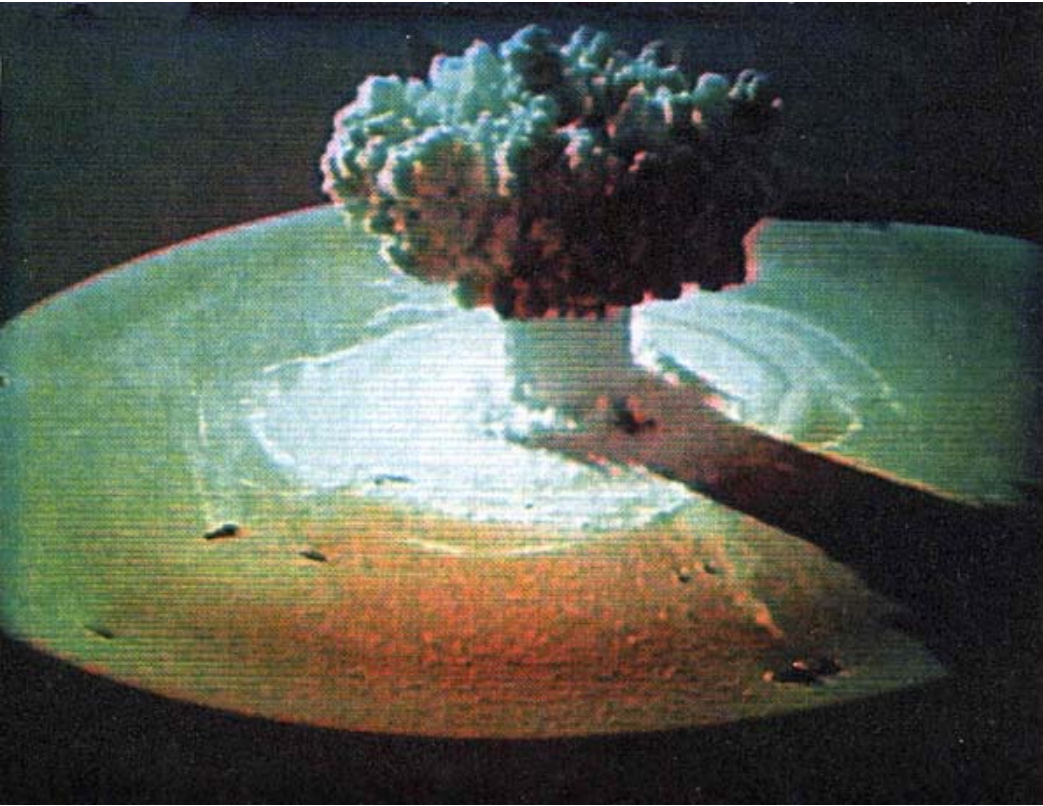
$\longleftrightarrow 10^{-15} \text{ M} \longrightarrow$

$m_{u,d} \approx 3..5$
MeV

$m_p \approx 1000$
MeV



Masses of material objects is due to gluon fields inside baryon



$$E = m_0 c^2$$

$$3m_q / m_{\text{baryon}} \approx 1/100$$

$$m_0 = \frac{E}{c^2}$$

Three body forces!

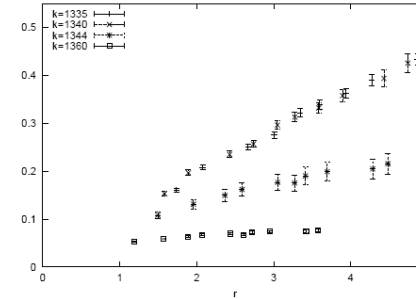
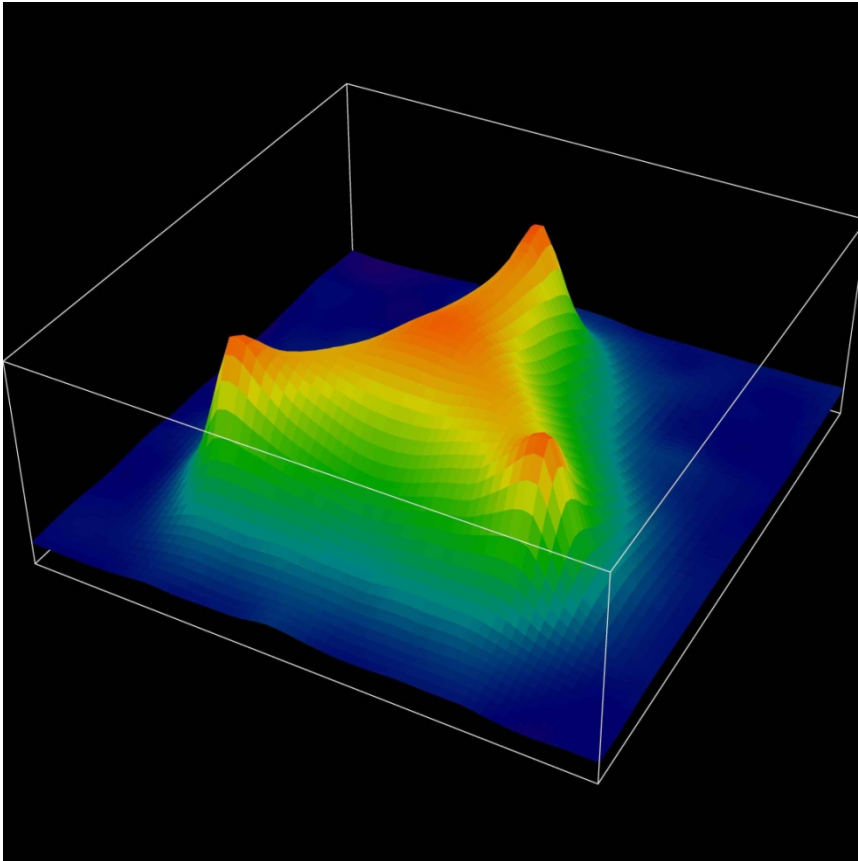


Figure 9: The monopole part of the baryon potential at finite temperature in full QCD as a function of L_Y ($T < T_c$) and L_Δ ($T > T_c$), respectively, in units of *God knows what*.

In Fig. 9 we show the baryon potential on the $16^3 8$ lattice at $\beta = 5.2$ for several values of κ . At this β value

$$T \propto \exp(-2.81/\kappa). \quad (4.1)$$

Increasing κ thus increases the temperature. We cross the finite temperature phase transition at $\kappa = 0.1344$ [14]. We see that the potential flattens off while we approach the transition point. However, the distances we were able to probe are not large enough to make any statement about string breaking.

To compute the action density ρ_A^{3Q} and the electric field and monopole correlators E_i^{3Q} and k^{3Q} , respectively, we need to reduce the statistical noise. Note that the Polyakov loops span an area of $\approx 16 \times 8$ lattice spacings. We do that by using extended operators

$$\begin{aligned} \rho_A^{3Q}(s) \longrightarrow & \frac{1}{8} \{ \rho_A^{3Q}(s) + \rho_A^{3Q}(s - \hat{x} - \hat{y} - \hat{z}) + \rho_A^{3Q}(s - \hat{x} - \hat{y}) \\ & + \rho_A^{3Q}(s - \hat{x} - \hat{z}) + \rho_A^{3Q}(s - \hat{y} - \hat{z}) + \rho_A^{3Q}(s - \hat{x}) \\ & + \rho_A^{3Q}(s - \hat{y}) + \rho_A^{3Q}(s - \hat{z}) \}, \end{aligned} \quad (4.2)$$

$$\begin{aligned} E_i^{3Q}(s) \longrightarrow & \frac{1}{4} \{ E_i^{3Q}(s) + E_i^{3Q}(s - \hat{x} - \hat{t}) \\ & + E_i^{3Q}(s - \hat{x}) + E_i^{3Q}(s - \hat{t}) \}, \end{aligned} \quad (4.3)$$

$$k^{3Q}(*s, \mu) \longrightarrow \frac{1}{2} \{ k^{3Q}(*s, \mu) + k^{3Q}(*s - \hat{z}, \mu) \}, \quad (4.4)$$

where (again) we have assumed that the quarks lie in the (x, y) plane, and we call the direction of the Polyakov lines the t direction.

Usually the teams are rather big, 5 - 10 -15 people

arXiv:hep-lat/0401026v1

arXiv:hep-lat/0401026v2

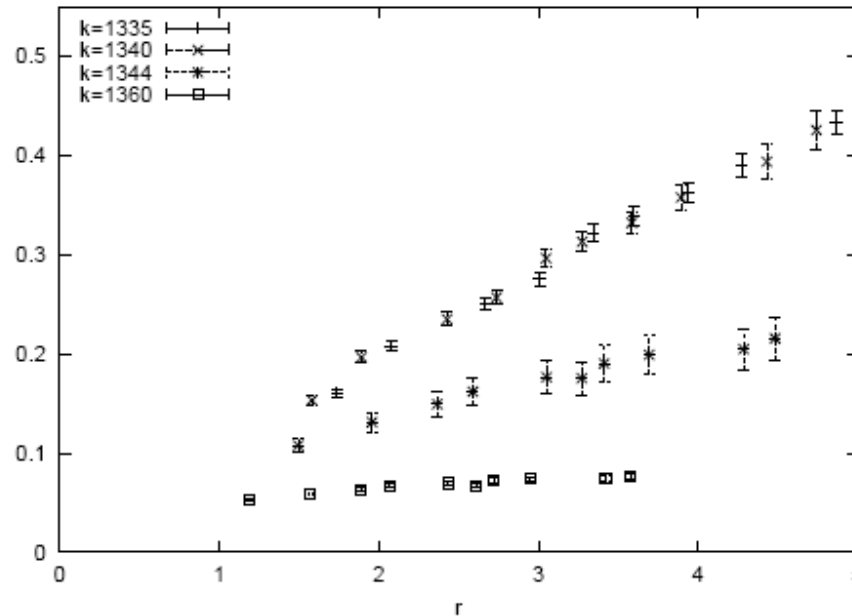
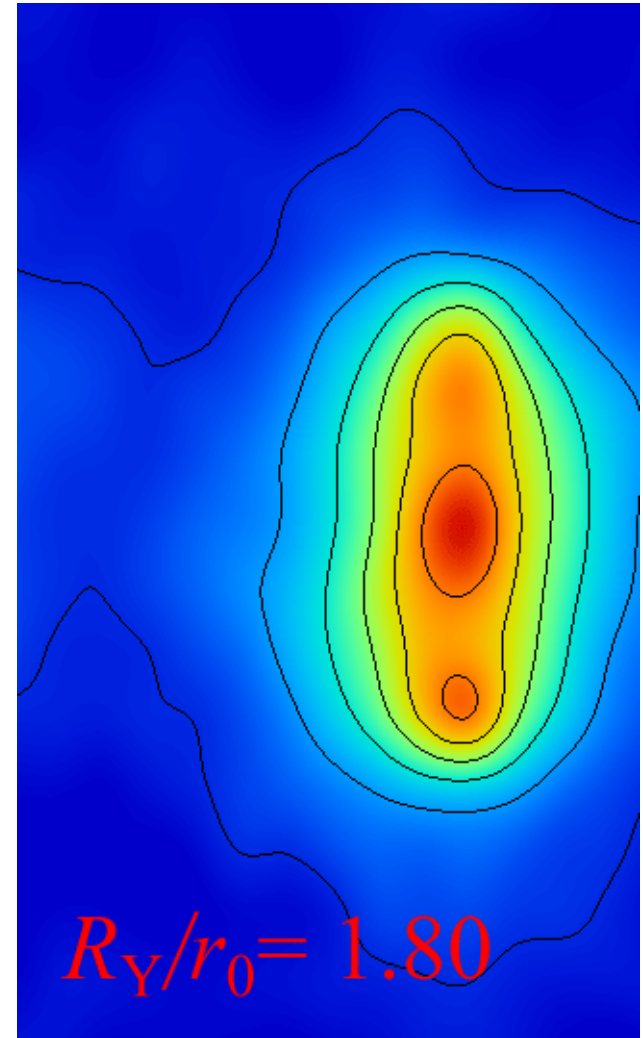
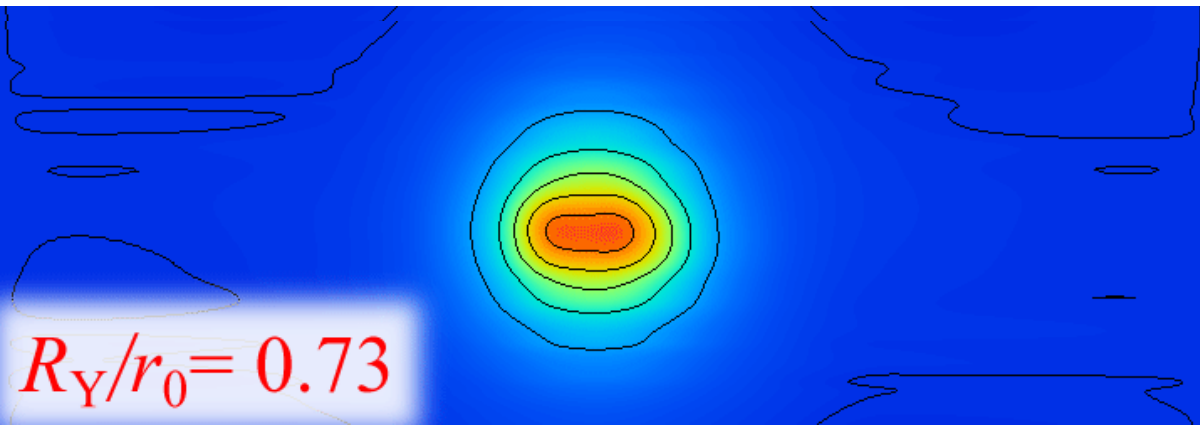


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SU(2) glue SU(3) glue 2qQCD (2+1)QCD

String Breaking (DIK collaboration)



SU(2) glue SU(3) glue 2qQCD (2+1)QCD

Hadron Mass Spectrum

Meson Summary Table

Baryon Summary Table

See also the table of suggested $q\bar{q}$ quark-model assignments in the Quark Model section.

- Indicates particles that appear in the preceding Meson Summary Table. We do not regard the other entries as being established.
- † Indicates that the value of J given is preferred, but needs confirmation.

This short table gives the name, the quantum numbers (where known), and the status of baryons in the Review. Only the baryons with 3- or 4-star status are included in the main Baryon Summary Table. Due to insufficient data or uncertain interpretation, the other entries in the short table are not established as baryons. The names with masses are of baryons that decay strongly. For N , Δ , and Ξ resonances, the partial wave is indicated by the symbol $L_{2I,2J}$, where L is the orbital angular momentum (S, P, D, \dots), I is the isospin, and J is the total angular momentum. For Λ and Σ resonances, the symbol is $L_{I,2J}$.

LIGHT UNFLAVORED ($S = C \neq B = 0$)		STRANGE ($S = \pm 1, C = B = 0$)		BOTTOM ($B = \pm 1$)	
$J^P(J^{PC})$	$J^P(J^{PC})$	$J^P(J^{PC})$	$J^P(J^{PC})$	$J^P(J^{PC})$	$J^P(J^{PC})$
• π^\pm • π^0 • η • $\eta(600)$ • $\rho(770)$ • $\omega(782)$ • $\eta'(958)$ • $\rho(980)$ • $a_0(980)$ • $\phi(1020)$ • $h_1(1170)$ • $b_1(1235)$ • $a_1(1260)$ • $f_2(1270)$ • $f_1(1285)$ • $\eta(1295)$ • $\pi(1300)$ • $a_2(1320)$ • $f_0(1370)$ • $h_1(1380)$ • $\pi_1(1400)$ • $\eta(1405)$ • $f_1(1420)$ • $\omega(1420)$ • $f_2(1430)$ • $a_0(1450)$ • $\rho(1450)$ • $\eta(1475)$ • $f_0(1500)$ • $f_1(1510)$ • $f_2'(1525)$ • $f_2(1565)$ • $h_1(1595)$ • $\pi_1(1600)$ • $a_1(1640)$ • $\eta_2(1645)$ • $\omega(1650)$ • $\omega_3(1670)$	• $\pi_2(1670)$ • $\phi(1680)$ • $\rho_3(1690)$ • $\rho(1700)$ • $a_2(1700)$ • $f_0(1710)$ • $\eta(1760)$ • $\pi(1800)$ • $f_2(1810)$ • $X(1835)$ • $\phi_3(1850)$ • $\eta_2(1870)$ • $\rho(1900)$ • $f_2(1910)$ • $f_2(1950)$ • $\rho_3(1990)$ • $f_2(2010)$ • $f_0(2020)$ • $a_4(2040)$ • $h_4(2050)$ • $\pi_2(2100)$ • $f_0(2100)$ • $f_2(2150)$ • $\rho(2150)$ • $f_0(2200)$ • $f_1(2220)$ • $\eta(2225)$ • $\rho_3(2250)$ • $f_2(2300)$ • $f_4(2300)$ • $f_2(2340)$ • $\rho_3(2350)$ • $a_6(2450)$ • $f_6(2510)$	• K^\pm • K^0 • K_S^0 • K_L^0 • $K_S^*(800)$ • $K^*(892)$ • $K_1(1270)$ • $K_1(1400)$ • $K^*(1410)$ • $K_S^*(1430)$ • $K_2^*(1430)$ • $K_1(1460)$ • $K_2(1580)$ • $K(1630)$ • $K_1(1650)$ • $K^*(1680)$ • $K_2(1770)$ • $K_3^*(1780)$ • $K_2(1820)$ • $K(1830)$ • $K_S^*(1950)$ • $K_2^*(1980)$ • $K_2^*(2045)$ • $K_2(2250)$ • $K_3(2320)$ • $K_2^*(2380)$ • $K_4(2500)$ • $K(3100)$	• B^\pm • B^0 • B^\pm/B^0 ADMIXTURE • $B^\pm/B^0/B_S^0/b$ -baryon ADMIXTURE V_{cb} and V_{ub} CKM Matrix Elements • B^* $B_J^*(5732)$	BOTTOM, STRANGE ($B = \pm 1, S = \pm 1$) • B_s^0 • B_s^\pm $B_{J,s}^*(5850)$	BOTTOM, CHARMED ($B = C = \pm 1$) • B_c^\pm
OTHER LIGHT		CHARMED ($C = \pm 1$)		$c\bar{c}$	
Further States		CHARMED, STRANGE ($C = S = \pm 1$)		$b\bar{b}$	
		NON- $q\bar{q}$ CANDIDATES			

