

On the theory of dust ionization waves in the gas discharge complex plasma

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Observation of the dust ionization waves (DIW) under microgravity conditions (PK-4 facility on board the International Space Station, polarity-switching dc discharge)

Naumkin V.N., Zhukhovitskii D.I., Lipaev A.M., Zobnin A.V., Usachev A.D., Petrov O.F., Thomas H.M., Thoma M.H., Skripochka O.I., and Ivanishin A.A. *Excitation of progressing dust ionization waves on PK-4 facility.* // Physics of Plasmas, 2021, vol. 28, no. 10, pp. 103704-1–103704-12.



Master equations

$$\begin{split} &\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} = -\frac{c_a^2}{n_d} \frac{\partial n_d}{\partial x} + \frac{Ze}{M} \frac{\partial \varphi}{\partial x}, \\ &\frac{\partial n_d}{\partial t} + \frac{\partial}{\partial x} (un_d) = 0, \\ &\frac{\partial \varphi}{\partial x} = \frac{T_e}{en_e} \frac{\partial n_e}{\partial x}, \\ &D \frac{\partial}{\partial x} \left(\frac{T_e}{T_i} \frac{n_i}{n_e} \frac{\partial n_e}{\partial x} + \frac{\partial n_i}{\partial x} \right) = Rn_d n_i - Kn_a n_e, \\ &Rn_{d0} n_{i0} = Kn_a n_{e0}, \\ &\frac{\partial^2 \varphi}{\partial x^2} = 4\pi e(Zn_d + n_e - n_i). \end{split}$$

Linearized equations

$$\begin{split} \frac{\partial u}{\partial t} &= -\frac{c_a^2}{n_{d0}} \frac{\partial n_d'}{\partial x} + \frac{Ze}{M} \frac{\partial \varphi}{\partial x}, \\ \frac{\partial n_d'}{\partial t} &+ n_{d0} \frac{\partial u}{\partial x} = 0, \\ \frac{\partial \varphi}{\partial x} &= \frac{T_e}{e n_e} \frac{\partial n_e'}{\partial x}, \\ D \frac{T_e}{T_i} \frac{n_{i0}}{n_{e0}} \frac{\partial^2 n_e'}{\partial x^2} &= R n_{d0} n_i' + R n_{i0} n_d' - K n_a n_e', \\ n_i' &= n_e' + Z n_d' \quad \text{if} \quad k r_{De} \gg 1, \ r_{De} &= (T_e / 4 \pi n_{e0} e^2)^{1/2}. \end{split}$$

Dispersion relation (DR)

$$\begin{split} \alpha^2 \tilde{k}^4 &- \left(\alpha^2 - 1 + \tilde{\omega}^2\right) \tilde{k}^2 + \tilde{\omega}^2 = 0 \quad \text{or} \\ \tilde{\omega}(\tilde{k}) &= \sqrt{\alpha^2 \tilde{k}^2 + 1} + \frac{1}{\tilde{k}^2 - 1}, \quad \tilde{k}_{\min} = \sqrt{\frac{\tilde{\omega}_{\min}}{\alpha}}, \\ \tilde{k} &= k / k_d, \, \omega = \tilde{\omega} / \omega_d, \, \alpha = \omega_a / \omega_d = c_a / c_d, \\ k_d^2 &= \frac{H}{(1 + H)^2} \frac{K n_a}{D} \frac{T_i}{T_e}, \\ \omega_d^2 &= \frac{1 + 2H}{(1 + H)^2} v_d^2 \frac{Z K n_a}{D} \frac{T_i}{T_e}, \\ c_d^2 &= \left(\frac{\omega_d}{k_d}\right)^2 = \frac{1 + 2H}{H} Z v_d^2, \quad v_d^2 = T_e / M. \end{split}$$

Obtained DR corresponds to two modes, LW and SW

The phase velocity is
$$c_{\rm ph} = c_d \frac{\tilde{\omega}}{\tilde{k}} = \sqrt{\alpha^2 + \frac{1}{\tilde{k}^2} + \frac{1}{\tilde{k}^2(\tilde{k}^2 + 1)}}$$

the group velocity is $c_{\rm gr} = c_d \frac{d\tilde{\omega}}{d\tilde{k}} = \frac{c_d^2}{c_{\rm ph}} \left[\alpha^2 - \frac{1}{(\tilde{k}^2 - 1)^2} \right].$

For LW mode, k is almost independent of ω :

$$ilde{k}\simeq 1+rac{1}{2}ig(ilde{\omega}^2-lpha^2-1ig)^{\!-1}, \;\; ilde{\omega}
ightarrow\infty.$$

For SW mode, k is almost proportional to ω : $\tilde{\omega} \simeq \sqrt{\alpha^2 \tilde{k}^2 + 1}$.

 $\begin{array}{ll} \mbox{The LW group velocity is} & c_{\rm gr} = -c_d (\omega \,/\, \omega_d)^3 = -\omega^3 \,/\, c_d^2 k_d^3, \\ \mbox{the DAW velocity is} & \tilde{\omega} \simeq \sqrt{\alpha^2 \tilde{k}^2 + 1}. \end{array}$

Wave number vs. the excitation frequency for the DIW (long-wave) mode (experiment and theory)



Wave number vs. the excitation frequency for the dust acoustic waves (DAW, short-wave mode)



Wave number vs. the excitation frequency for the DIW and DAW (LW and SW modes)



Thank you for your attention!

For more details, visit http://oivtran.ru/dmr