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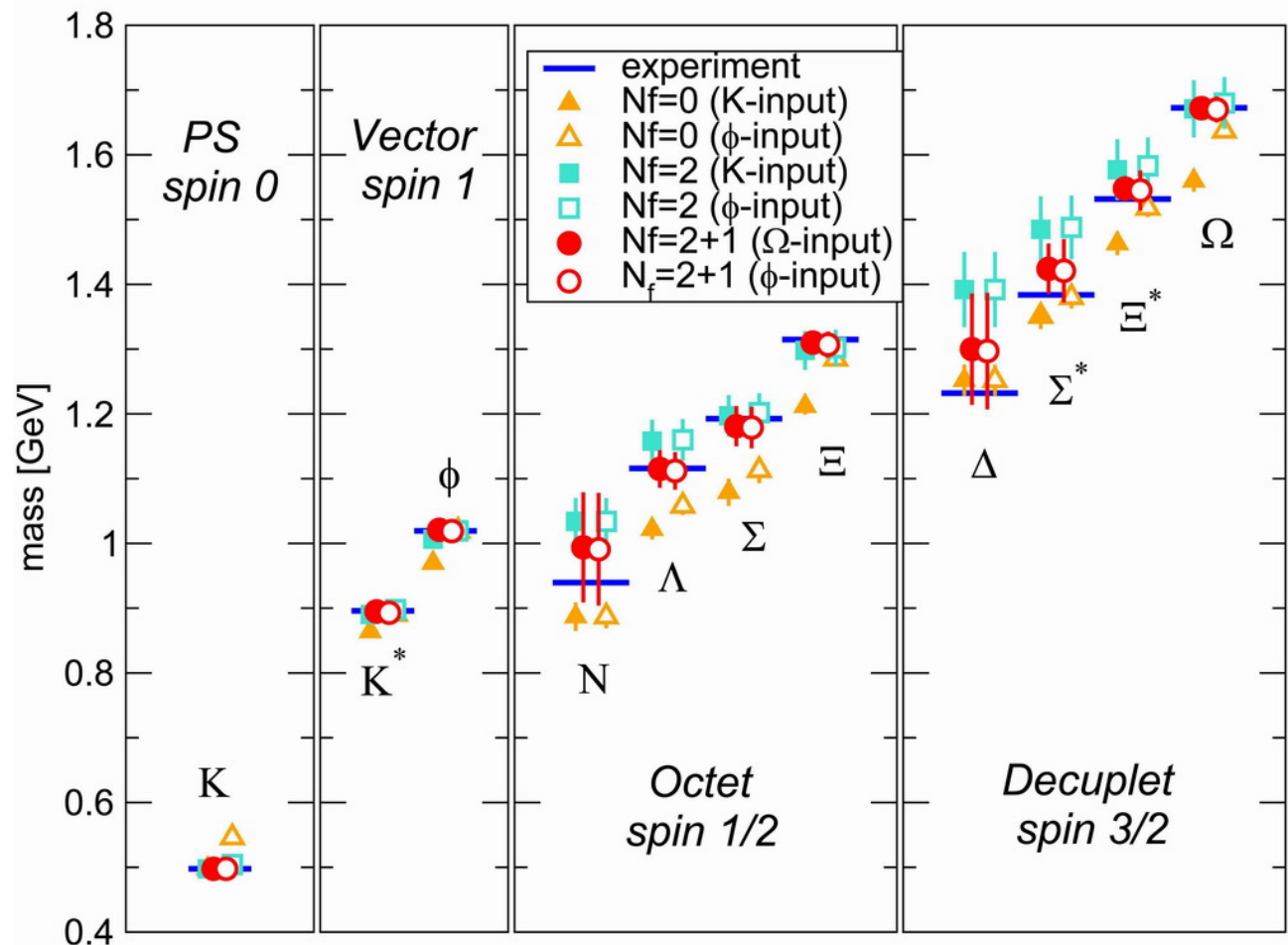
P	P_{11}	****	$\Delta(1232)$	P_{33}	****	Λ	P_{01}	****	Σ^+	P_{11}	****	Ξ^0	P_{11}	****
n	P_{11}	****	$\Delta(1600)$	P_{33}	***	$\Lambda(1405)$	S_{01}	****	Σ^0	P_{11}	****	Ξ^-	P_{11}	****
$N(1440)$	P_{11}	****	$\Delta(1620)$	S_{31}	****	$\Lambda(1520)$	D_{03}	****	Σ^-	P_{11}	****	$\Xi(1530)$	P_{13}	****
$N(1520)$	D_{13}	****	$\Delta(1700)$	D_{33}	****	$\Lambda(1600)$	P_{01}	***	$\Sigma(1385)$	P_{13}	****	$\Xi(1620)$		*
$N(1535)$	S_{11}	****	$\Delta(1750)$	P_{31}	*	$\Lambda(1670)$	S_{01}	****	$\Sigma(1480)$		*	$\Xi(1690)$		***
$N(1650)$	S_{11}	****	$\Delta(1900)$	S_{31}	**	$\Lambda(1690)$	D_{03}	****	$\Sigma(1560)$		**	$\Xi(1820)$	D_{13}	***
$N(1675)$	D_{15}	****	$\Delta(1905)$	F_{35}	****	$\Lambda(1800)$	S_{01}	***	$\Sigma(1580)$	D_{13}	*	$\Xi(1950)$		***
$N(1680)$	F_{15}	****	$\Delta(1910)$	P_{31}	****	$\Lambda(1810)$	P_{01}	***	$\Sigma(1620)$	S_{11}	**	$\Xi(2030)$		***
$N(1700)$	D_{13}	***	$\Delta(1920)$	P_{33}	***	$\Lambda(1820)$	F_{05}	****	$\Sigma(1660)$	P_{11}	***	$\Xi(2120)$		*
$N(1710)$	P_{11}	***	$\Delta(1930)$	D_{35}	***	$\Lambda(1830)$	D_{05}	****	$\Sigma(1670)$	D_{13}	****	$\Xi(2250)$		**
$N(1720)$	P_{13}	****	$\Delta(1940)$	D_{33}	*	$\Lambda(1890)$	P_{03}	****	$\Sigma(1690)$		**	$\Xi(2370)$		**
$N(1900)$	P_{13}	**	$\Delta(1950)$	F_{37}	****	$\Lambda(2000)$	*		$\Sigma(1750)$	S_{11}	***	$\Xi(2500)$		*
$N(1990)$	F_{17}	**	$\Delta(2000)$	F_{35}	**	$\Lambda(2020)$	F_{07}	*	$\Sigma(1770)$	P_{11}	*			*
$N(2000)$	F_{15}	**	$\Delta(2150)$	S_{31}	**	$\Lambda(2100)$	G_{07}	****	$\Sigma(1775)$	D_{15}	****	Ω^-		****
$N(2080)$	D_{13}	**	$\Delta(2200)$	G_{37}	*	$\Lambda(2110)$	F_{05}	***	$\Sigma(1840)$	P_{13}	*	$\Omega(2250)^-$		***
$N(2090)$	S_{11}	*	$\Delta(2300)$	H_{39}	**	$\Lambda(2325)$	D_{03}	*	$\Sigma(1880)$	P_{11}	**	$\Omega(2380)^-$		**
$N(2100)$	P_{11}	*	$\Delta(2350)$	D_{35}	**	$\Lambda(2350)$	H_{09}	***	$\Sigma(1915)$	F_{15}	****	$\Omega(2470)^-$		**
$N(2190)$	G_{17}	****	$\Delta(2390)$	F_{37}	*	$\Lambda(2585)$	**	**	$\Sigma(1940)$	D_{13}	***			*
$N(2200)$	D_{15}	***	$\Delta(2400)$	G_{39}	**				$\Sigma(2000)$	S_{11}	*	Λ_c^+		****
$N(2220)$	H_{19}	****	$\Delta(2420)$	$H_{3,11}$	****				$\Sigma(2030)$	F_{17}	****	$\Lambda_c(2593)^+$		***
$N(2250)$	G_{19}	****	$\Delta(2750)$	$k_{3,13}$	***				$\Sigma(2070)$	F_{15}	*	$\Lambda_c(2625)^+$		***
$N(2600)$	$h_{1,11}$	***	$\Delta(2950)$	$k_{3,15}$	**				$\Sigma(2080)$	P_{13}	**	$\Lambda_c(2765)^+$		*
$N(2700)$	$K_{1,13}$	**							$\Sigma(2100)$	G_{17}	*	$\Lambda_c(2880)^+$		**
			$\Theta(1540)^+$	*					$\Sigma(2250)$		***	$\Sigma_c(2455)$		****
									$\Sigma(2455)$		**	$\Sigma_c(2520)$		***
									$\Sigma(2620)$		**	$\Sigma_c(2800)$		***
									$\Sigma(3000)$		*	Ξ_c^+		***
									$\Sigma(3170)$		*	Ξ_c^0		***
												Ξ_c^+		***
												Ξ_c^0		***
												Ξ_c^+		***
												Ξ_c^0		***
												Ξ_c^+		***
												Ξ_c^0		***
												Ξ_c^+		***
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												Ξ_c^+		***
												Ξ_c^0		***
												Ξ_c^+		***

SU(2) glue SU(3) glue 2qQCD (2+1)QCD

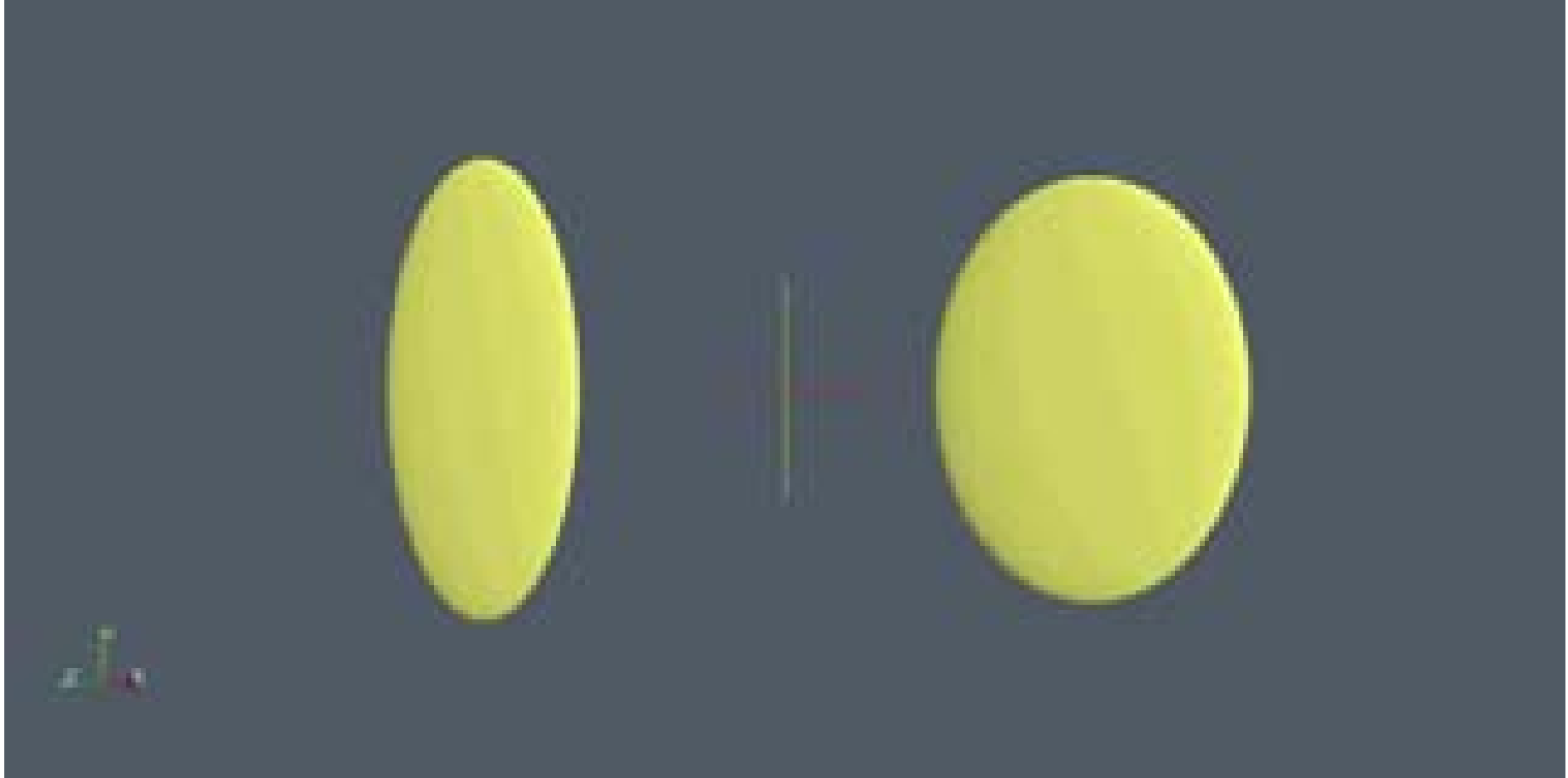
Wilson non-perturbatively improved Fermions
“WORKING HORSE” of lattice QCD calculations

Y. Kuramashi Lattice 2007

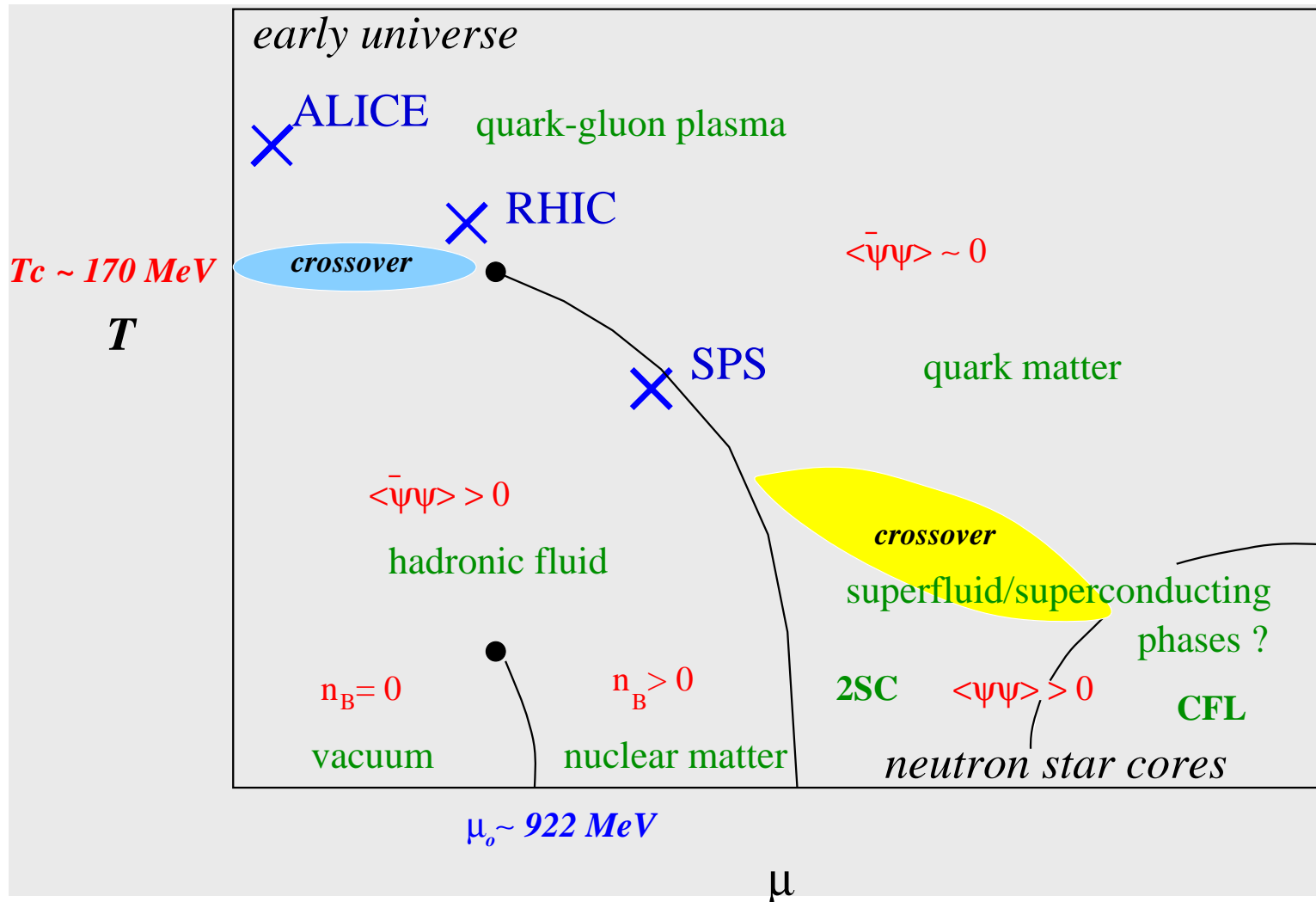
Iwasaki gauge action +
clover quarks
 $a^{-1} = 2.2\text{GeV}$,
lattice size: $32^3 \times 64$



Heavy ions Collisions and Quark- Gluon Plasma



Phase diagram of QCD

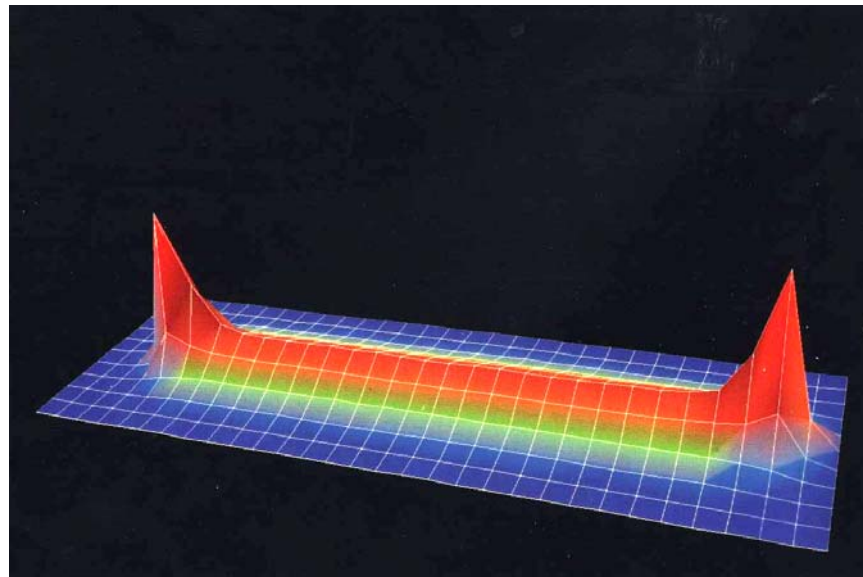


**The closer our calculations to
nature the more complicated
they are**

2 dimensional gluodynamics
(no dynamical quarks)
can be solved analytically

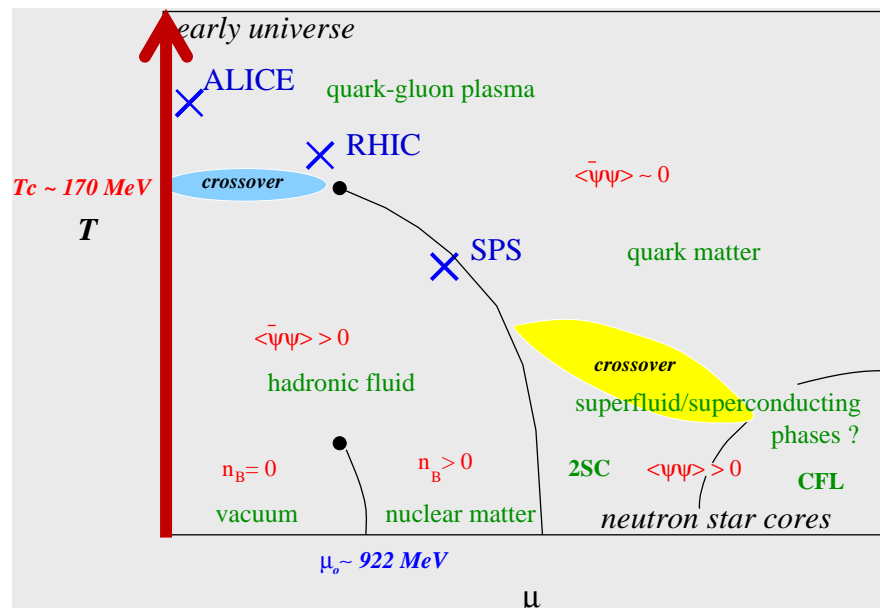
The closer our calculations to nature the more complicated they are

4 dimensional gluodynamics (no dynamical quarks) can be “solved” on laptop



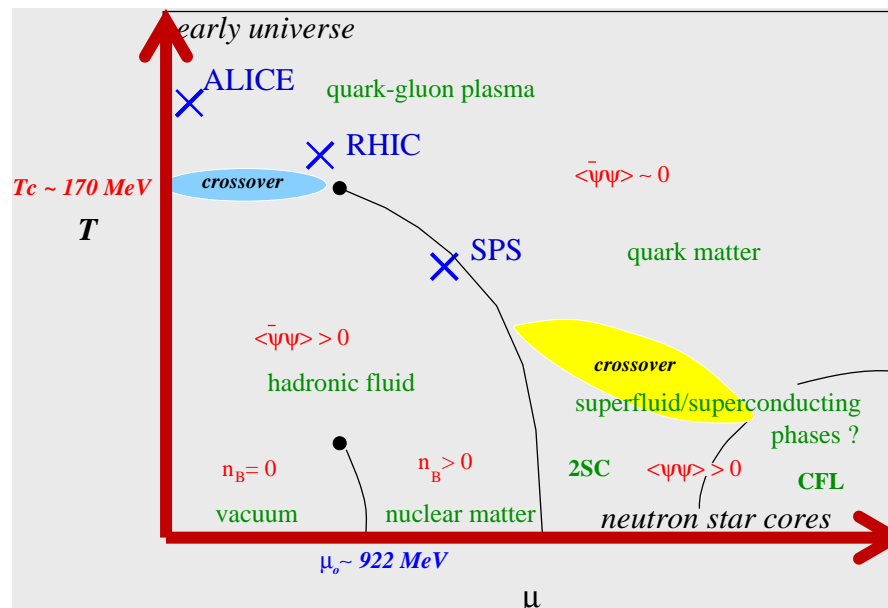
The closer our calculations to nature the more complicated they are

4 dimensional QCD (with dynamical quarks) needs 100-100000 times more CPU time than gluodynamics (we need supercomputers)

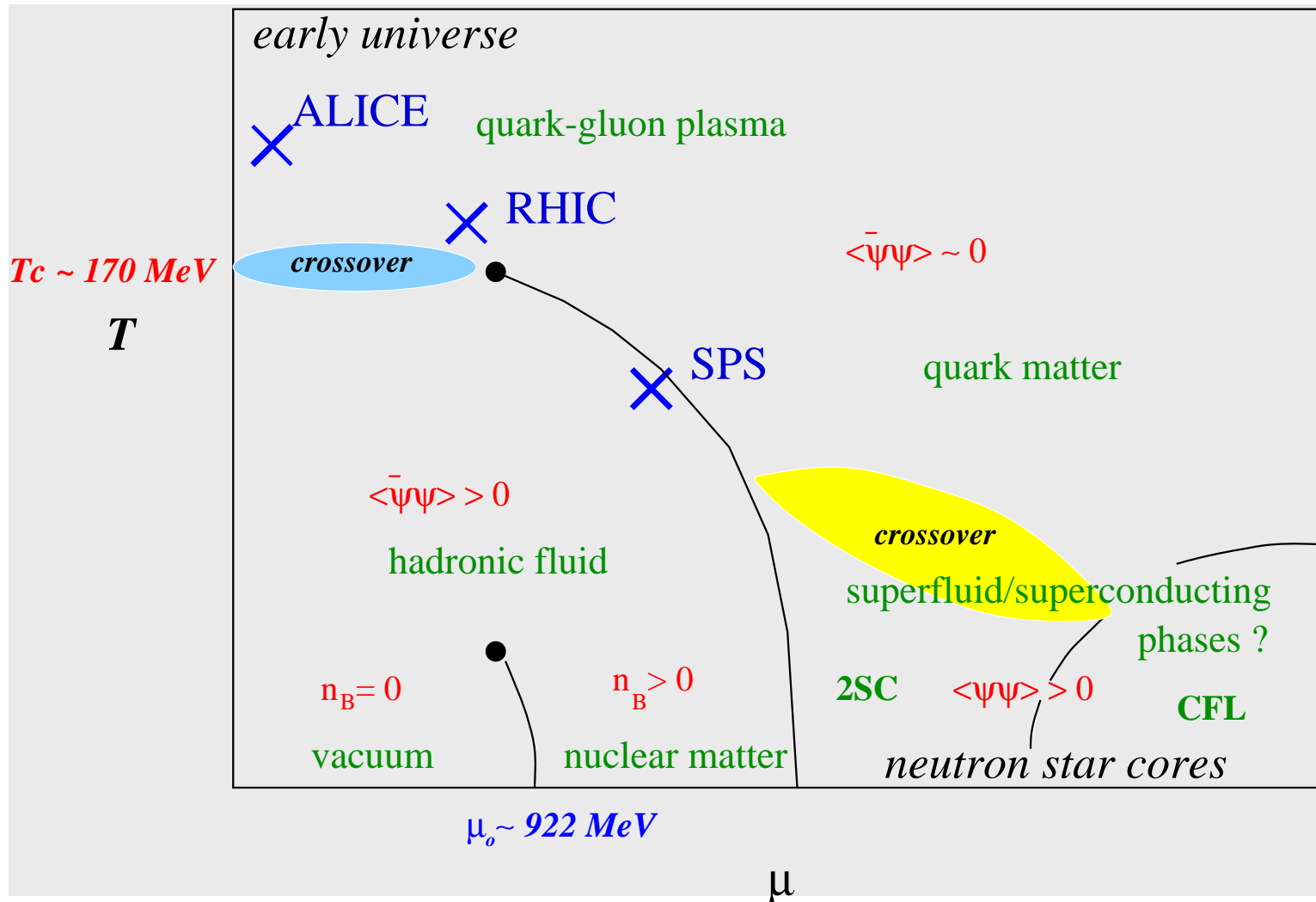


The closer our calculations to nature the more complicated they are

We do not know how to solve 4 dimensional QCD (with dynamical quarks) at finite chemical potential

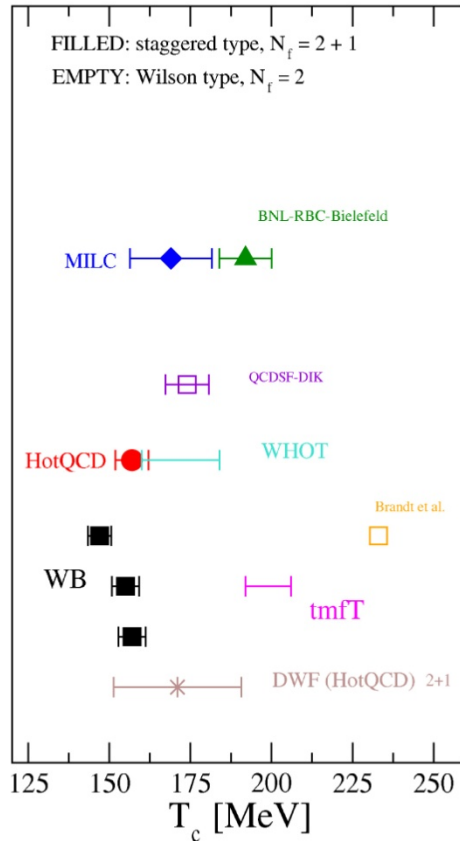


Phase diagram of QCD

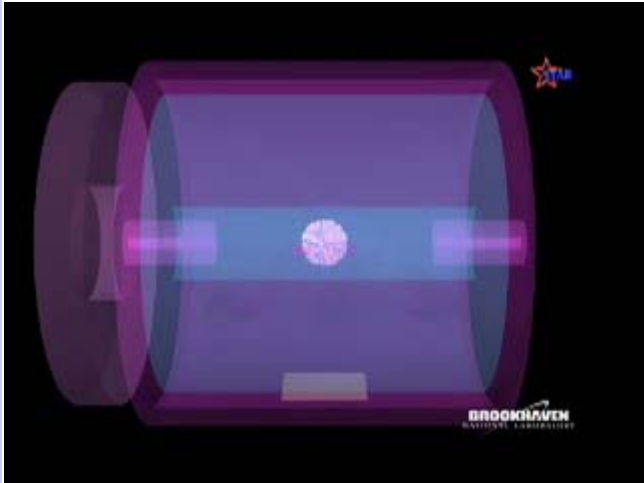
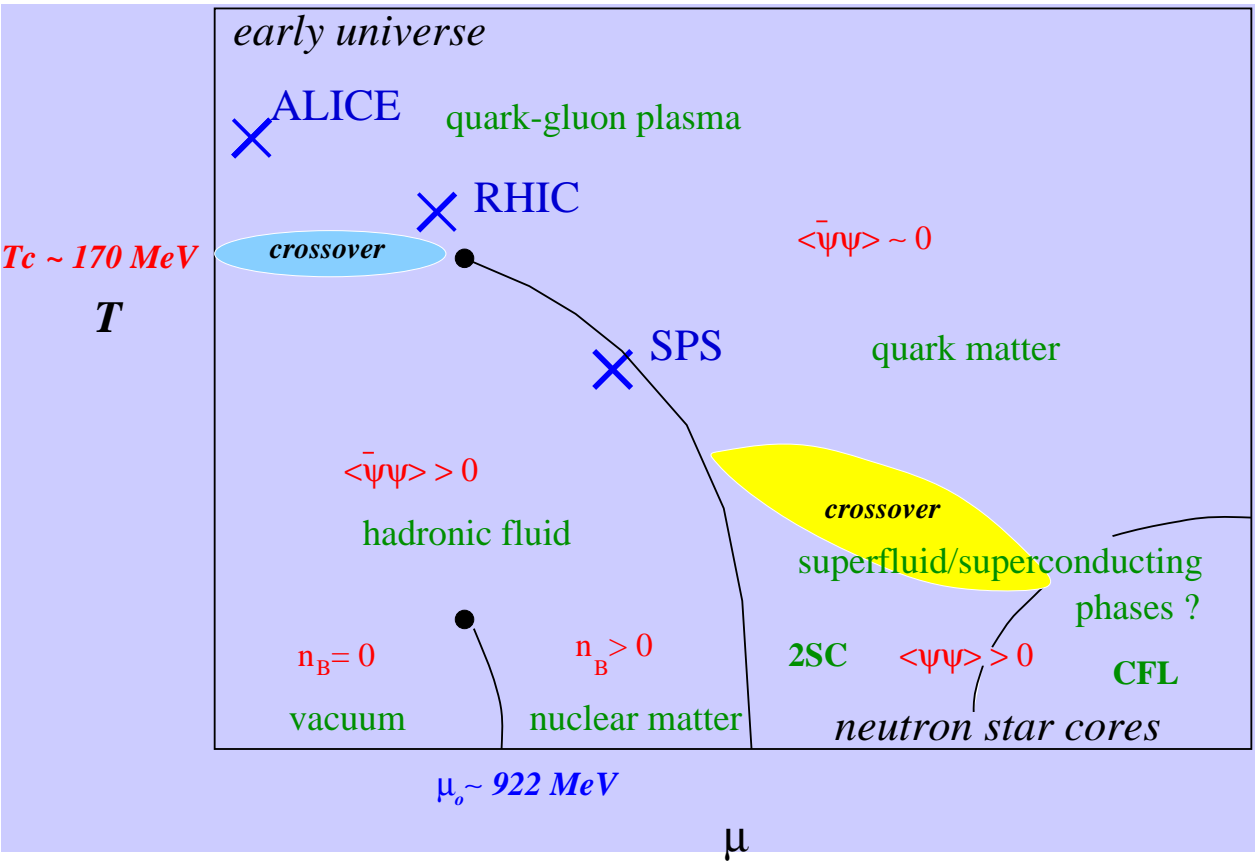


Critical temperature

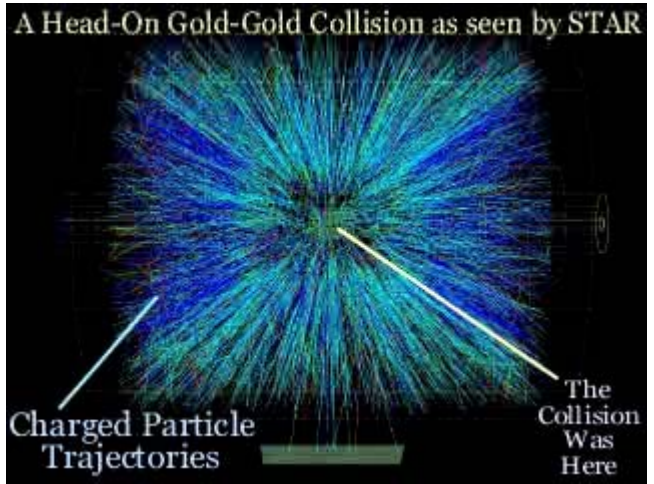
Transition temperature from a variety of studies



- ▶ Staggered types, $N_f = 2 + 1$: p4, asqtad, HISQ, stout — already introduced. Data from only chiral type observables.
- ▶ Wilson types, $N_f = 2$:
 - ▷ QCDSF-DIK [arXiv:0910.2392], clover + plaquette, $N_t = 8 - 14$
 - ▷ WHOT-QCD [arXiv:0909.2121], clover + Iwasaki, $N_t = 4 - 6$
 - ▷ Brandt et al. [arXiv:1011.6172], clover, $N_t = 16$
 - ▷ tmfT (Florian Burger talk), mtmWilson + tree-level Symanzik, $N_t = 8 - 12$
- ▶ DWF (HotQCD), $N_f = 2+1$:+Iwasaki, $N_t = 8, L_s = 32 - 96$



RHIC



AMS 2005, Tampa meeting

created matter at a temperature of about 4 trillion degrees Celsius — the hottest temperature ever reached in a laboratory, about 250,000 times hotter than the center of the Sun

using a giant atom smasher said on they have created a new state of matter - a hot, dense liquid made out of basic atomic particles - and said it shows what the early universe looked like for a very, very brief ime.

"We think we are looking at a phenomenon ... in the universe 13 billion years ago when free quarks and gluons ... cooled down to the particles that we know today," Aronson told a news conference carried by telephone from a meeting of the American Physical Society in Tampa, Fla.

Liquid, not a gas

The quark-gluon plasma was made in the Relativistic Heavy Ion Collider — a powerful atom smasher at Brookhaven National Laboratory in Upton, N.Y. Unexpectedly, the quark-gluon plasma behaved like a perfect liquid of quarks, instead of a gas, the physicists said.

Evidence of 5-th state of matter in heavy ions collisions

1. Thermalisation
2. Elliptic flow
3. Jets quenching
4. Spectrum of photons
5. Share viscosity η/s and hydrodynamic approach
6. Lattice calculations vs experiment

.....

QUARK-GLUON PLASMA THERMALIZATION AND PLASMA INSTABILITIES

PETER ARNOLD

[arXiv:hep-ph/0409002v1](https://arxiv.org/abs/hep-ph/0409002v1)

when they are in *local* thermal equilibrium. Macroscopic currents in one region of the plasma can interact magnetically with other currents in other regions, over tremendous distance scales, creating complicated structures like Fig. 1. Non-Abelian plasmas, however, are somewhat different. From theoretical studies of the equilibrium properties of such plasmas, we know that the non-Abelian interactions cause magnetic *confinement* over distances of order $1/(g^2T)$. It is reasonable to assume that, even dynamically, color magnetic fields cannot exist on distance scales larger than the confinement length. So, unlike traditional electromagnetic plasmas, there are no large-distance magnetic fields. As far as the color degrees of freedom are concerned, the long-distance effective theory of a non-Abelian plasma is hydrodynamics rather than magneto-hydrodynamics.

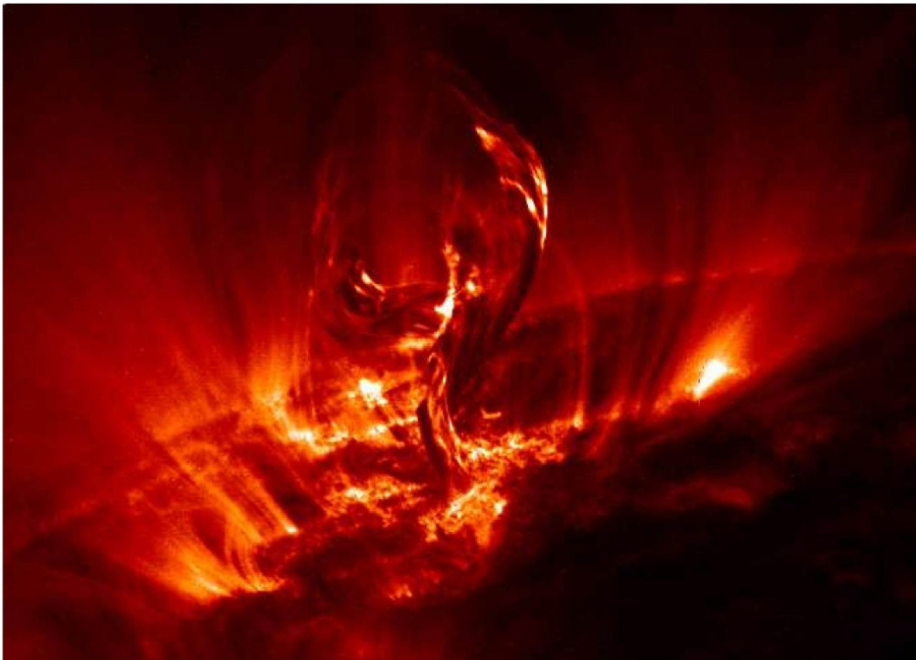
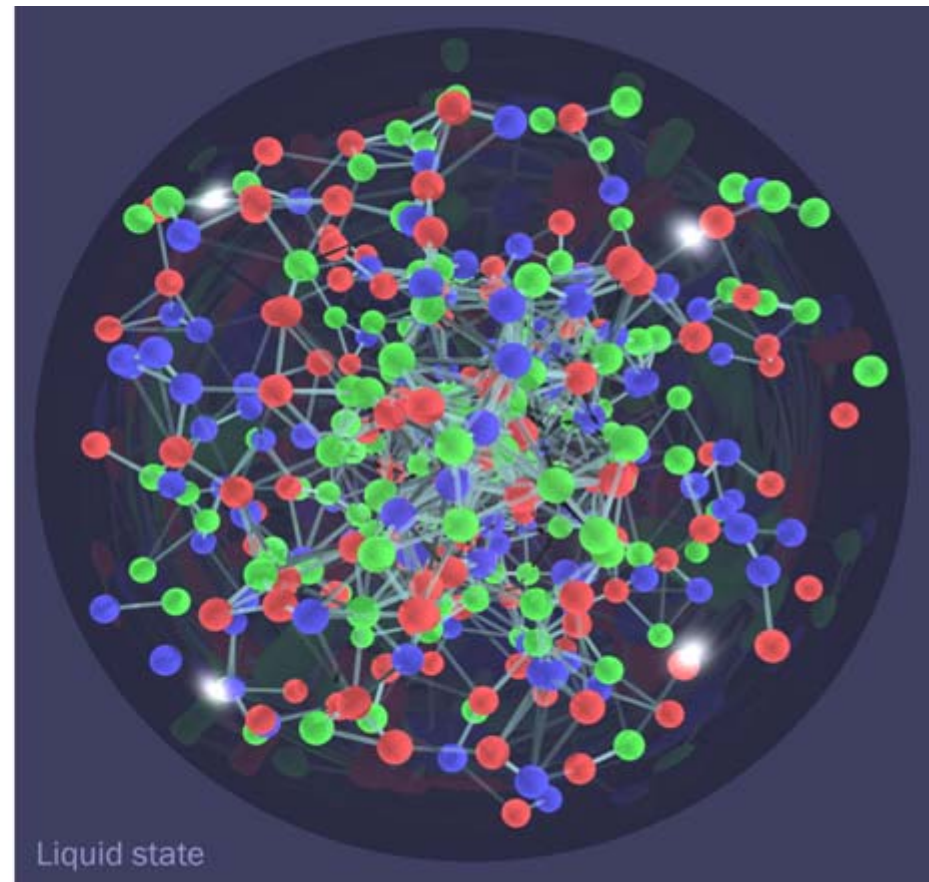
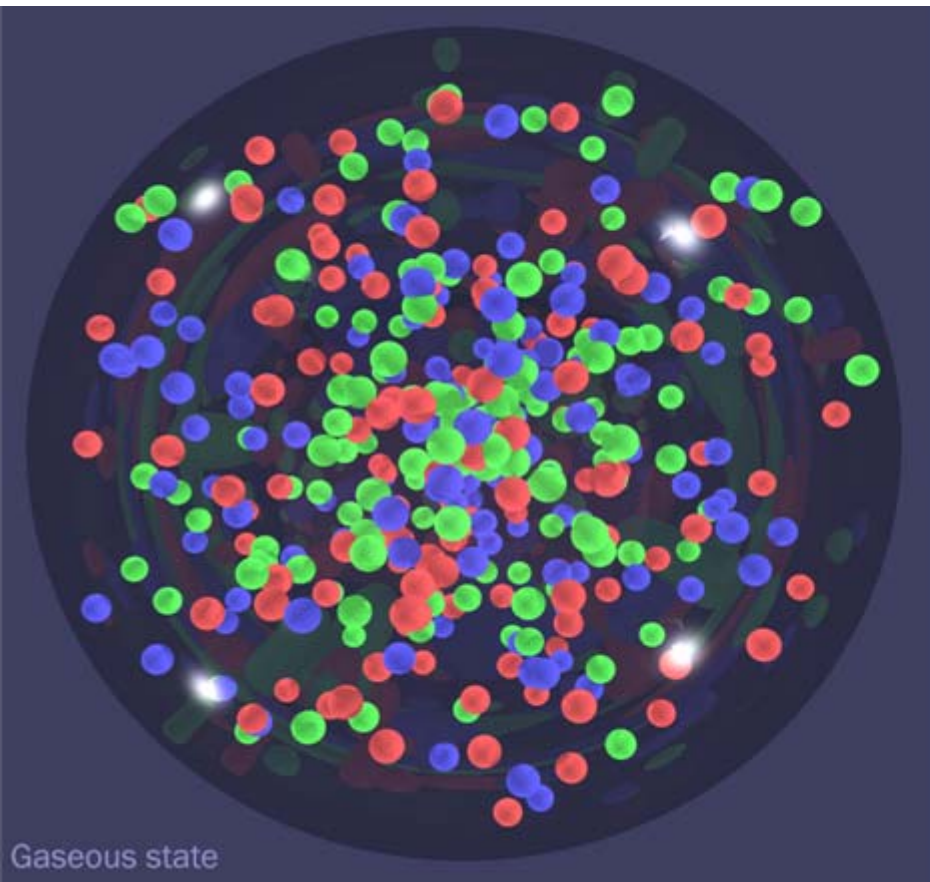


Figure 1. Image of a solar coronal filament from NASA's TRACE satellite, from <http://antwrp.gsfc.nasa.gov/apod/ap000809.html>.

QGP is the thermalized strongly correlated liquid

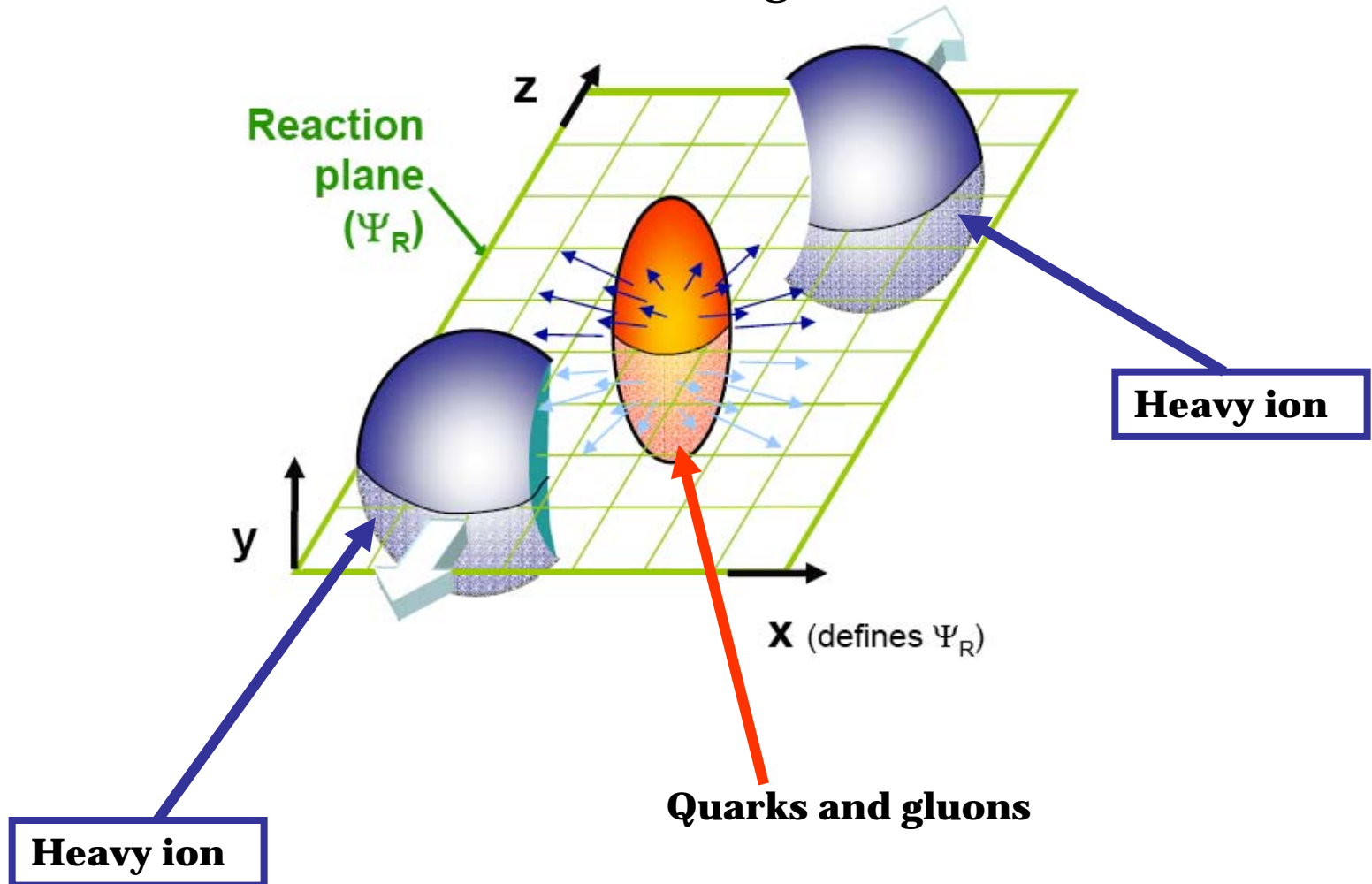


Collision time is very short and how thermalization occurs it is a question

Below I use a lot of slides made
by
M.N. Chernodub,
P.V. Buividovich and
D.E. Kharzeev

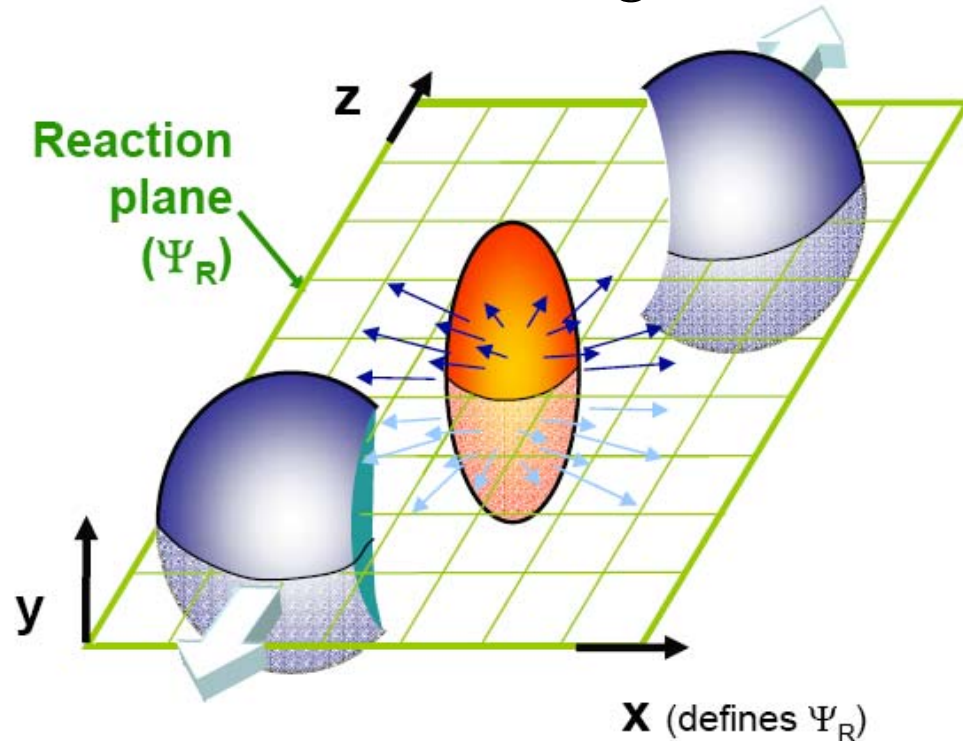
Magnetic fields in non-central collisions

[Fukushima, Kharzeev, Warringa, McLerran '07-'08]



Magnetic fields in non-central collisions

[Fukushima, Kharzeev, Warringa, McLerran '07-'08]



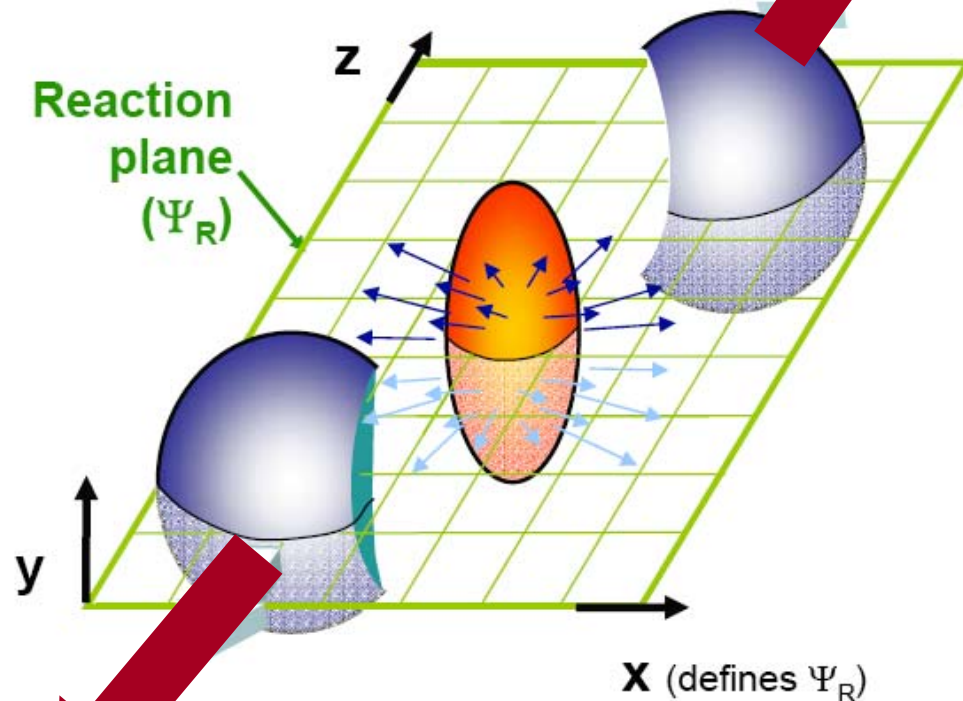
[1] K. Fukushima, D. E. Kharzeev, and H. J. Warringa, *Phys. Rev. D* **78**, 074033 (2008),
URL <http://arxiv.org/abs/0808.3382>.

[2] D. Kharzeev, R. D. Pisarski, and M. H. G. Tytgat, *Phys. Rev. Lett.* **81**, 512 (1998),
URL <http://arxiv.org/abs/hep-ph/9804221>.

[3] D. Kharzeev, *Phys. Lett. B* **633**, 260 (2006), URL <http://arxiv.org/abs/hep-ph/0406125>.

[4] D. E. Kharzeev, L. D. McLerran, and H. J. Warringa, *Nucl. Phys. A* **803**, 227 (2008),
URL <http://arxiv.org/abs/0711.0950>.

Magnetic fields in non-central collisions



Charge is large
Velocity is high

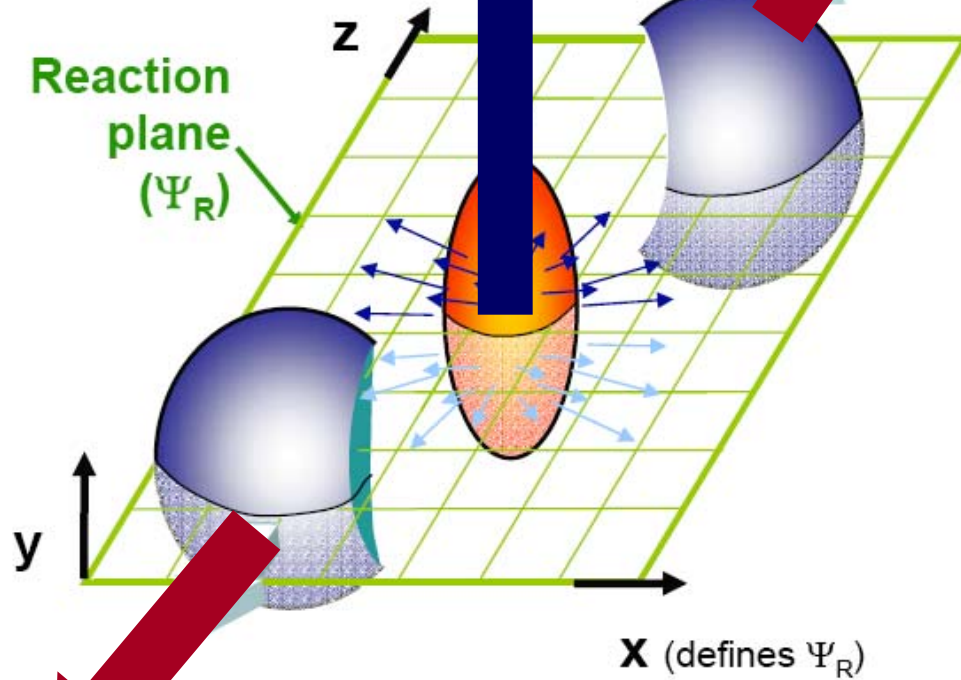
Thus we have
two very big
currents

The medium is filled by electrically charged particles

Large orbital momentum, perpendicular to the reaction plane

Large magnetic field along the direction of the orbital momentum

Magnetic fields in **B** central collisions



Two very big
currents
produce a very

*big magnetic
field*

The medium is filled by electrically charged particles

Large orbital momentum, perpendicular to the reaction plane

Large magnetic field along the direction of the orbital momentum

Comparison of magnetic fields

D.Kharzeev



The Earth's magnetic field

0.6 Gauss

A common, hand-held magnet

100 Gauss



The strongest steady magnetic fields achieved so far in the laboratory

4.5×10^5 Gauss

The strongest man-made fields ever achieved, if only briefly

10^7 Gauss



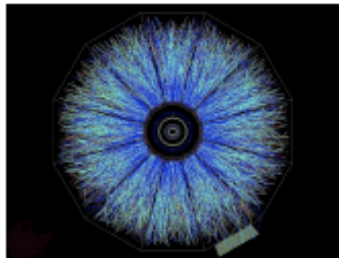
Typical surface, polar magnetic fields of radio pulsars

10^{13} Gauss

Surface field of Magnetars

10^{15} Gauss

<http://solomon.as.utexas.edu/~duncan/magnetar.html>



Off central Gold-Gold Collisions at 100 GeV per nucleon

$$eB(\tau = 0.2 \text{ fm}) = 10^3 \sim 10^4 \text{ MeV}^2 \sim 10^{17} \text{ Gauss}$$

Magnetic forces are of the order of strong interaction forces

first time in my life I see such effect

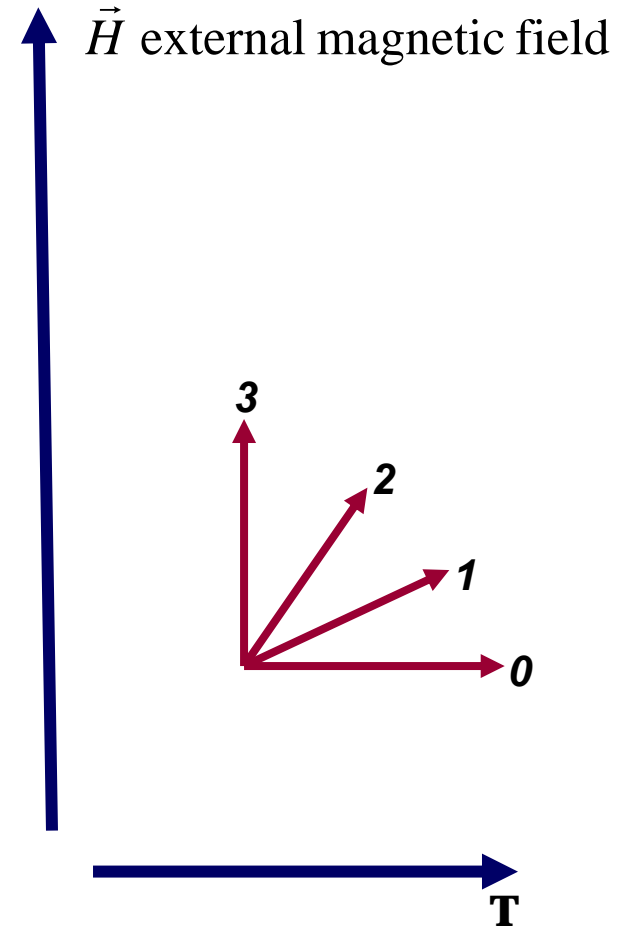
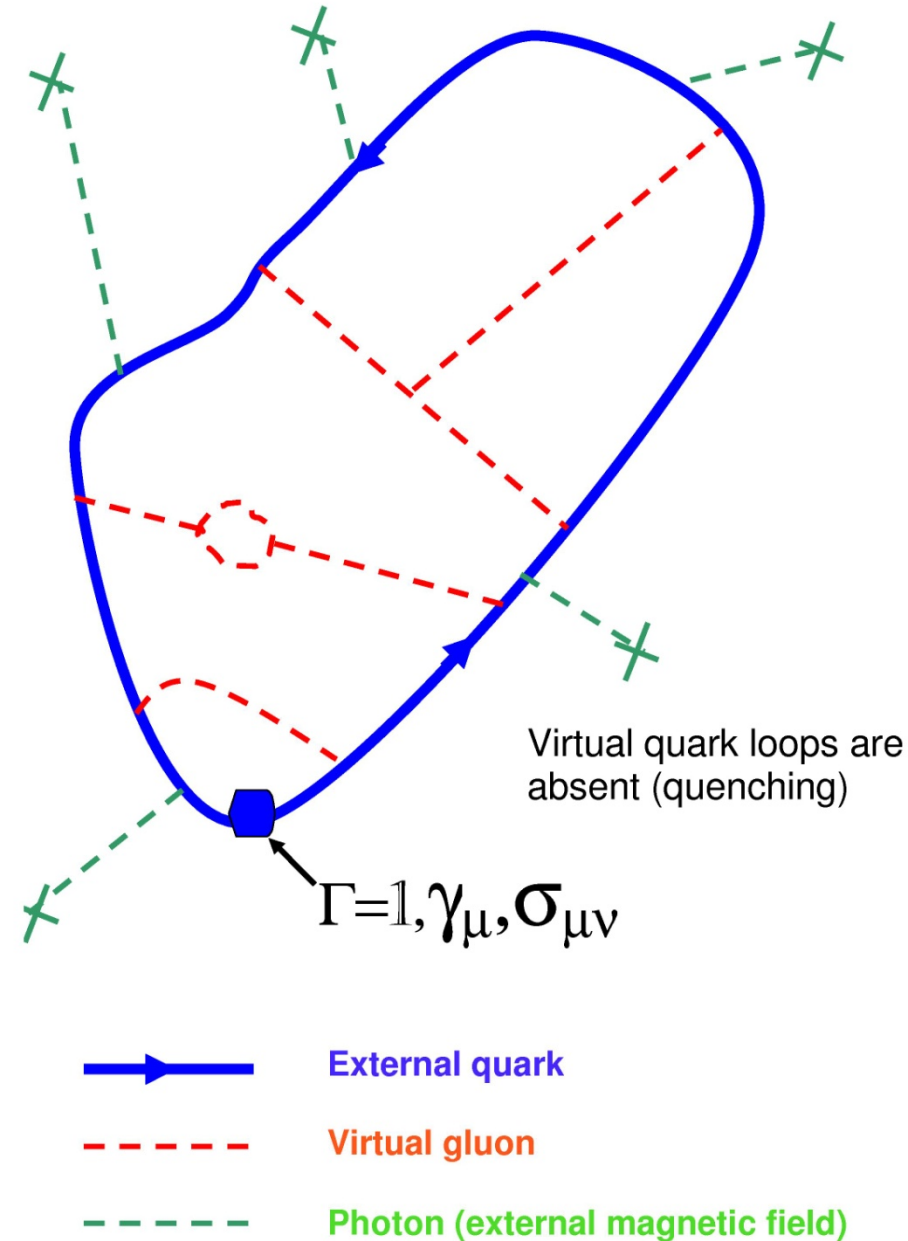
$$eB \approx \Lambda_{QCD}^2$$

We expect the influence of magnetic field on strong interaction physics

The effects are nonperturbative, it is impossible to perform analytic calculations and we use

Lattice Calculations

We calculate $\langle \bar{\psi} \Gamma \psi \rangle$; $\Gamma = 1, \gamma_\mu, \sigma_{\mu\nu}$
 in the external magnetic field and in the presence of the vacuum gluon fields



Chiral Magnetic Effect

[Fukushima, Kharzeev, Warringa, McLerran '07-'08]

Electric current appears at regions

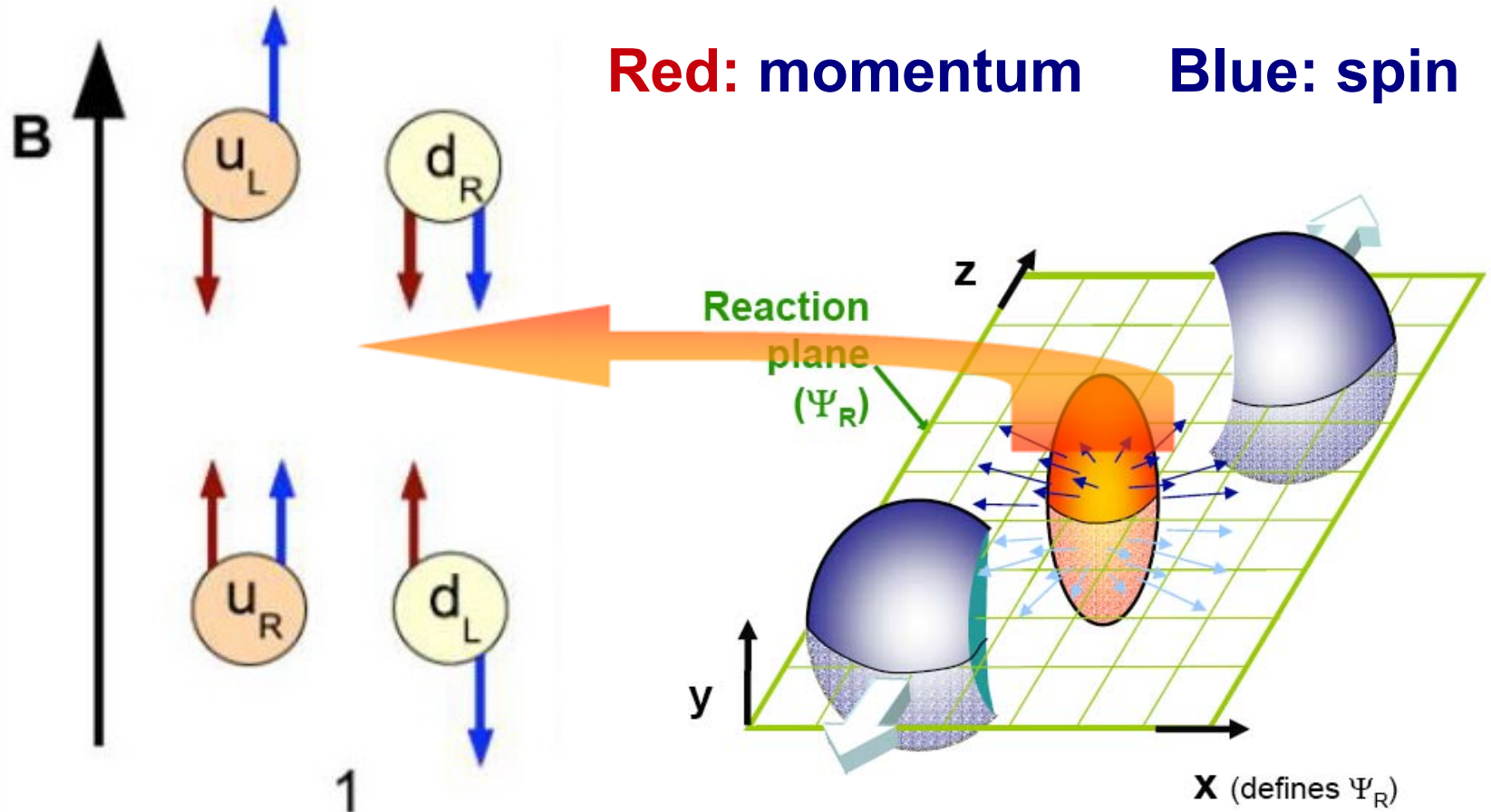
- 1. with non-zero topological charge density**
- 2. exposed to external magnetic field**

Experimentally observed at RHIC :

charge asymmetry of produced particles at heavy ion collisions

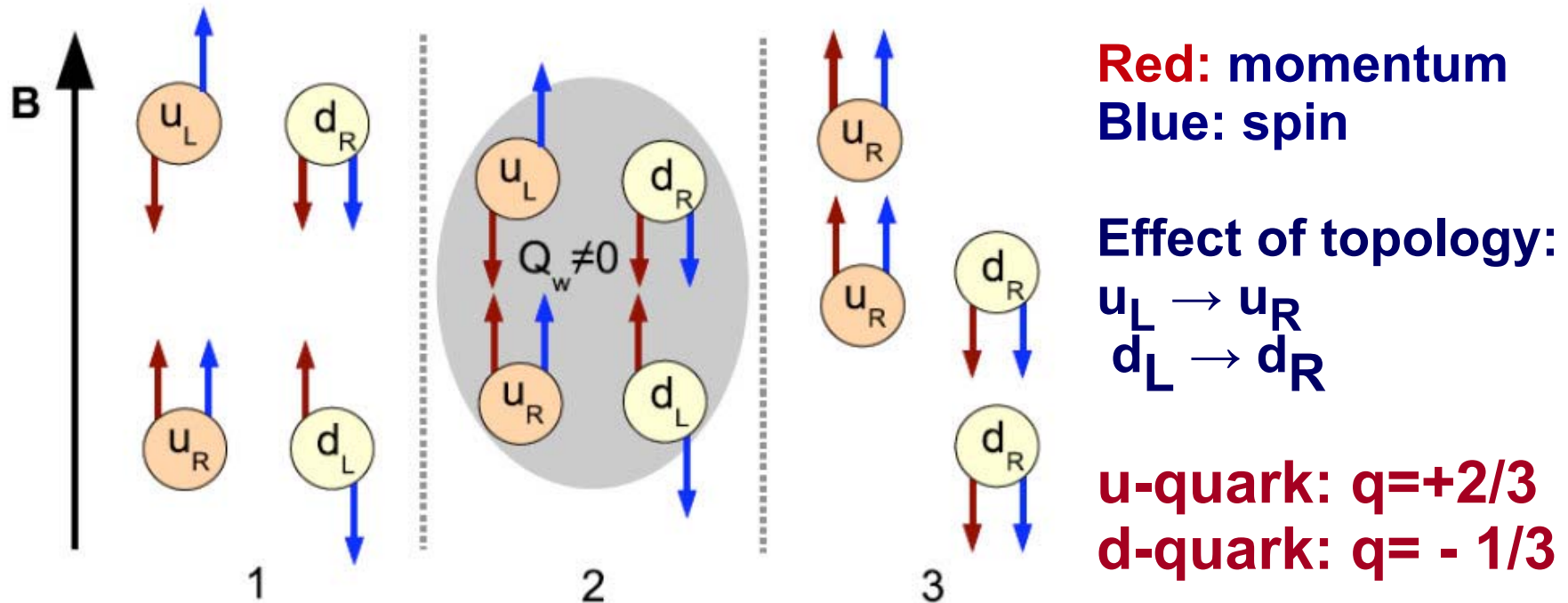
Chiral Magnetic Effect by Fukushima, Kharzeev, Warringa, McLerran

1. Massless quarks in external magnetic field.

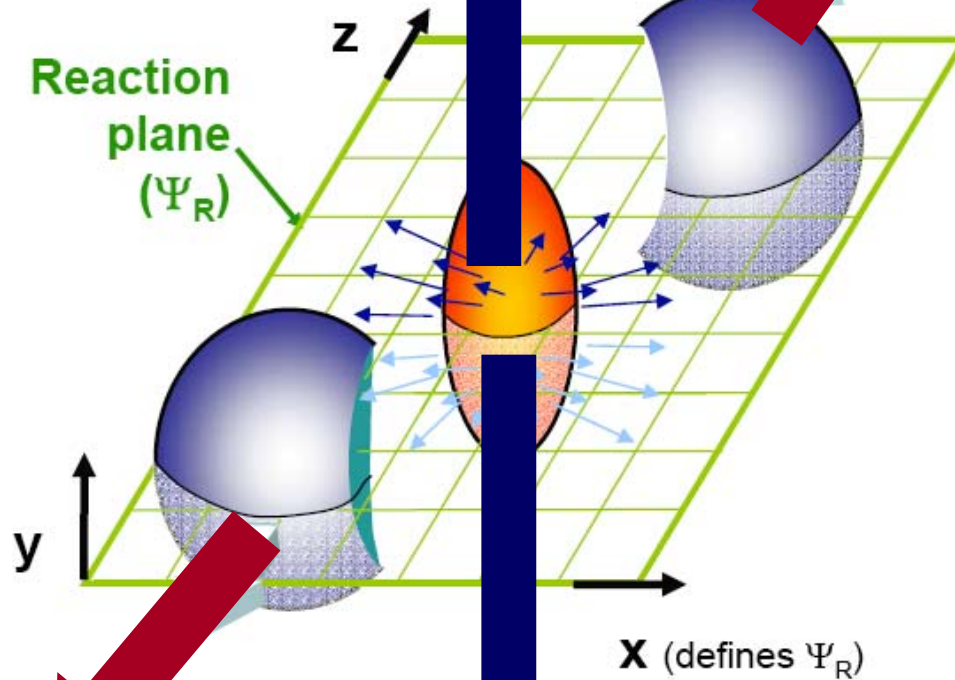


Chiral Magnetic Effect by Fukushima, Kharzeev, Warringa, McLerran

3. Electric current is along magnetic field In the *instanton* field



Magnetic fields in non-central collisions



Two very big currents produce a very

big magnetic field

The medium is filled by electrically charged particles

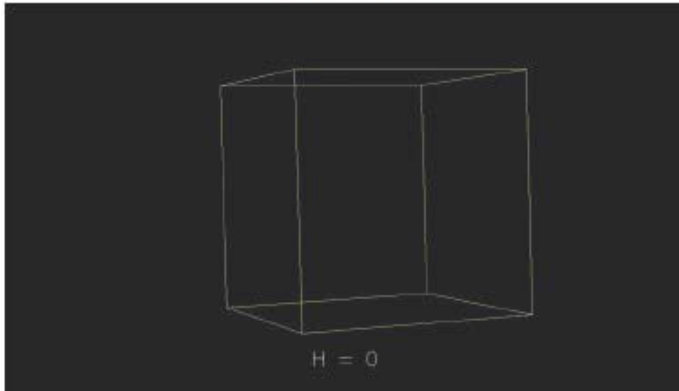
Large orbital momentum, perpendicular to the reaction plane

Large magnetic field along the direction of the orbital momentum

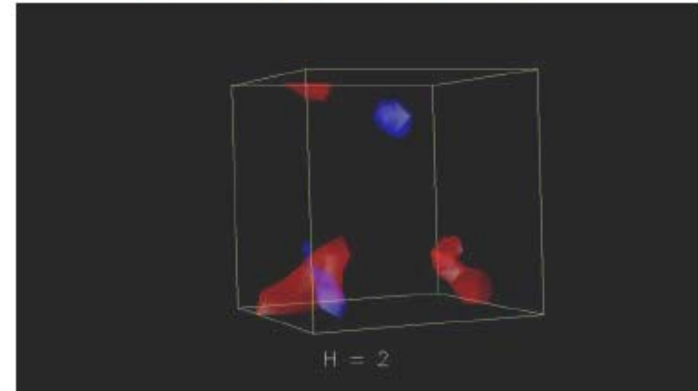
Chiral Magnetic Effect on the lattice, charge separation

Density of the electric charge vs. magnetic field

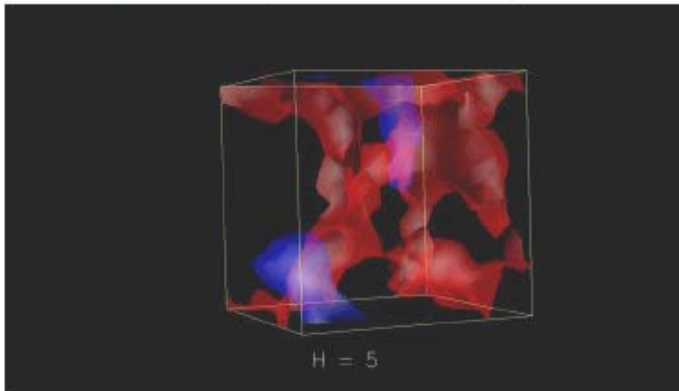
$$B = 0$$



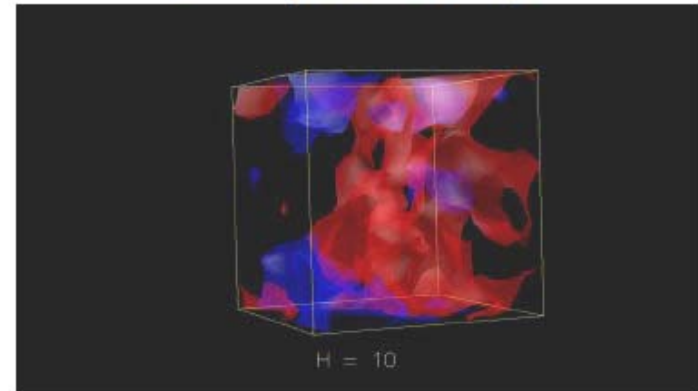
$$B = (500 \text{ MeV})^2$$



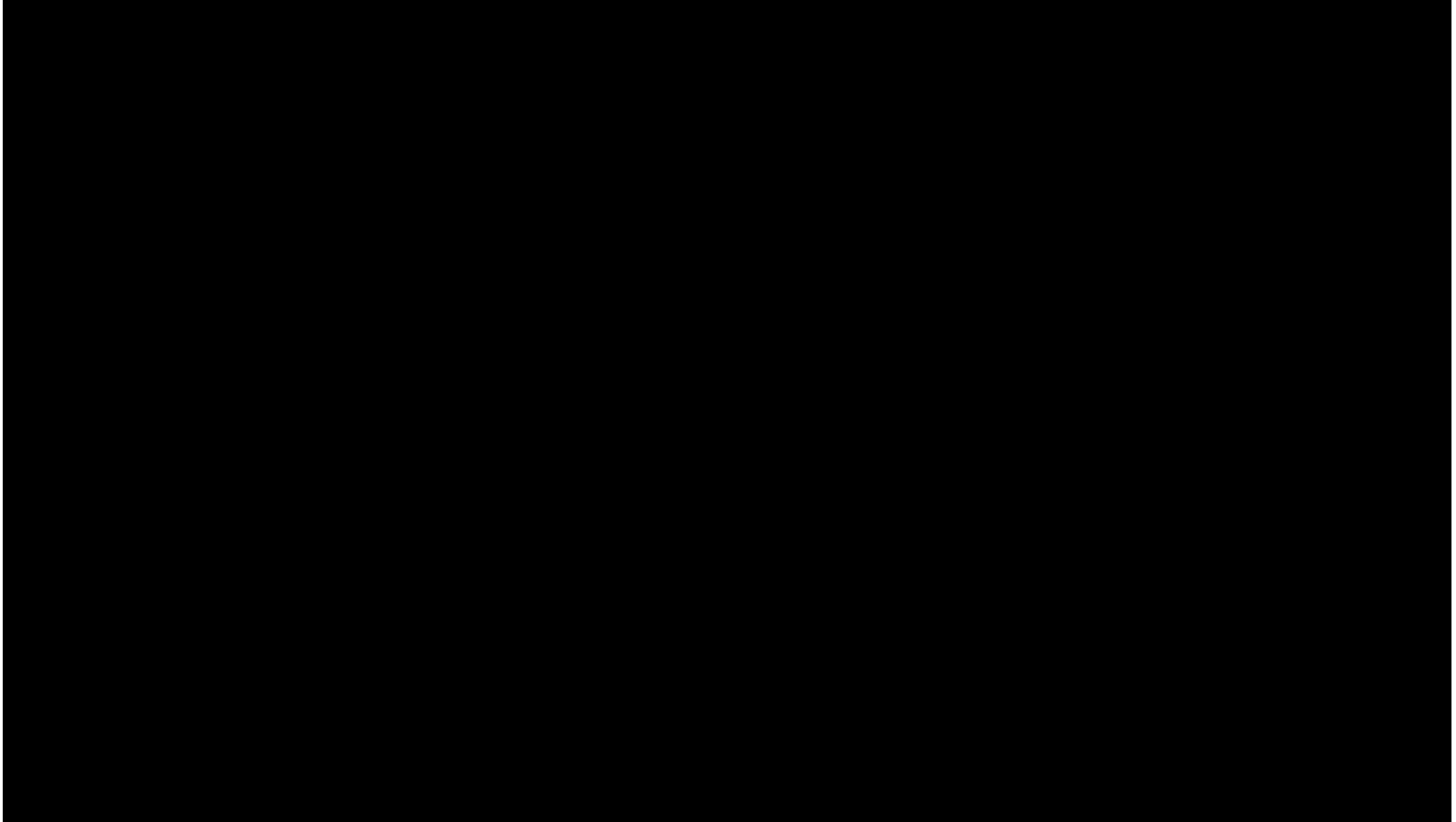
$$B = (780 \text{ MeV})^2$$



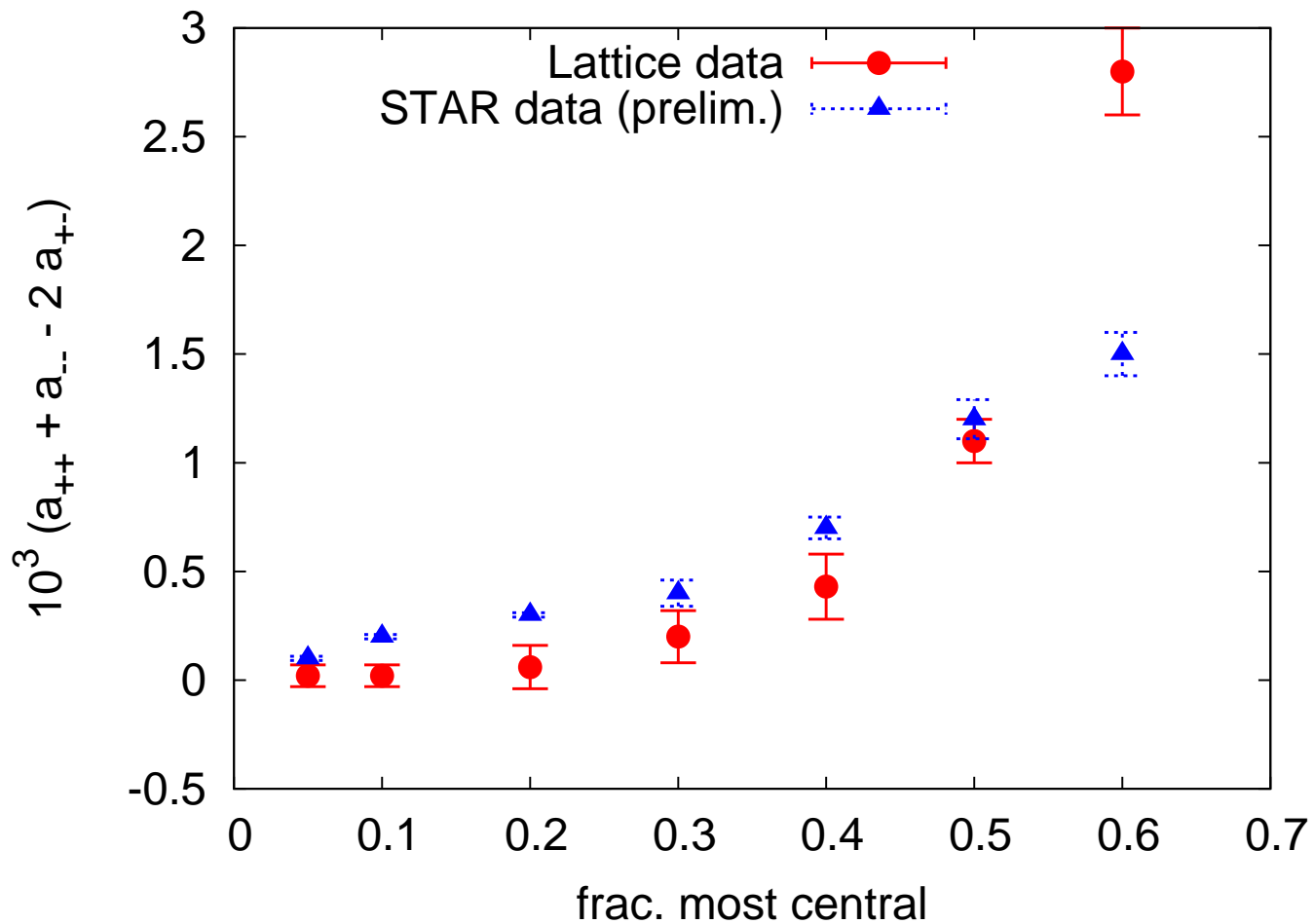
$$B = (1.1 \text{ GeV})^2$$



Chiral Magnetic Effect on the lattice,
Non-zero field, subsequent time slices
Electric charge density



Chiral Magnetic Effect, EXPERIMENT VS LATTICE DATA (Au+Au)



Preliminary results: conductivity of the vacuum

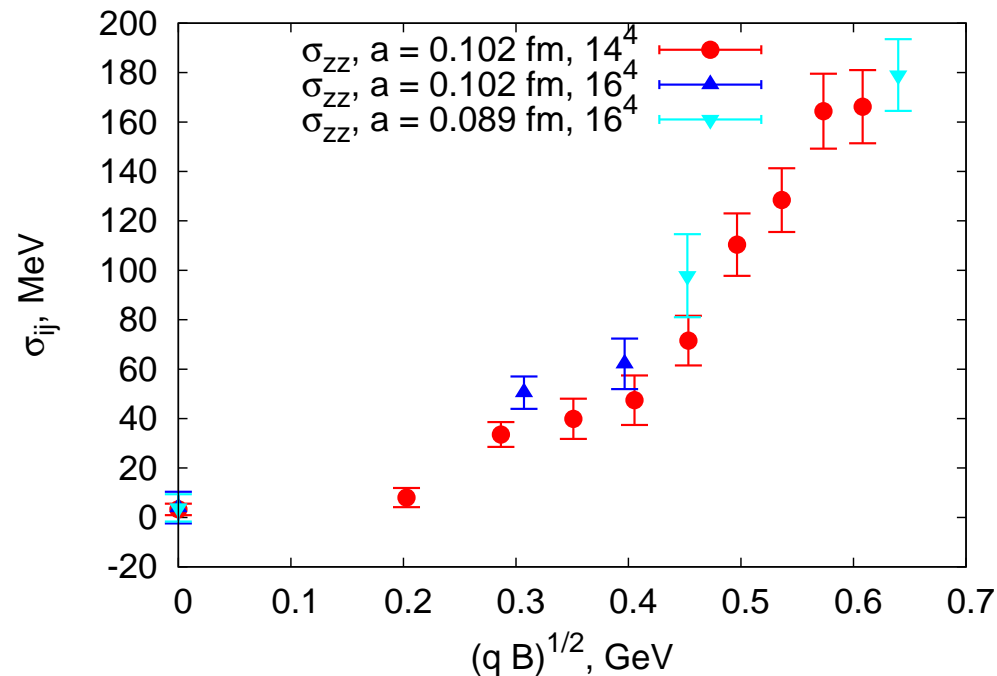
Qualitative definition of conductivity \blacklozenge

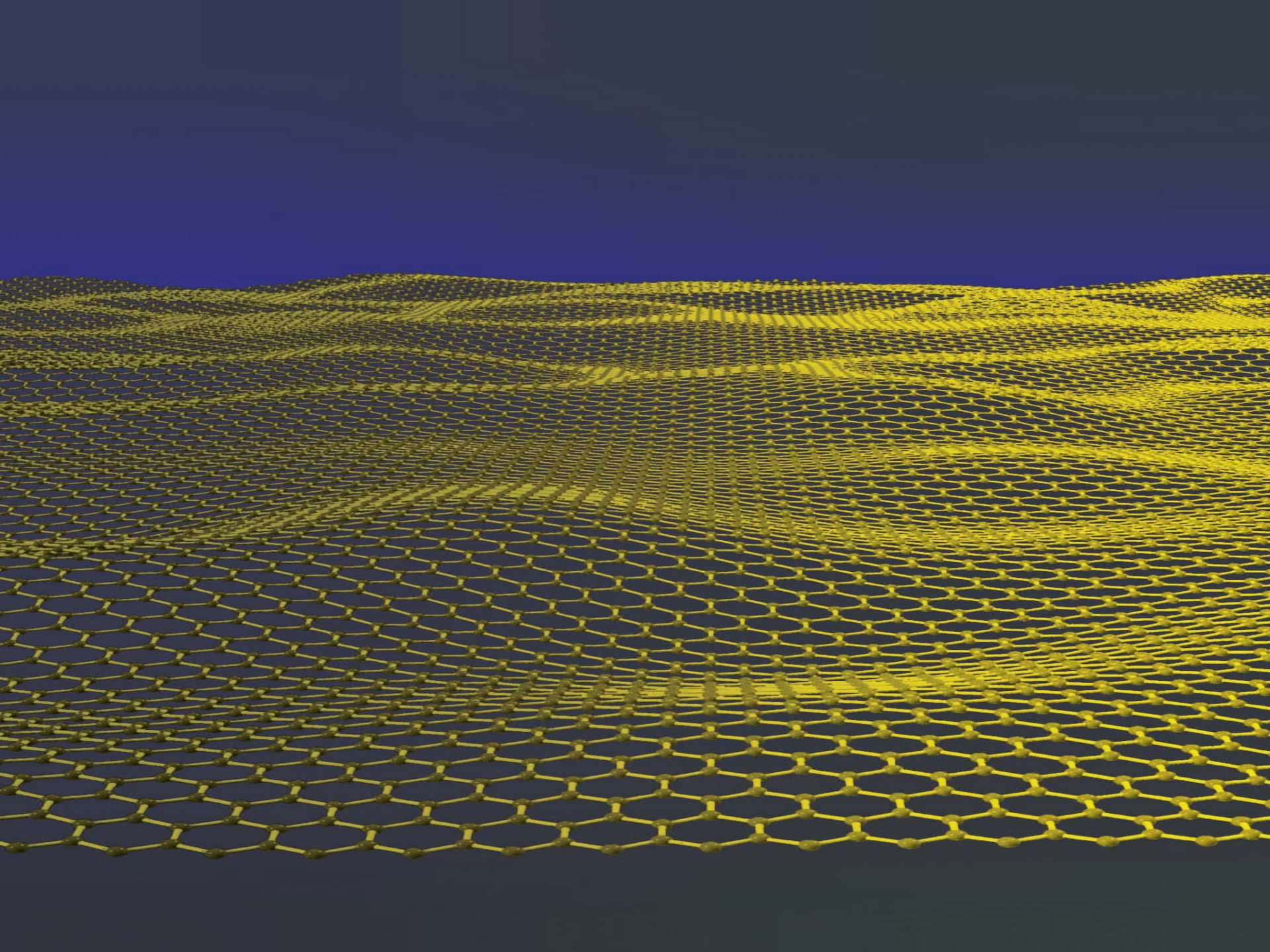
$$\langle j_{\mu}(x) j_{\nu}(y) \rangle = C + A \cdot \exp\{-m|x - y|\}$$

$$\sigma \propto C$$

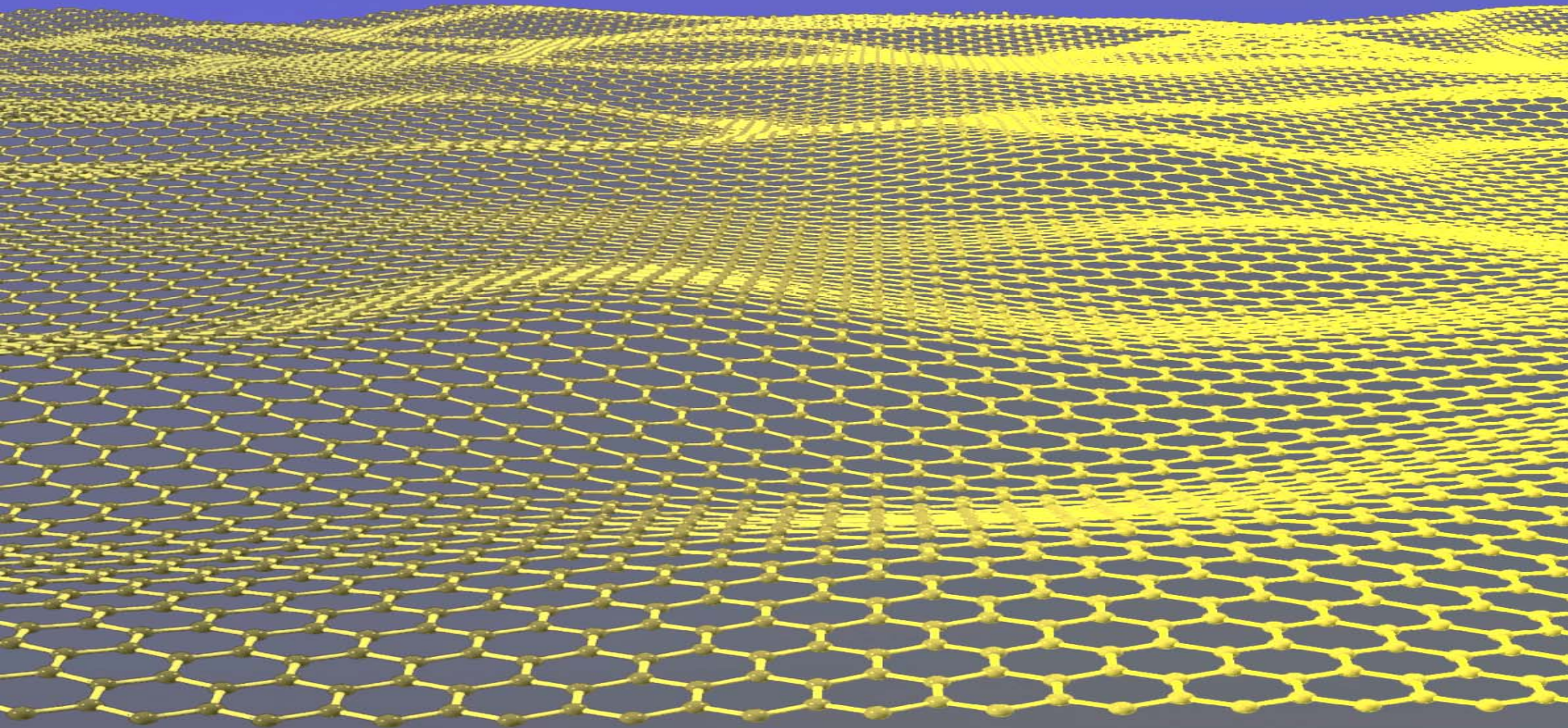
Preliminary results: conductivity of the vacuum

Conductivity at $T > 0$

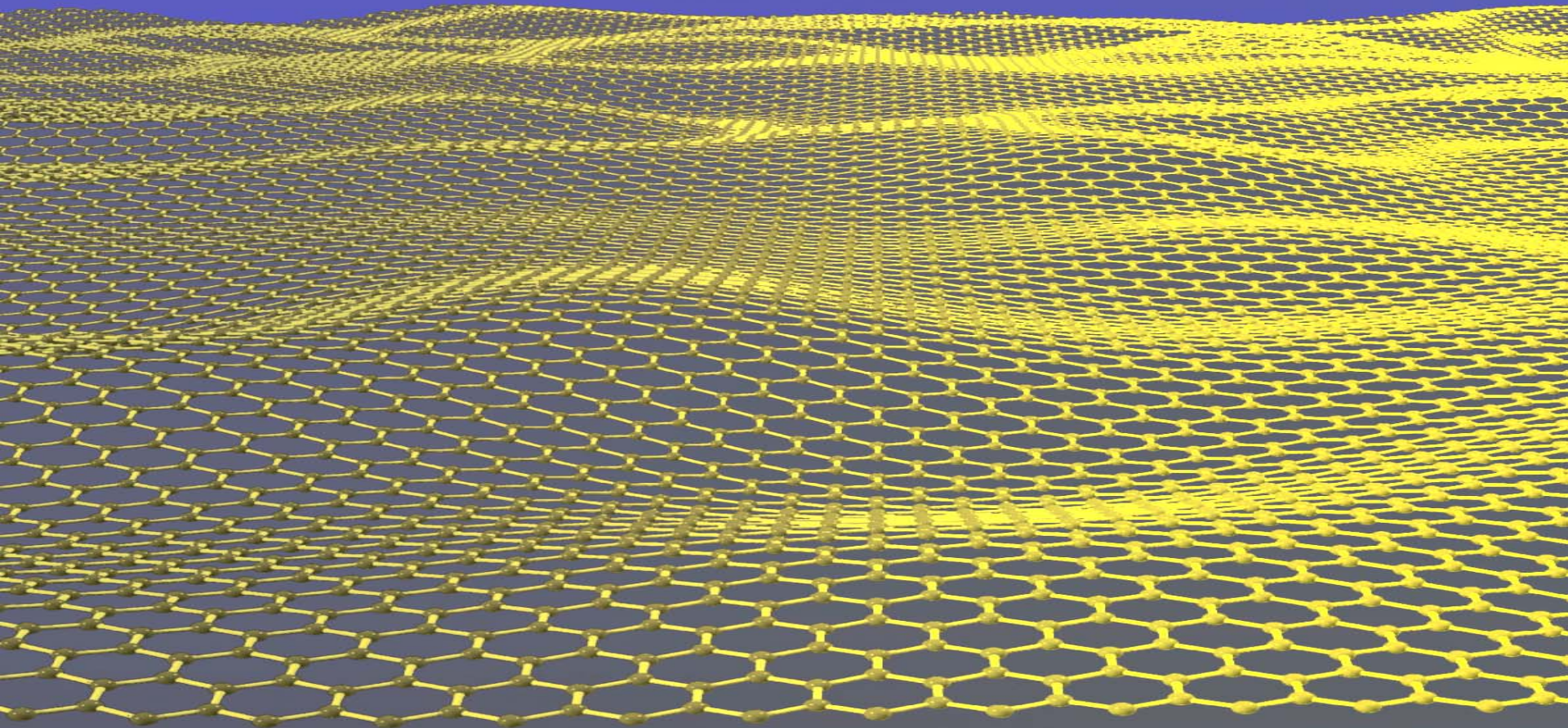




Graphene



**The Nobel Prize in Physics for 2010 was awarded to
Andre Geim and Konstantin Novoselov
"for groundbreaking experiments regarding the
two-dimensional material graphene"**





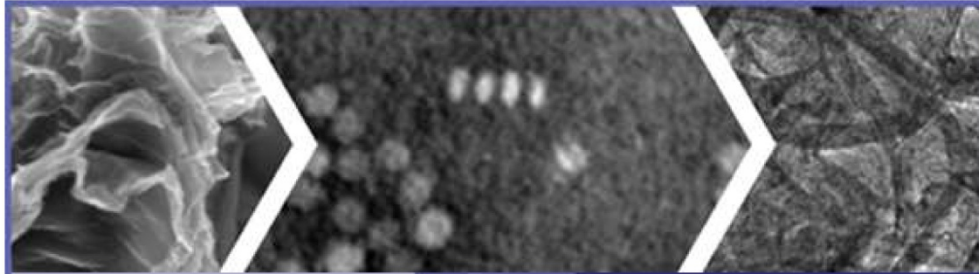
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- Graphene Value Kits
- Graphene Solutions



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Available

Featured products

**Single Layer Graphene on Copper foil: Graphene Nanopowder: 8 nm Flakes- Q-graphene: 1 gram
4"x2" 5 g**





Our price: \$450.00

Quantity 1

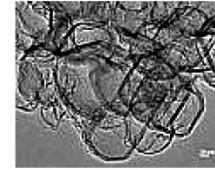
Buy Now



Our price: \$99.00

Quantity 1

Buy Now



Our price: \$100.00

Quantity 1

Buy Now

Reduced Graphene Oxide: 60 mg, Dry Nanopowder



Our price: \$175.00

Quantity 1

Buy Now

Trial pack: 10 CVD Graphene TEM Grids



Our price: \$175.00

Quantity 1

Buy Now

Graphene Oxide Paper



Our price: \$300.00

Quantity 1

Buy Now

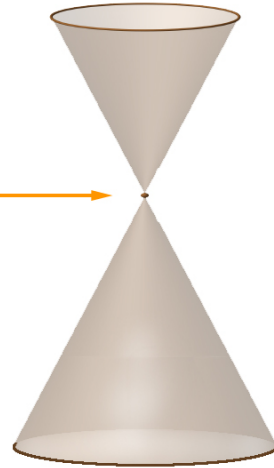
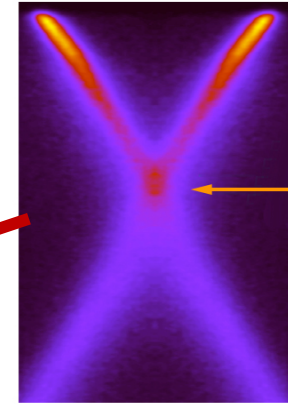
Relativistic particle $E = \sqrt{m^2 c^4 + p^2 c^2}$

Massless particle $E = cp$

Relativistic particle $E = \sqrt{m^2 c^4 + p^2 c^2}$

Massless particle $E = cp$

Graphene $E = v_F p$; $v_F = \frac{c}{300}$;



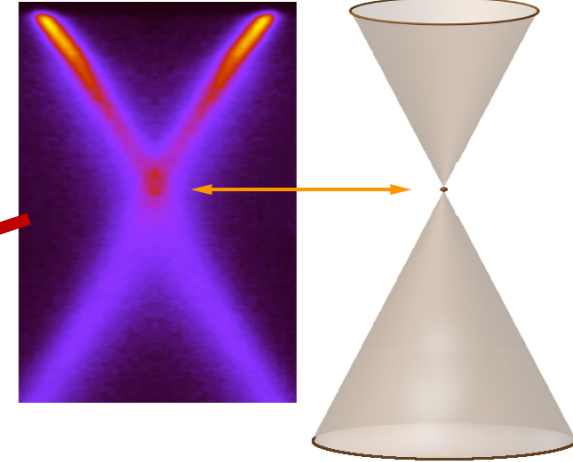
Relativistic particle $E = \sqrt{m^2 c^4 + p^2 c^2}$

Massless particle $E = cp$

Graphene $E = v_F p$; $v_F = \frac{c}{300}$;

$$\alpha_g = 300\alpha = 2.16 > 1$$

$\alpha_g > \alpha_g^{crit} = 1.11 \pm 0.06$ Pure graphene is the insulator!



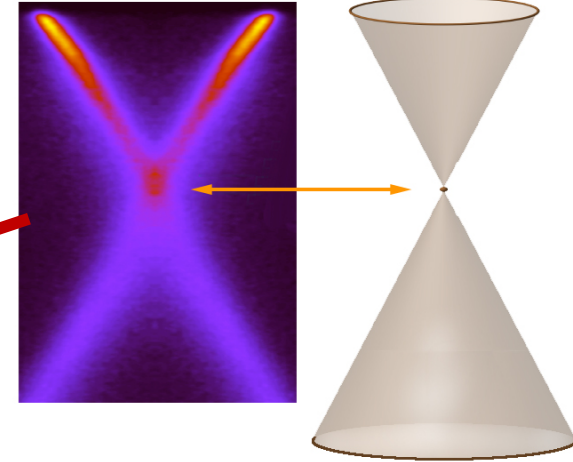
Relativistic particle $E = \sqrt{m^2 c^4 + p^2 c^2}$

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Graphene $E = v_F p$; $v_F = \frac{c}{300}$;

$$\alpha_g = 300\alpha = 2.16 > 1$$

$\alpha_g > \alpha_g^{crit} = 1.11 \pm 0.06$ Pure graphene is the insulator!



If we put graphene on a substrate we can get conductor: $\alpha_g \rightarrow \frac{2}{1+\epsilon} \alpha_g$

Numerical calculation of α_g^{crit}

Is graphene in vacuum an insulator?.

Joaquin E. Drut Timo A. Lahde

e-Print: [arXiv:0807.0834](https://arxiv.org/abs/0807.0834) [cond-mat.str-el],
PRL (2009)

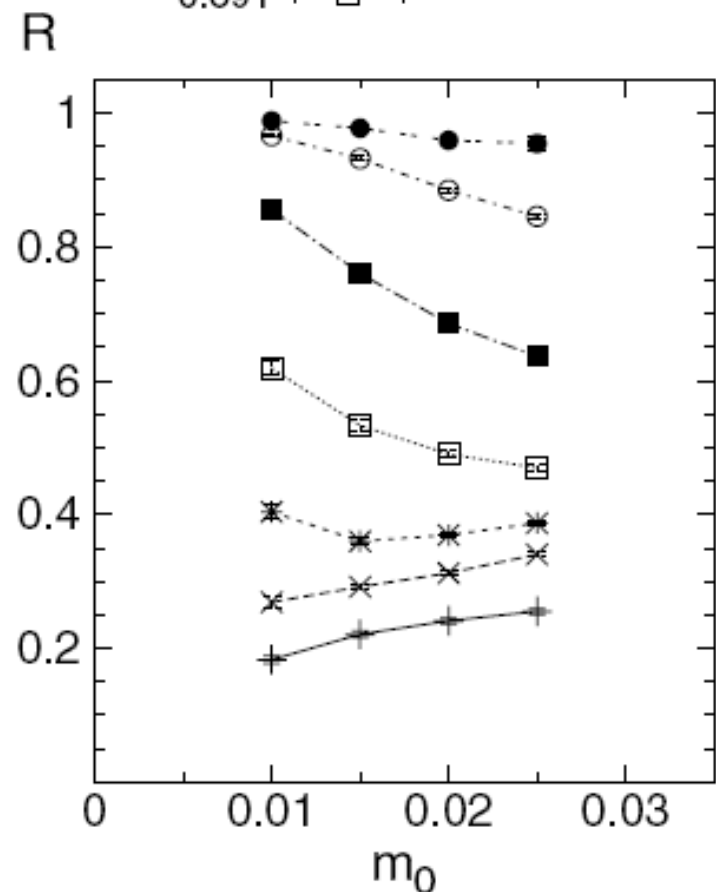
Monte Carlo Simulation of the Semimetal-Insulator
Phase Transition in Monolayer Graphene.

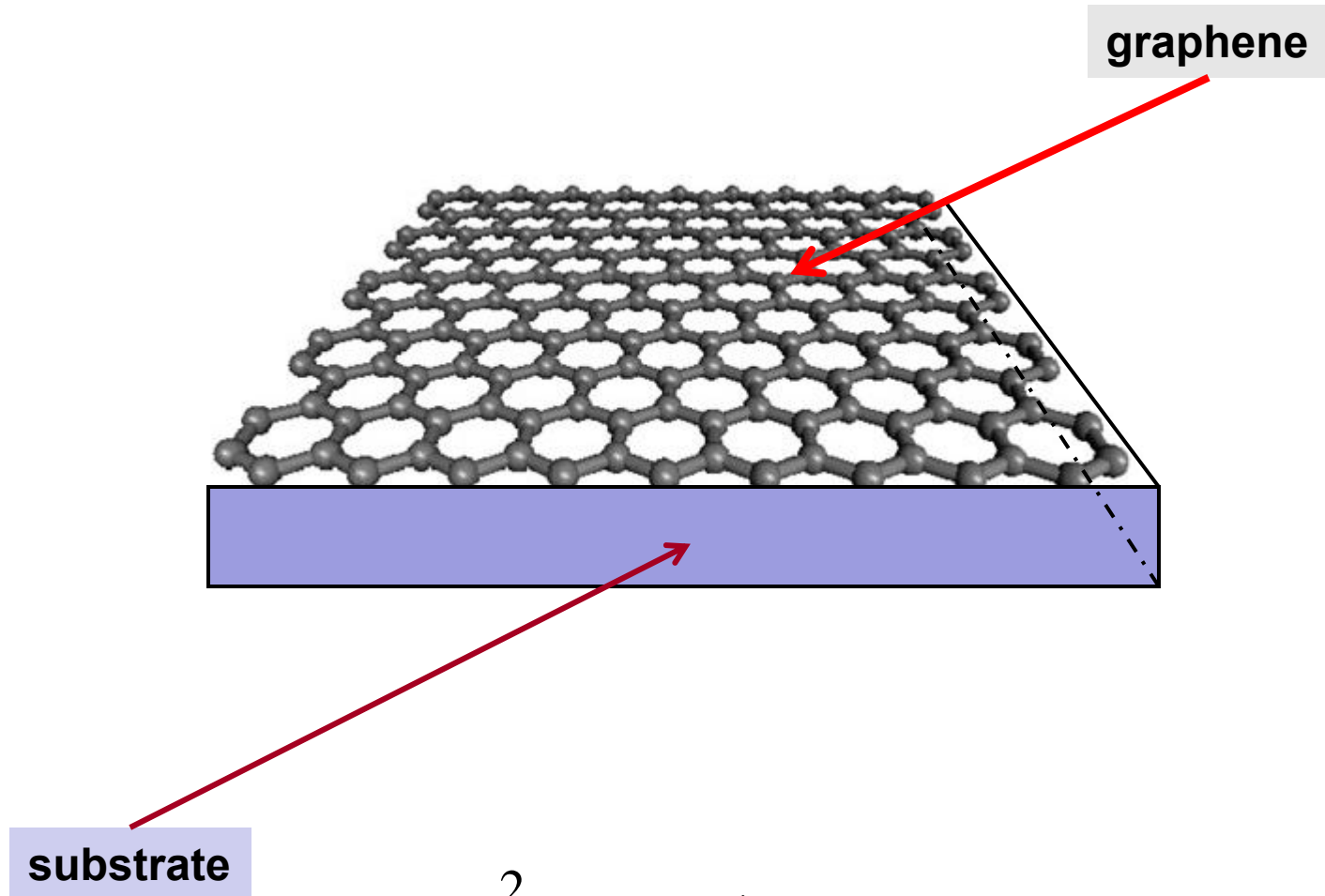
W. Armour , Simon Hands, Costas Strouthos

Published in **Phys.Rev. B81 (2010) 125105**

e-Print: [arXiv:0910.5646](https://arxiv.org/abs/0910.5646) [cond-mat.str-el]

$N_f = 2, \beta = 0.050$ $\text{---}+ \text{---}$ 0.111 $\text{---}\blacksquare \text{---}$
 0.067 $\text{---}\times \text{---}$ 0.143 $\text{---}\ominus \text{---}$
 0.077 $\text{---}\ast \text{---}$ 0.200 $\text{---}\bullet \text{---}$
 0.091 $\text{---}\square \text{---}$

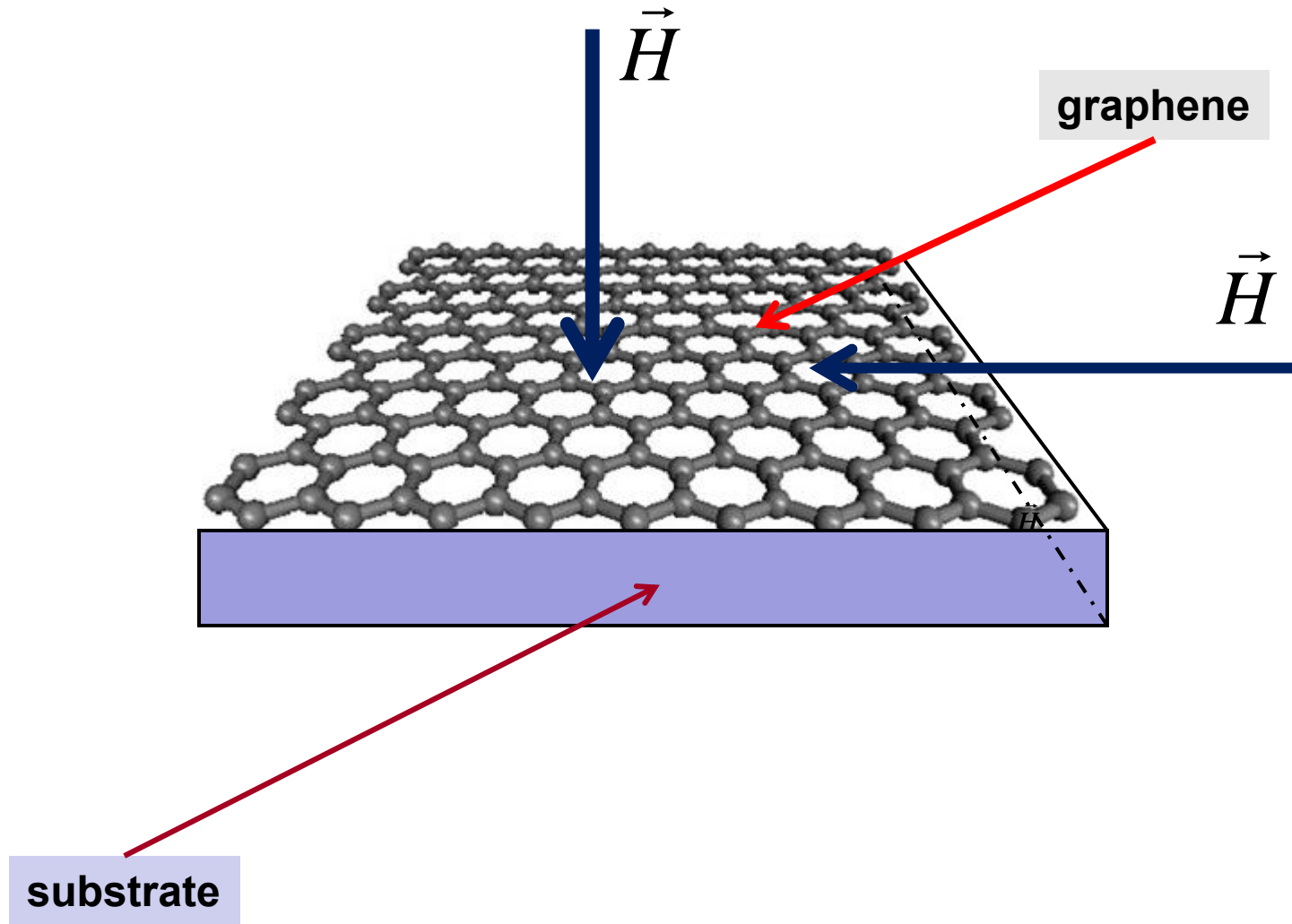




if $\frac{2}{1+\epsilon} \alpha_g > \alpha_g^{crit} (=1.11)$ graphene is the conductor

We can numerically simulate conductor – insulator phase transition!

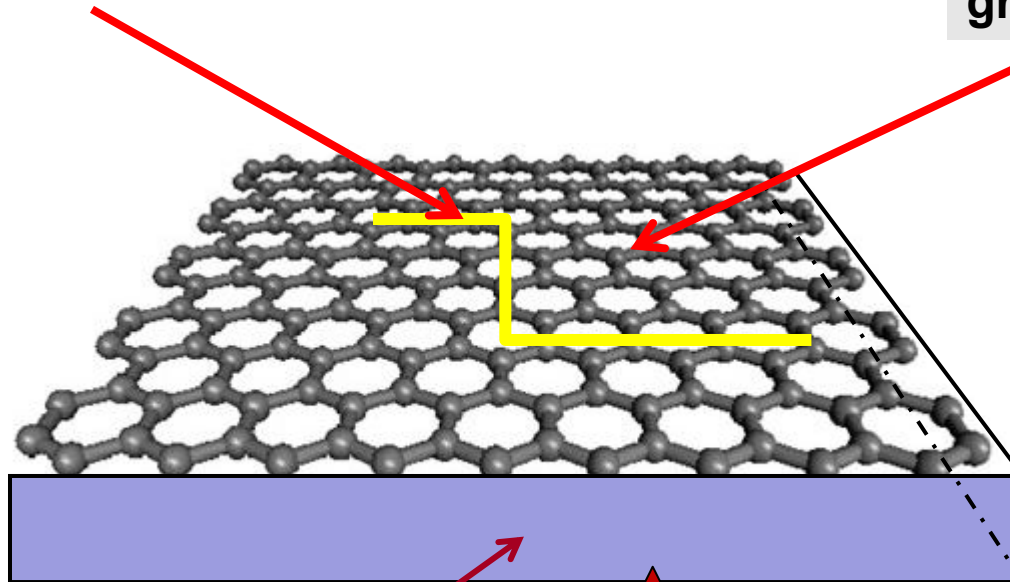
Magnetic Field and Graphene



Graphene changes its properties when an external magnetic field is applied, we can numerically simulate all that

Trajectory of the magnetic head

graphene



Ferromagnetic substrate

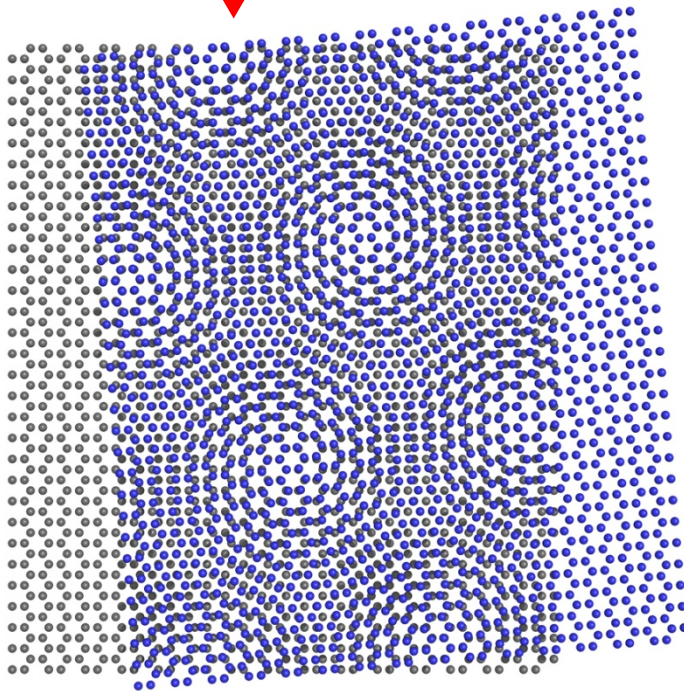
magnetic head

Along the trajectory of the magnetic head graphene becomes the conductor!

We can draw (construct) chips! All that we can simulate on computers

Problems for graphene numerical simulations

Magnetic field
Finite temperature
Impurities
2-3-4 layers
Conductivity
Viscosity – Entropy
Optical properties
Critical indices



Monte Carlo simulation of monolayer graphene at non-zero temperature

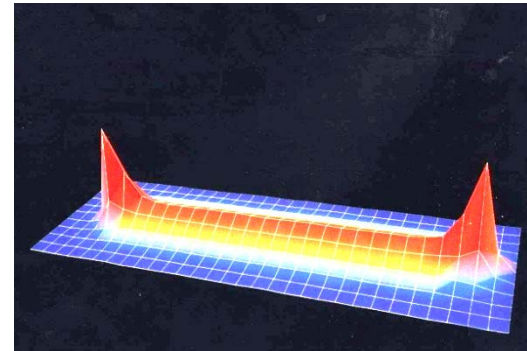
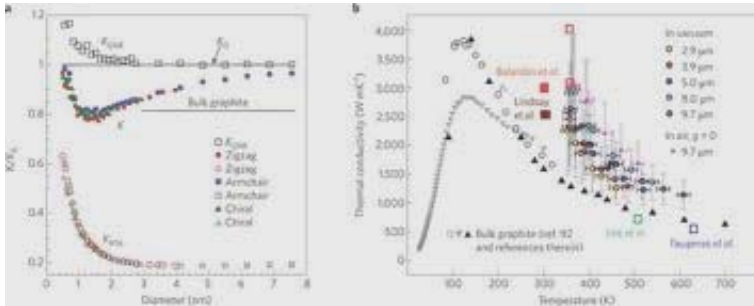
Wesley Armour^{a,b}, Simon Hands^c, and Costas Strouthos^d

arXiv:1105.1043v1 [cond-mat.str-el] 5 May 2011

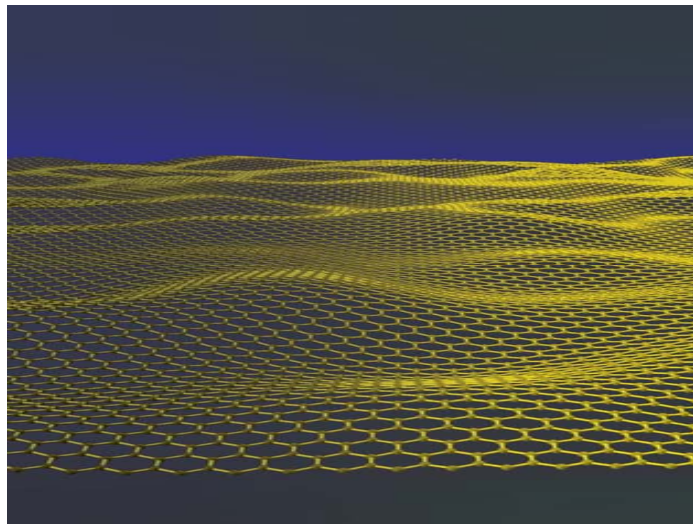
Graphene has relations with many theoretical problems

Insulator – Conductor

Confinement - Deconfinement



Curvature of the graphene leads to two dimensional gravity for fermions



Computer simulations help to unify physical systems

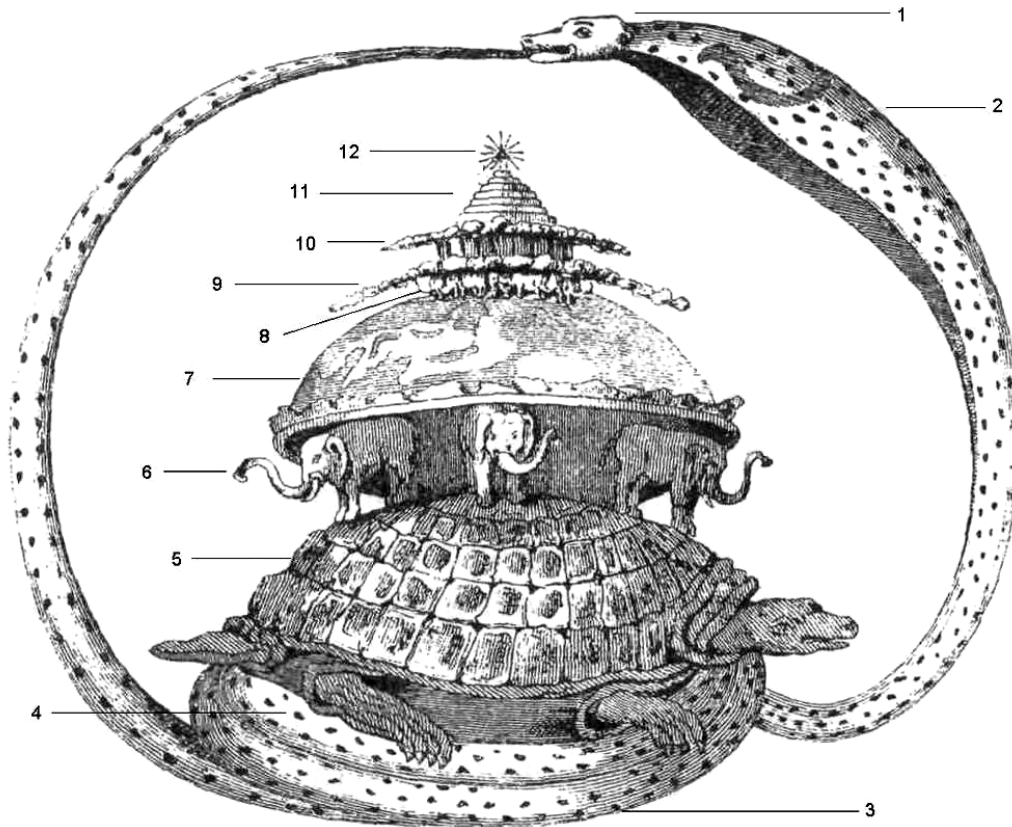
Computer simulations help to unify physical systems

QCD confinement problems

Quark-Gluon plasma in heavy ion collisions

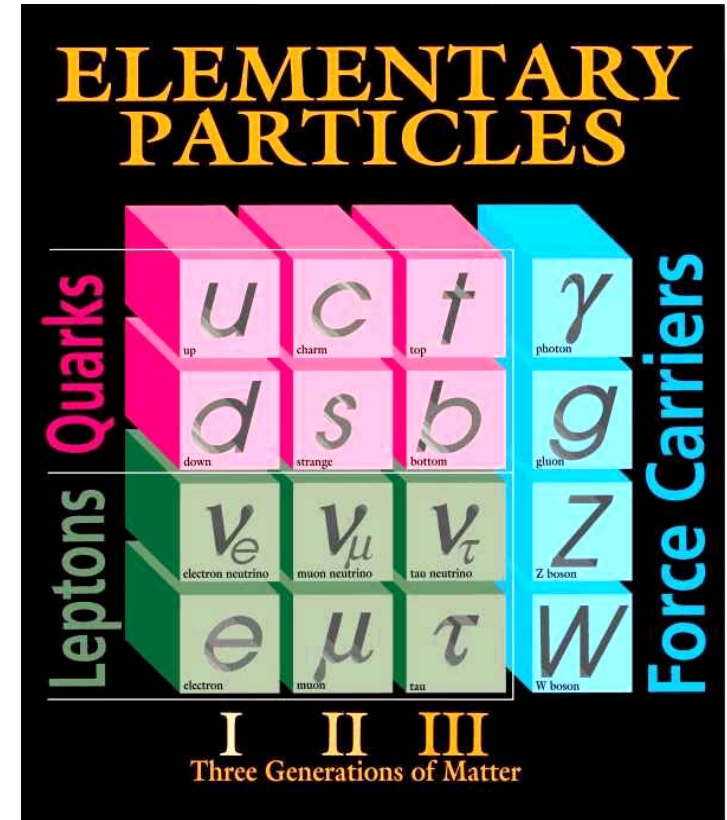
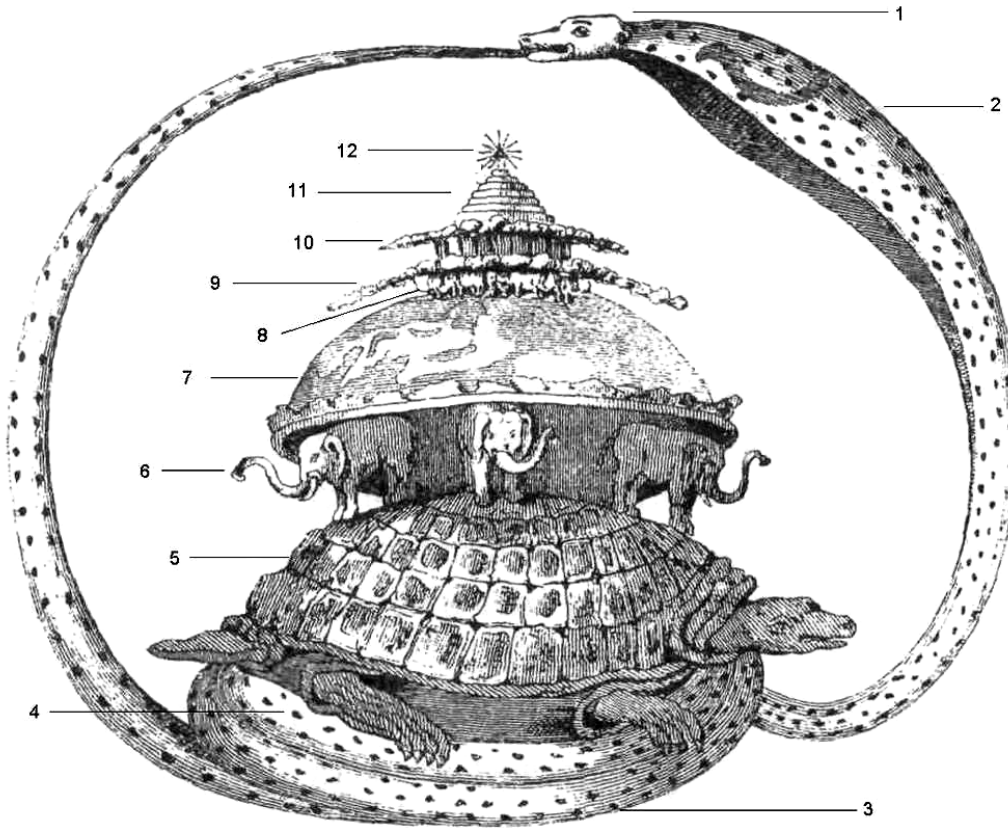
Graphene

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Fermilab 95-759

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